

# Chirality and wobbling: new achievements and perspectives

## Three successful experiments

### RITU + JUROGAM II – 2016 (B. F. Lv)

$^{135}\text{Nd}$ ,  $^{136}\text{Nd}$ ,  $^{137}\text{Nd}$  – multiple chiral bands

$^{135}\text{Nd}$  – Wobbling at low spin **NO**

$^{136}\text{Nd}$  – Wobbling 2qp at high spin **YES** (F.Q. Chen)

### GALILEO + EUCLIDES + N WALL – 2017 (S. Guo)

$^{130}\text{Ba}$  – Wobbling 2qp **YES** (Q. B. Chen, Y. X. Liu)

$^{131}\text{Ba}$  – chiral bands+octupole correlations

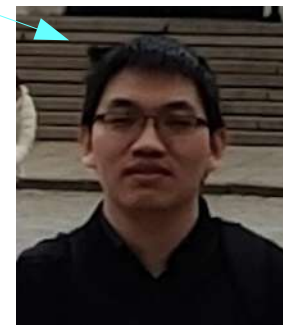
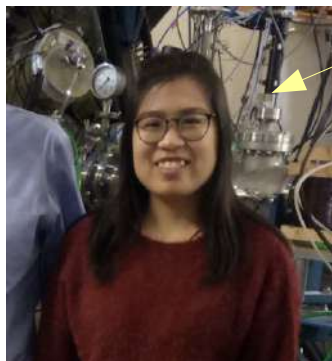
### MARA + JUROGAM III – 2019 (K. K. Zheng)

$^{119}\text{Cs}$  – electric revolving chirality

$^{119}\text{Cs}$  – prolate-oblate shape coexistence

$^{119}\text{Ba}$  – neutron 1-qp configurations

$^{118}\text{Cs}$  – isomers at the proton-drip line



# JUROGAM II + RITU, $^{40}\text{Ar} + ^{100}\text{Mo} \rightarrow \text{Nd}$ 20 pnA (1 week, October 2016)

## JUROGAM II

24 Clovers HPGe

15 Coaxial HPGe

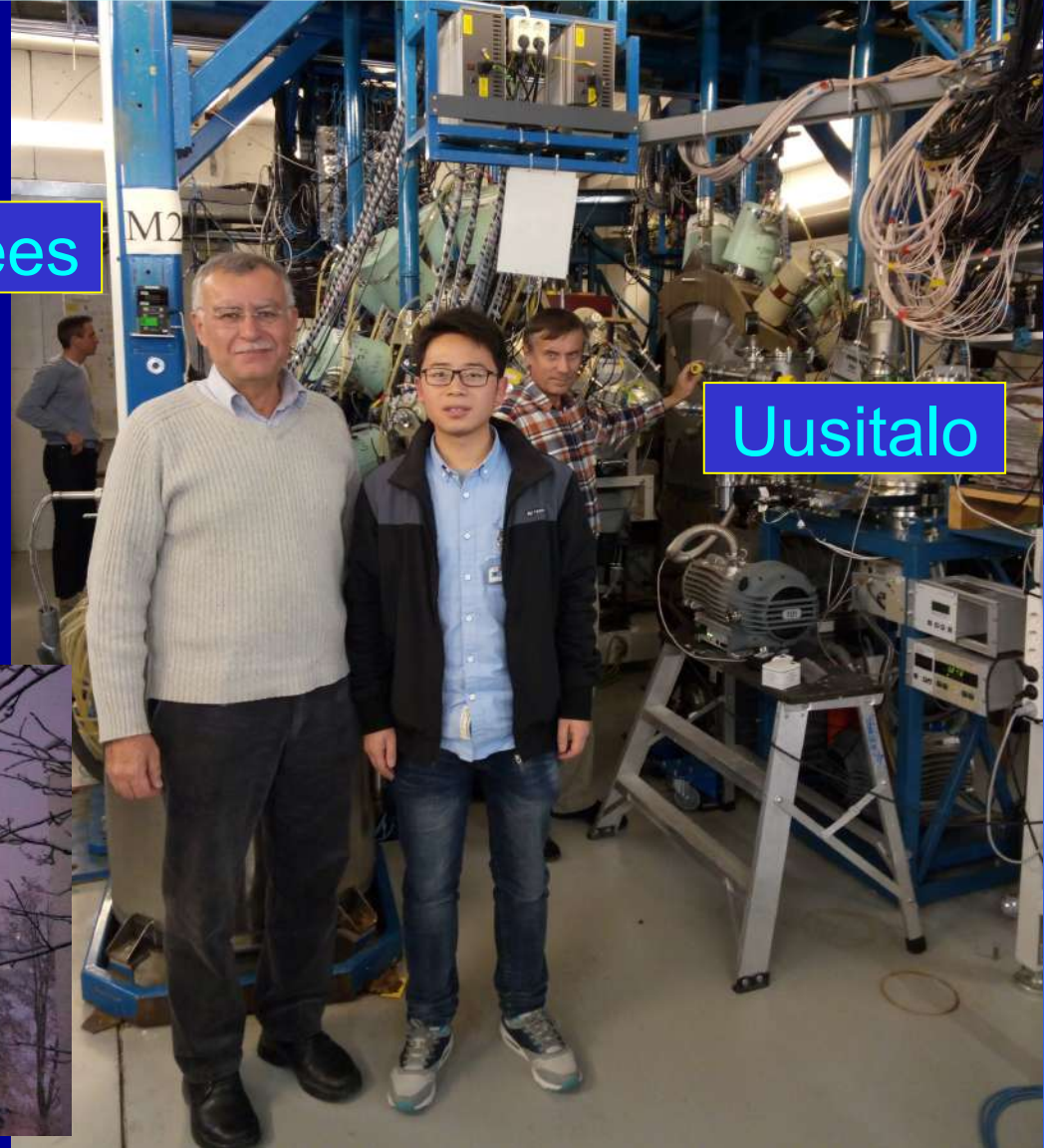
39 BGO shields

$\varepsilon_{\text{tot}} = 4\%$

## RITU

Greenlees

Uusitalo



# MARA + JUROGAM 3, $^{64}\text{Zn} + ^{58}\text{Ni} \rightarrow \text{Cs, Ba, LA}$ (3 days, May 2019)

MARA

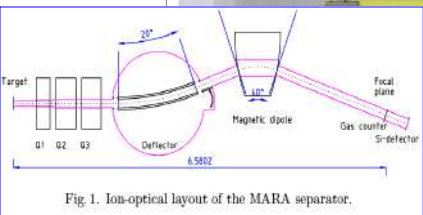
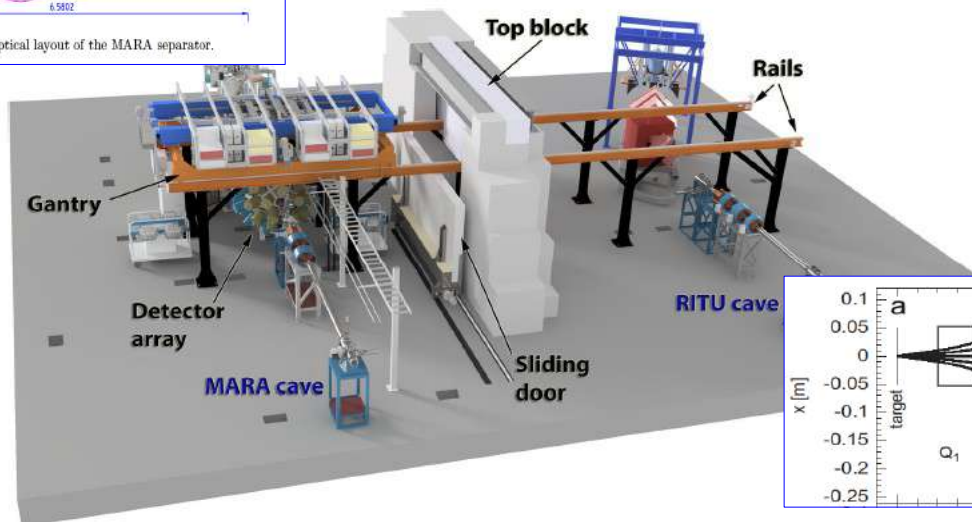
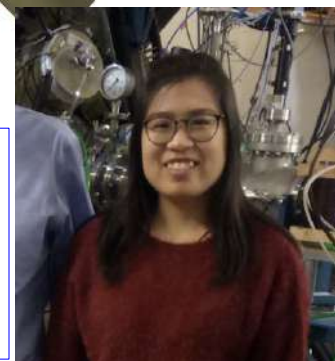
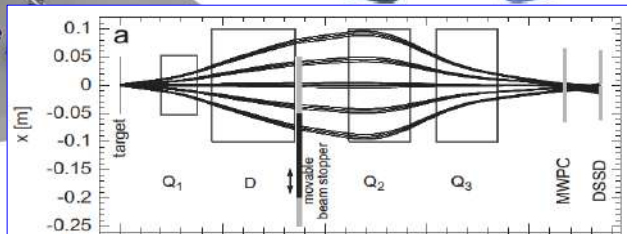
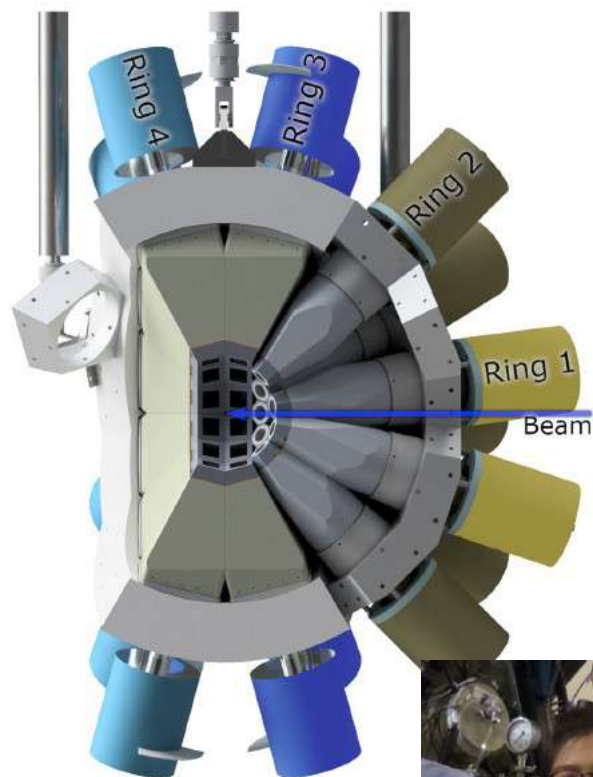


Fig. 1. Ion-optical layout of the MARA separator.

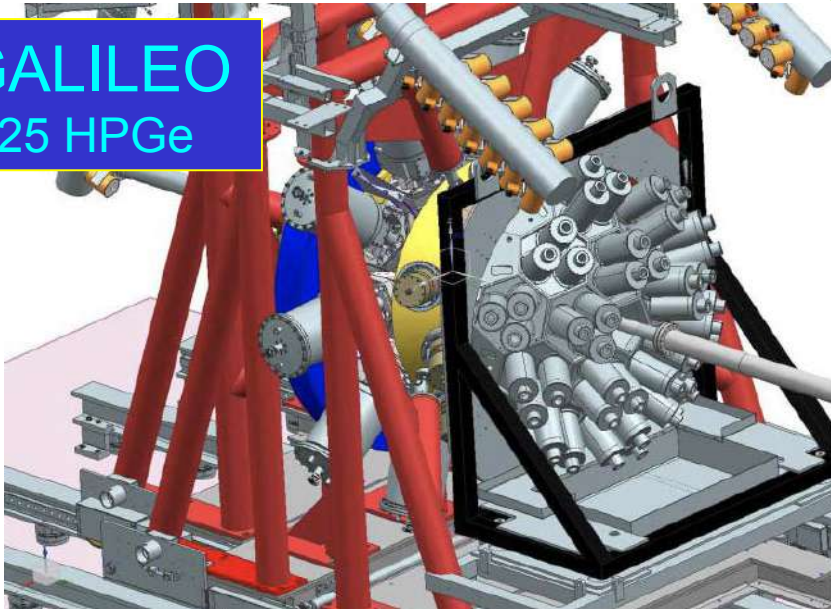


JUROGAM 3

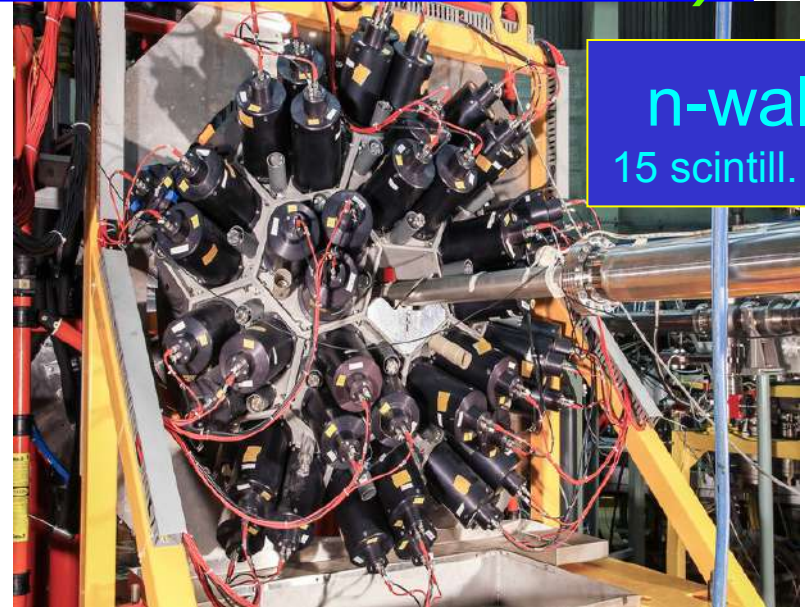


# GALILEO + EUCLIDES + n wall, $^{13}\text{C} + ^{122}\text{Sn} \rightarrow \text{Ba}$ (1 week, March 2017)

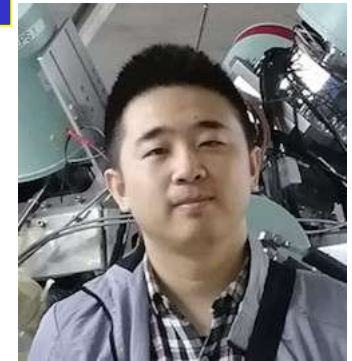
GALILEO  
25 HPGe



n-wall  
15 scintill. det.



EUCLIDES  
40  $\Delta E-E$





# Chirality

## Triaxiality

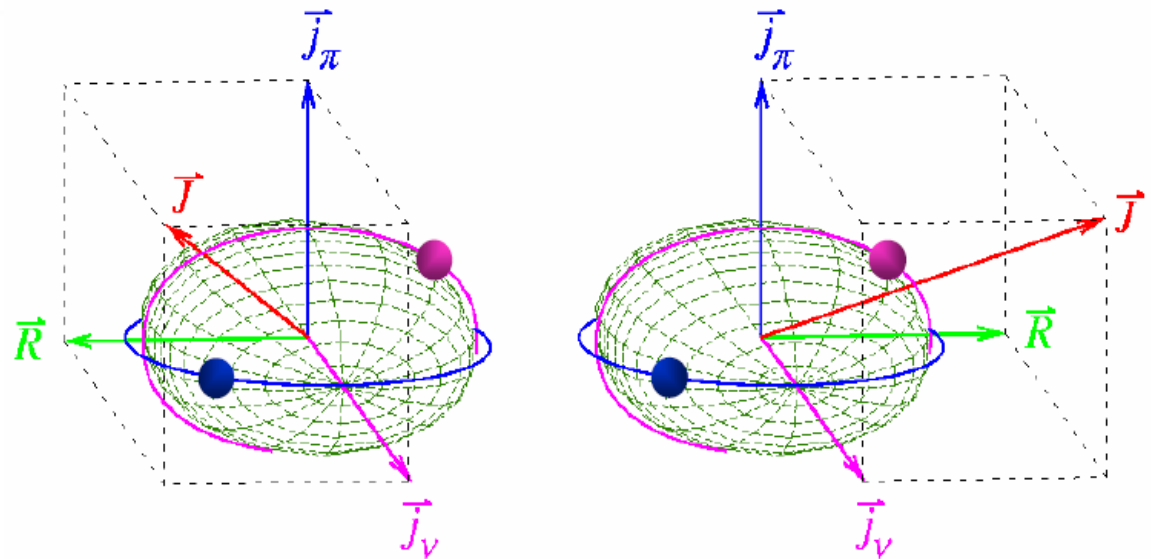
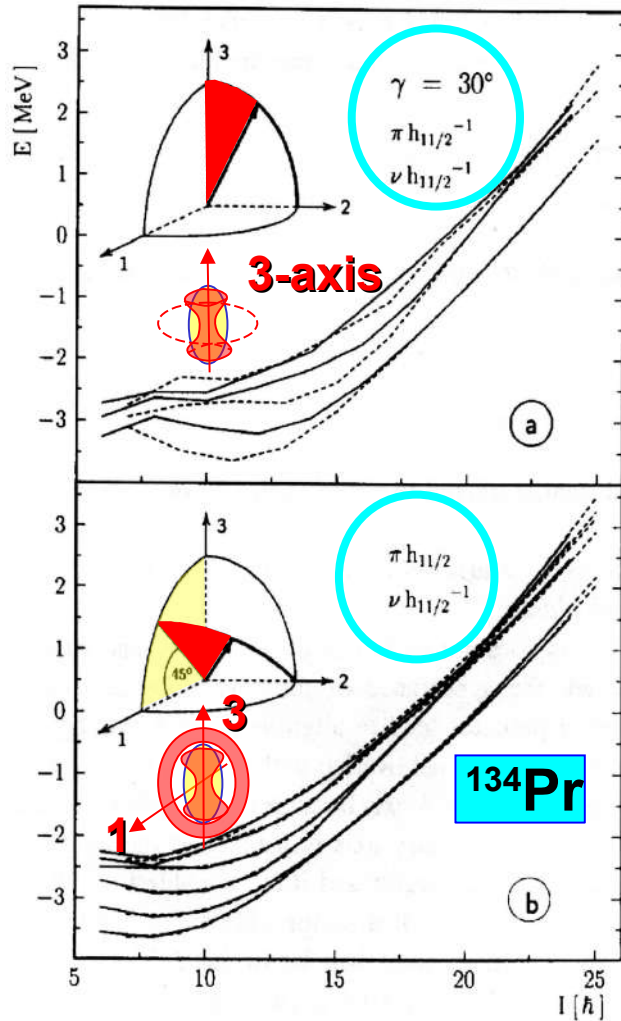


Frauendorf & Meng, NPA 617, 1997

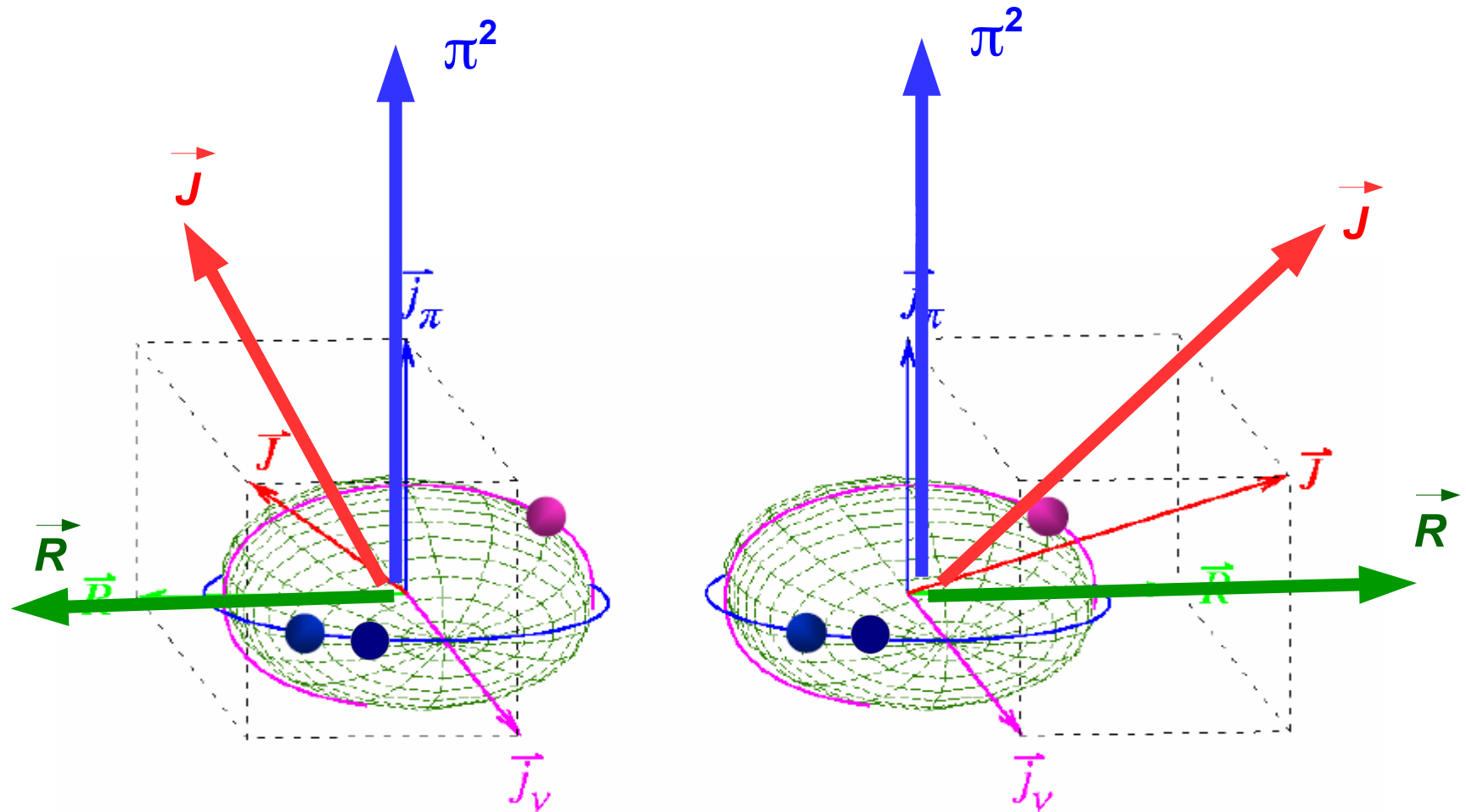
C.P. et al, NPA 597, 1996

### Chiral Geometry in Nuclei

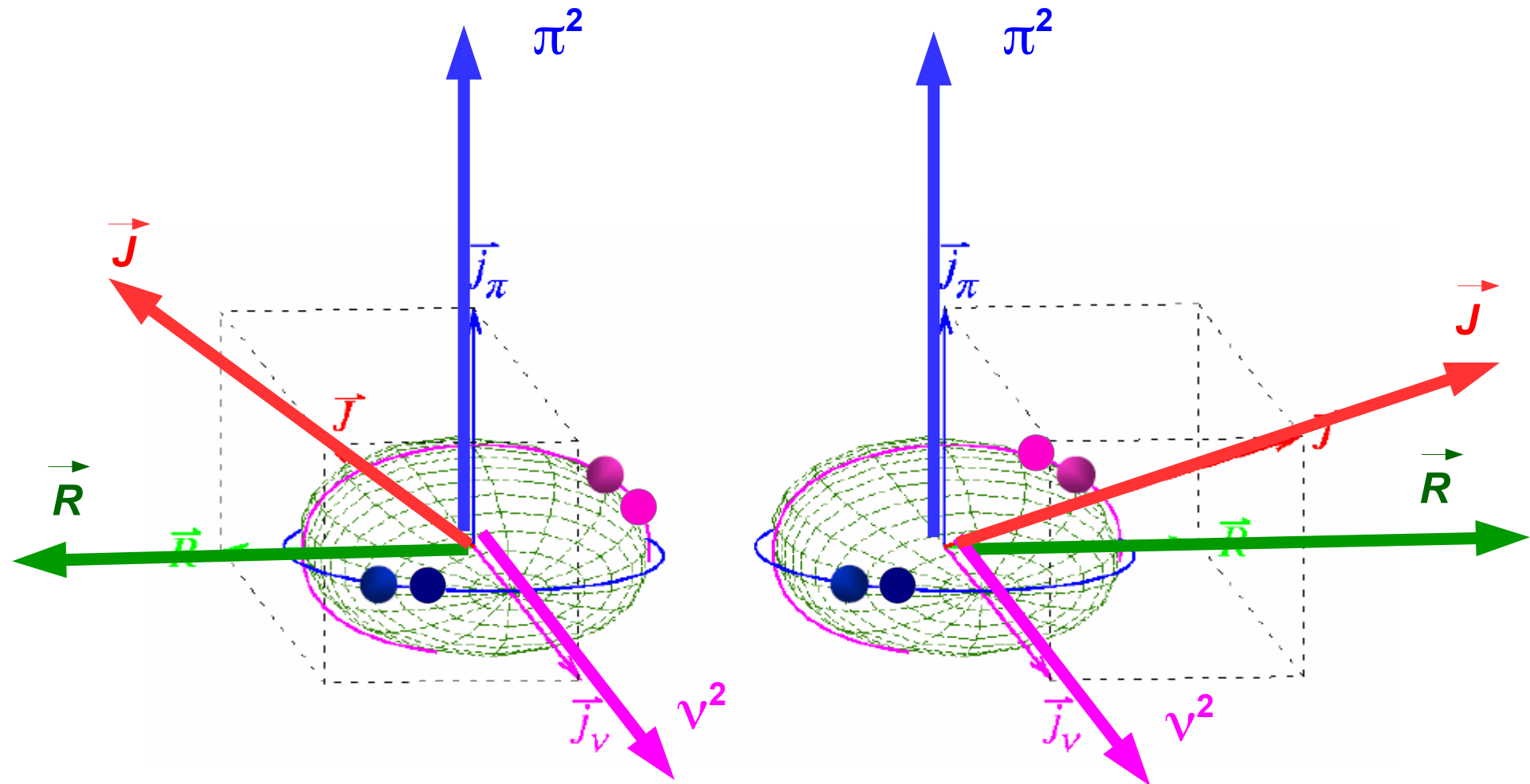
Mutually orthogonal coupling of three angular momenta in odd-odd nuclei



# Chirality in odd-even nuclei: 3-qp configurations



# Chirality in even-even nuclei: 4-qp configurations



Y. X. Luo, et al. - PLB 670 (2009) 307

$^{110,112}\text{Ru}$  - Many of the experimental findings can be explained by microscopic calculations that combine the TAC mean-field with RPA but a simple geometrical explanation is not apparent.

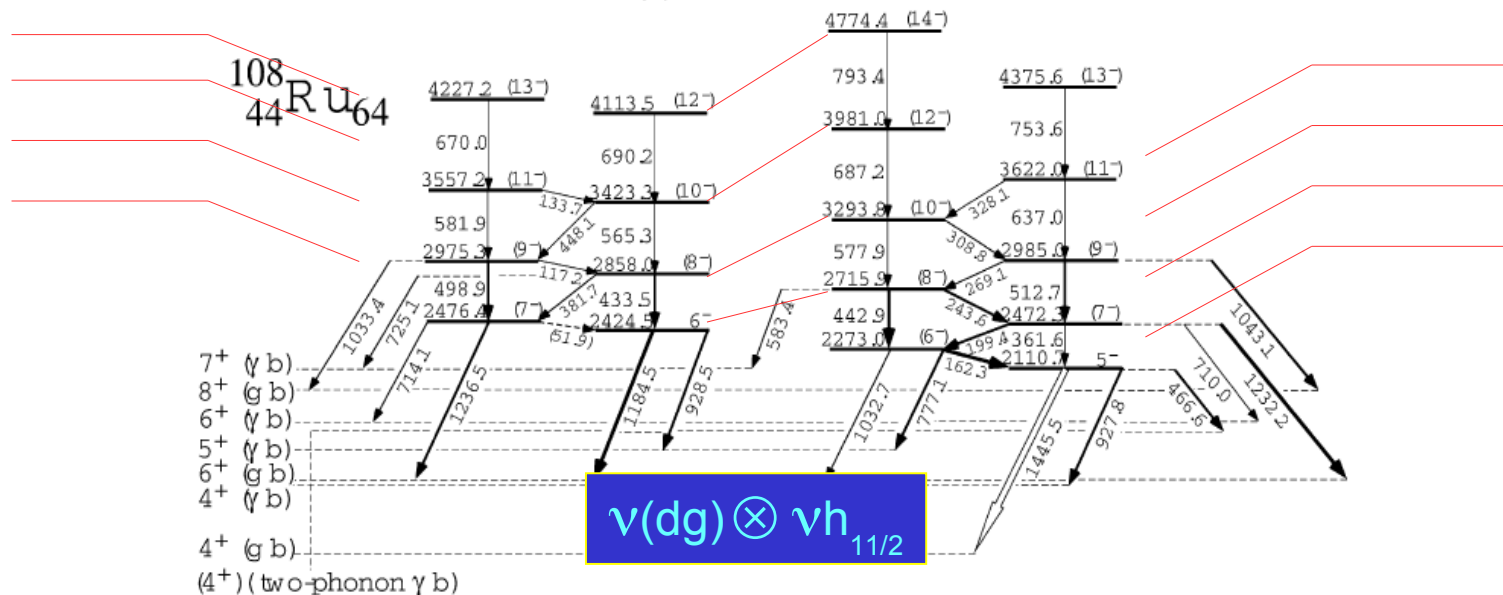
The lowest configuration is obtained by exciting a neutron from the highest  $h_{11/2}$  level to the low-lying mixed  $d_{5/2} - g_{7/2}$  levels.

The tendency to chirality comes about from the interplay of all the neutrons in the open shell, and we could not find a simple partition.

No chiral partner observed!

No interband transitions observed!

No chiral partner observed!





# Five chiral doublets in one nucleus: apotheosis of chirality in $^{136}\text{Nd}$

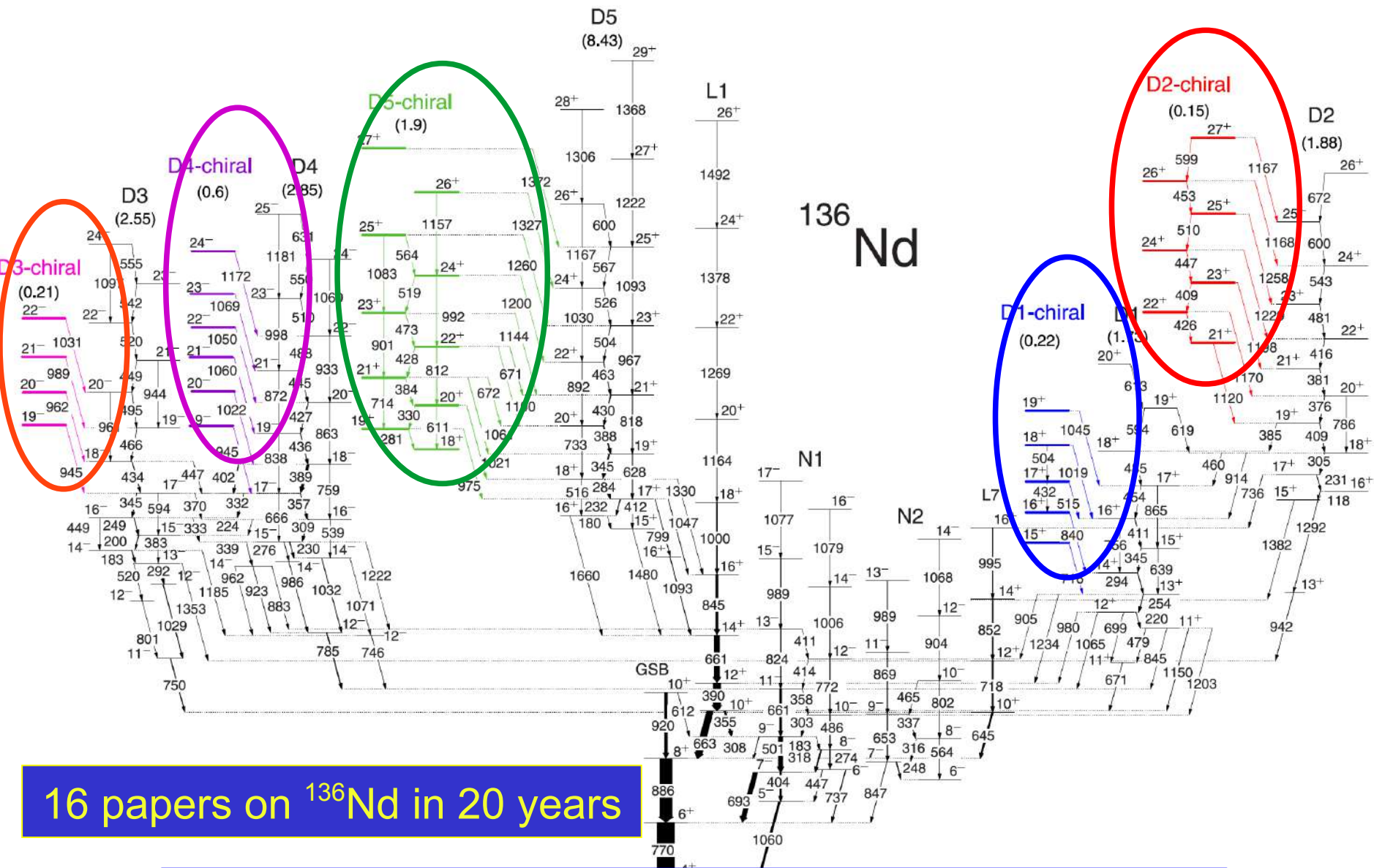
CP, B.F. Lv, et al.

PRC 97 (2018) 041304(R)

Breaking two pairs of nucleons and placing them in orbitals with orthogonal angular momenta lead to much more combinations than in odd-odd nuclei.

The challenge is to identify the very weakly populated 4-qp bands!

# Ultimate chirality: clear evidence in even-even nuclei

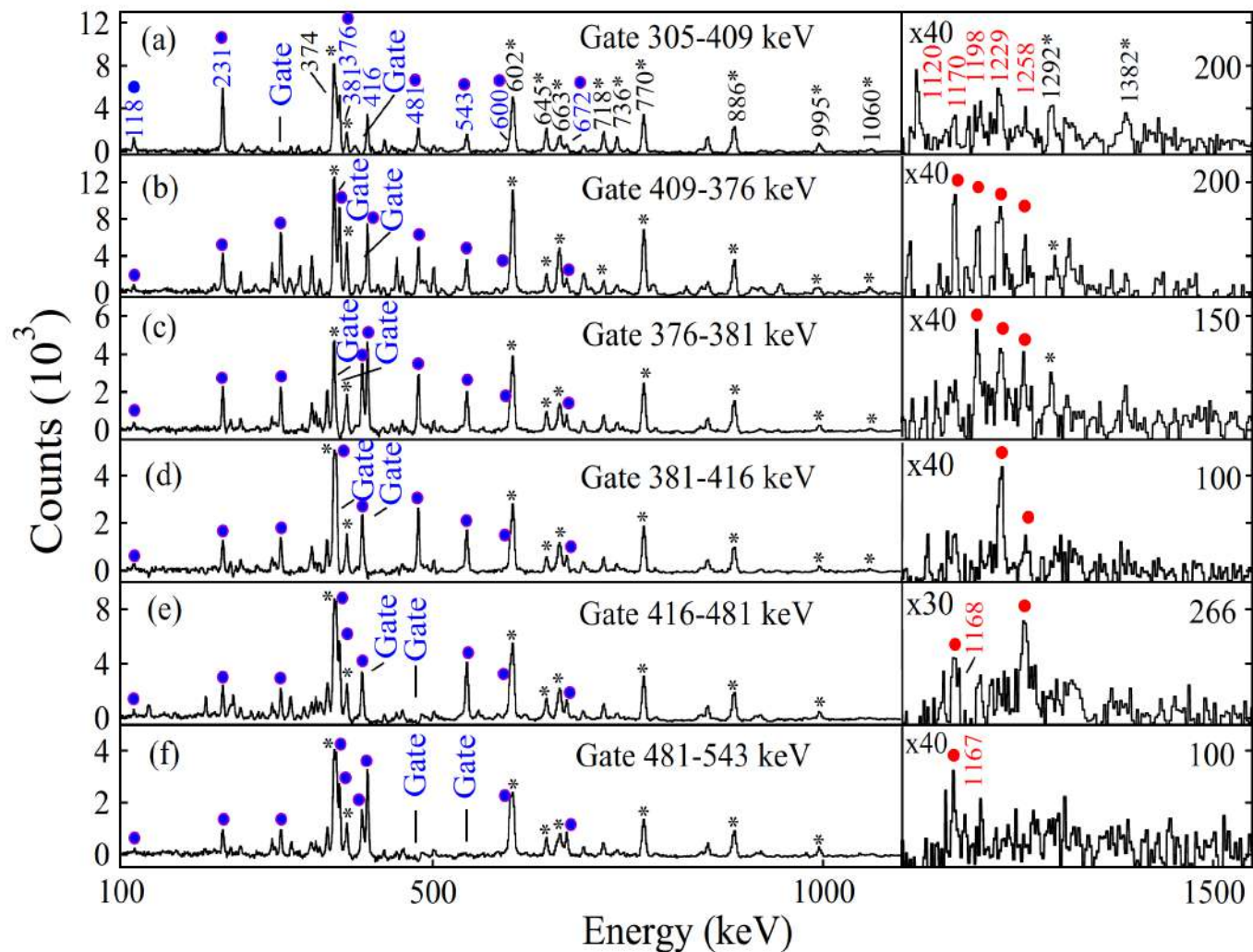
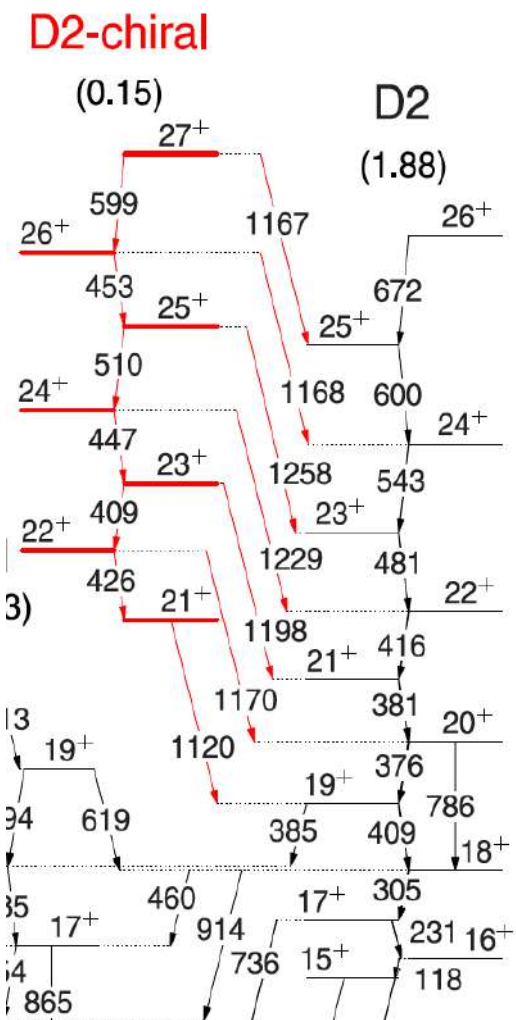


16 papers on  $^{136}\text{Nd}$  in 20 years

CP, B.F. Lv et al, PRC 97 (2018) 041304(R)

# $^{136}\text{Nd}$ – D2 chiral doublet

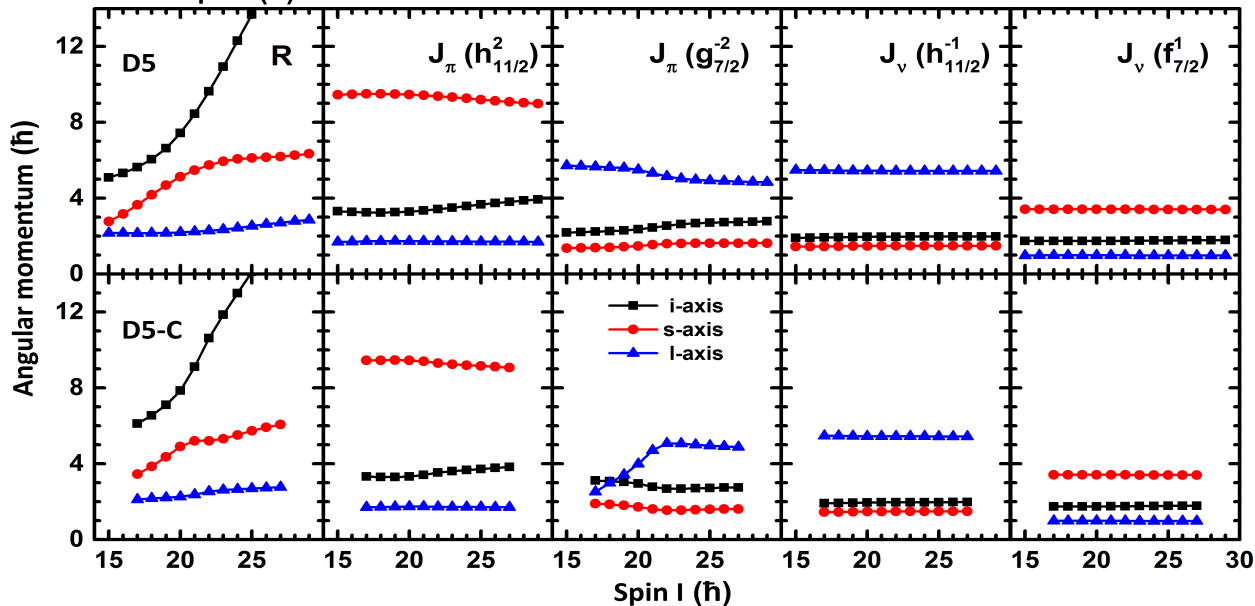
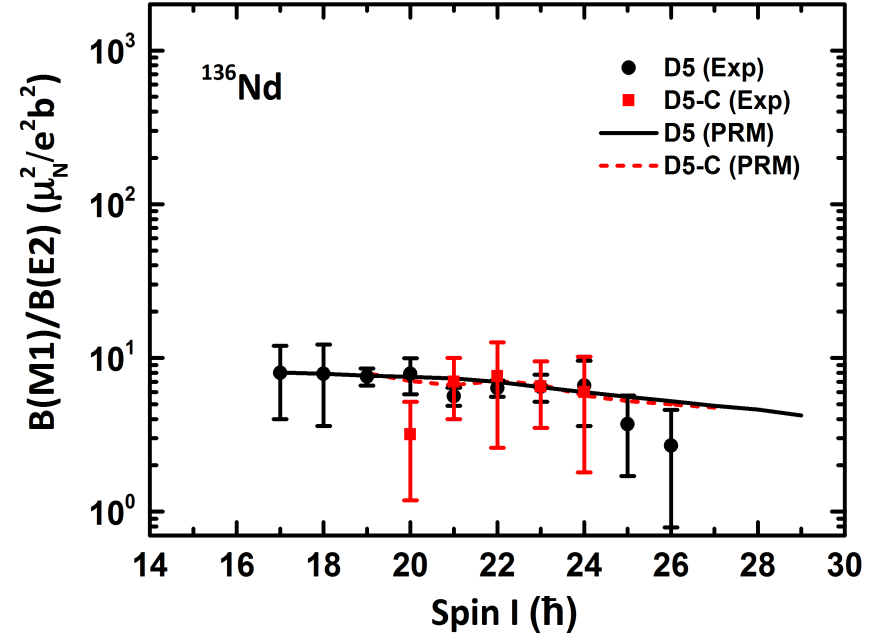
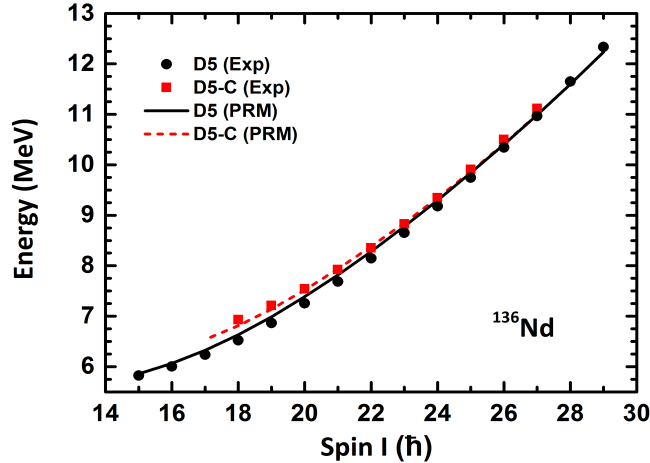
$\pi h^3(dg)^{-1} \otimes \nu h^{-1}(sd)^{-1}$  (3 particles+3 holes)



# $^{136}\text{Nd}$ – chiral doublet D5 (I=2%)

## Numerical details

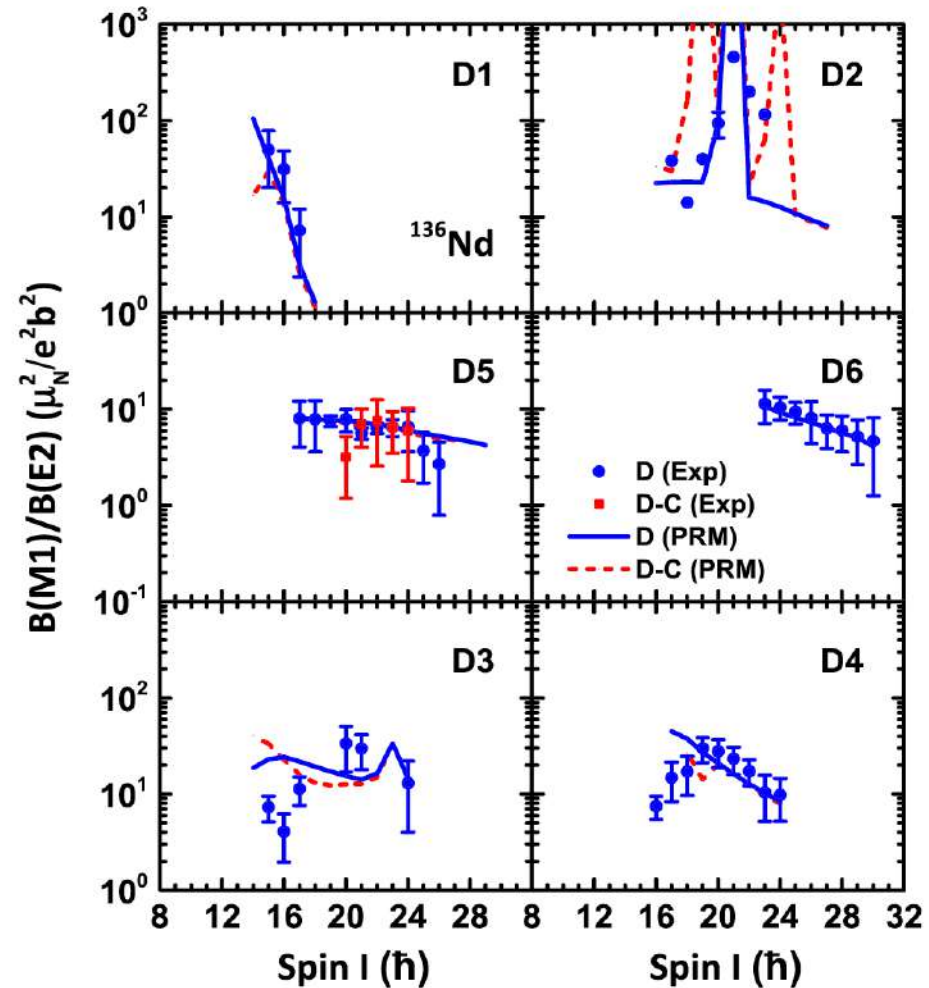
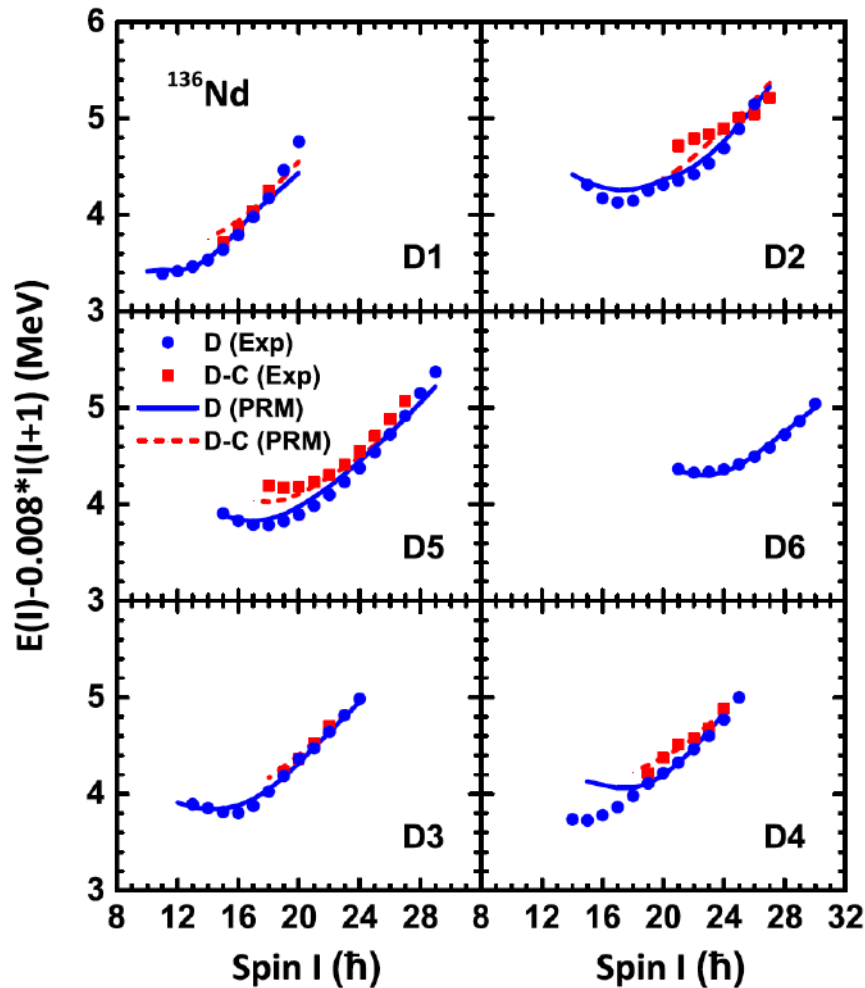
- Configuration:  $\pi (1h_{11/2})^2 (1g_{7/2})^{-2} \nu (1h_{11/2})^{-1} (1f_{7/2})^1$
- Deformation: ( $\beta = 0.26$ ,  $\gamma = 23.0^\circ$ )
- Irr. MOI:  $\mathfrak{S} = 40$  MeV
- Coriolis attenuation factor: 0.93



# Multiple chiral doublets in four- $j$ shells particle rotor model: Five possible chiral doublets in $^{136}_{60}\text{Nd}_{76}$

Q.B. Chen<sup>a</sup>, B.F. Lv<sup>b</sup>, C.M. Petrache<sup>b</sup>, J. Meng<sup>c,d,e,\*</sup>

Physics Letters B 782 (2018) 744–749



# Evidence for pseudospin-chiral quartet bands in the presence of octupole correlations

S. Guo<sup>a,b,\*</sup>, C.M. Petrache<sup>c,\*</sup>, D. Mengoni<sup>d,e</sup>, Y.H. Qiang<sup>a</sup>, Y.P. Wang<sup>f</sup>, Y.Y. Wang<sup>f</sup>, J. Meng<sup>f,g</sup>, Y.K. Wang<sup>f</sup>, S.Q. Zhang<sup>f</sup>, P.W. Zhao<sup>f</sup>, A. Astier<sup>c</sup>, J.G. Wang<sup>a,b</sup>, H.L. Fan<sup>a</sup>, E. Dupont<sup>c</sup>, B.F. Lv<sup>c</sup>, D. Bazzacco<sup>d,e</sup>, A. Boso<sup>d,e</sup>, A. Goasduff<sup>d,e</sup>, F. Recchia<sup>d,e</sup>, D. Testov<sup>d,e</sup>, F. Galtarossa<sup>h,i</sup>, G. Jaworski<sup>h</sup>, D.R. Napoli<sup>h</sup>, S. Riccetto<sup>h</sup>, M. Siciliano<sup>h</sup>, J.J. Valiente-Dobon<sup>h</sup>, M.L. Liu<sup>a,b</sup>, G.S. Li<sup>a,b</sup>, X.H. Zhou<sup>a,b</sup>, Y.H. Zhang<sup>a,b</sup>, C. Andreoiu<sup>j</sup>, F.H. Garcia<sup>j</sup>, K. Ortner<sup>j</sup>, K. Whitmore<sup>j</sup>, A. Ataç-Nyberg<sup>k</sup>, T. Bäck<sup>k</sup>, B. Cederwall<sup>k</sup>, E.A. Lawrie<sup>l,m</sup>, I. Kuti<sup>n</sup>, D. Sohler<sup>n</sup>, T. Marchlewski<sup>o</sup>, J. Srebrny<sup>o</sup>, A. Tucholski<sup>o</sup>



Physics Letters B 807 (2020) 135572

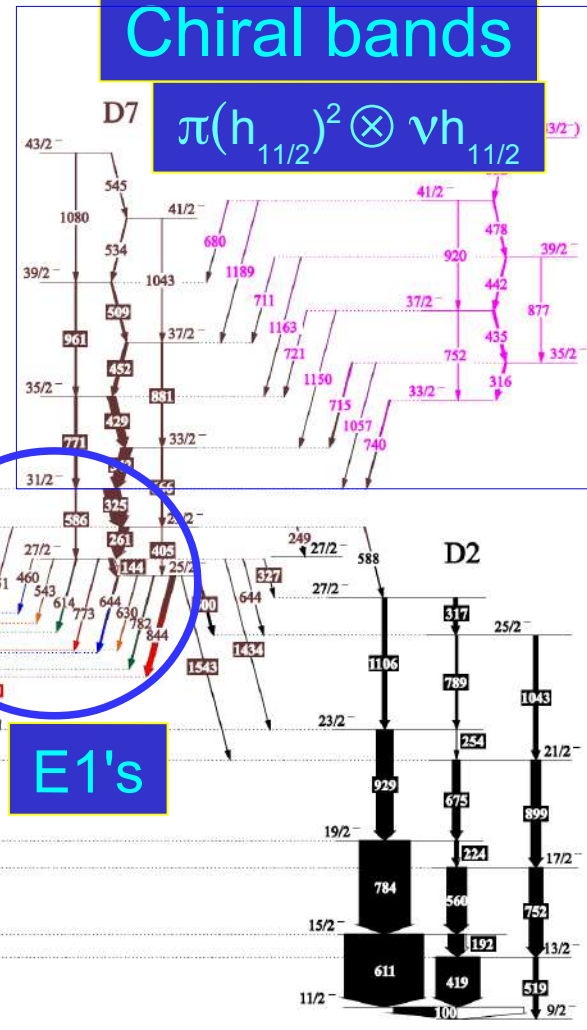
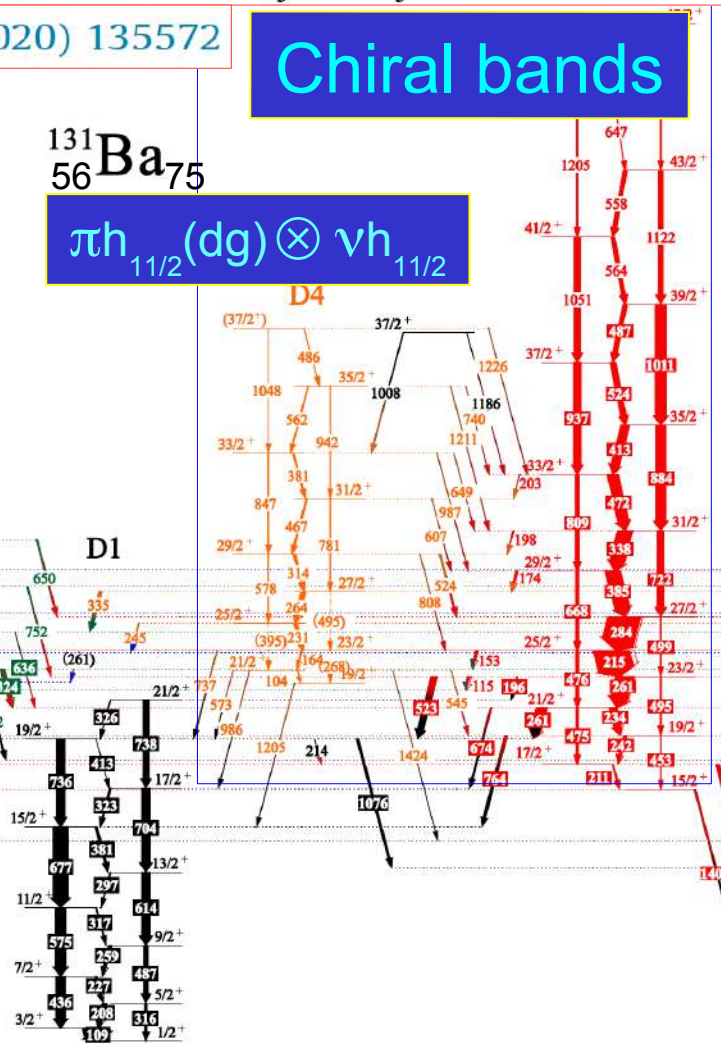
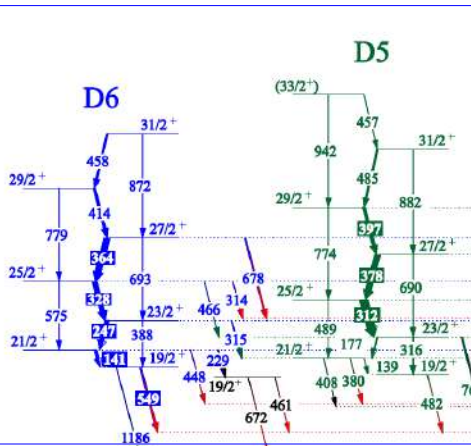
## Chiral bands

## Chiral bands

$$^{131}_{56}\text{Ba}_{75} \quad \pi h_{11/2}(dg) \otimes \nu h_{11/2}$$

## Chiral bands

$$D7 \quad \pi(h_{11/2})^2 \otimes \nu h_{11/2}$$



## E1's

# Selection rules of electromagnetic transitions for chirality-parity violation in atomic nuclei

Yuanyuan Wang<sup>a</sup>, Xinhui Wu<sup>a</sup>, Shuangquan Zhang<sup>a</sup> ✉, Pengwei Zhao<sup>a</sup>, Jie Meng<sup>a, b, c</sup> ✉



Science Bulletin

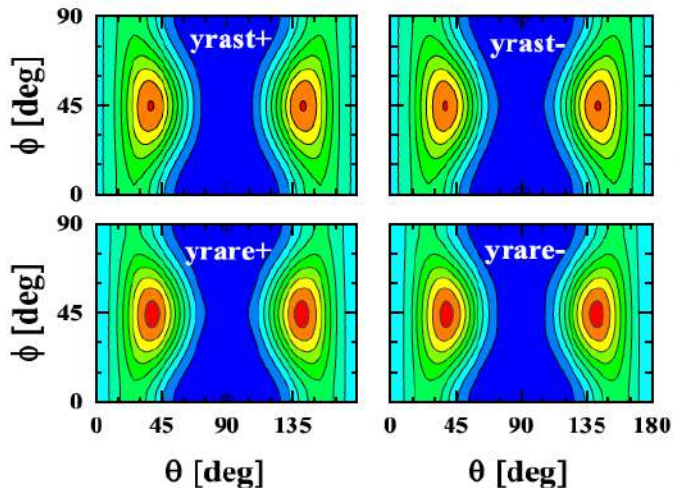
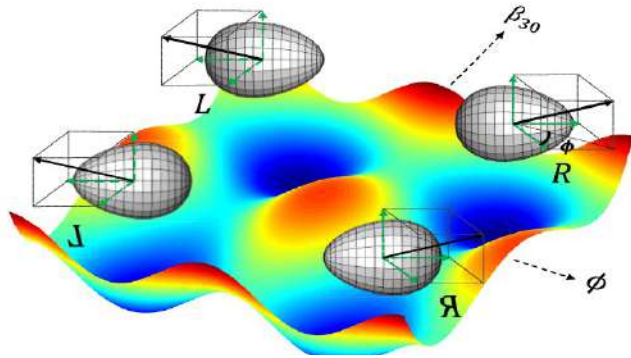
Volume 65, Issue 23, 15 December 2020, Pages 2001-2006



## Multiple chiral doublet bands with octupole correlations in reflection-asymmetric triaxial particle rotor model

Y.Y. Wang (王媛媛)<sup>a</sup>, S.Q. Zhang (张双全)<sup>b</sup>, P.W. Zhao (赵鹏巍)<sup>b</sup>, J. Meng (孟杰)<sup>b, a, c, \*</sup>

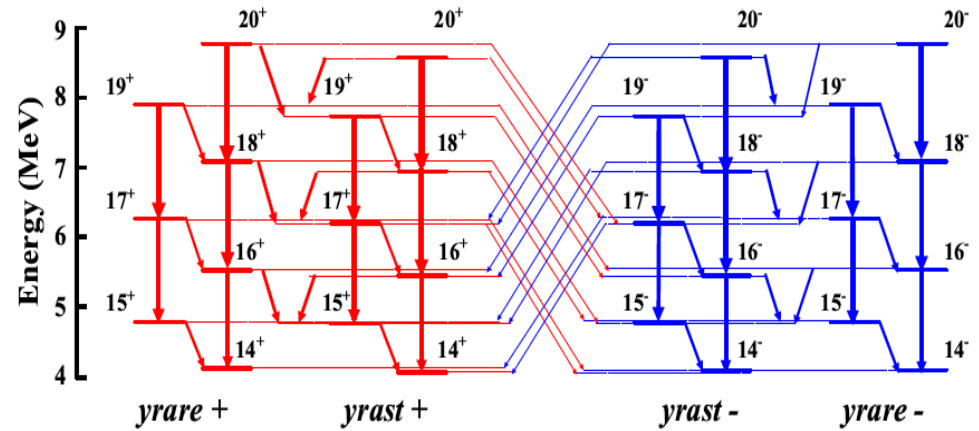
Physics Letters B 792 (2019) 454–460



New quantum numbers

Chiture  $\mathcal{A}$ , similar to signature  $\mathcal{R}$

Chiplex  $\mathcal{B}=\mathcal{A}\mathcal{P}$ , similar to simplex  $\mathcal{S}=\mathcal{R}(\pi)\mathcal{P}$



Robustness of chiral symmetry in atomic nuclei with reflection-asymmetric shapes

Costel Marian Petrace ✉



Science Bulletin

Volume 65, Issue 23, 15 December 2020, Pages 1956-1957



# Electric revolving chirality at the limits

3D rotation (bottom) → 3D rotation (revolving) → 2D rotation (top)

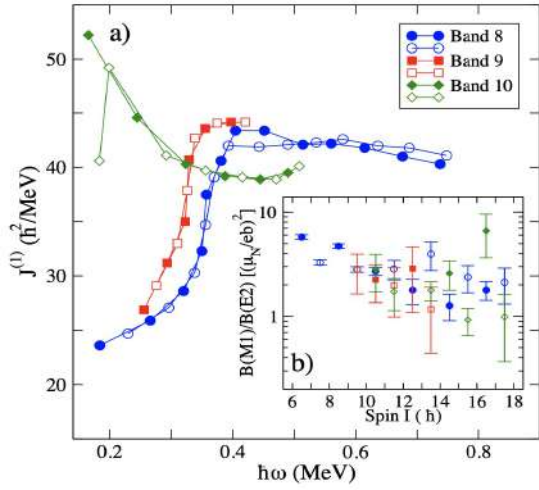
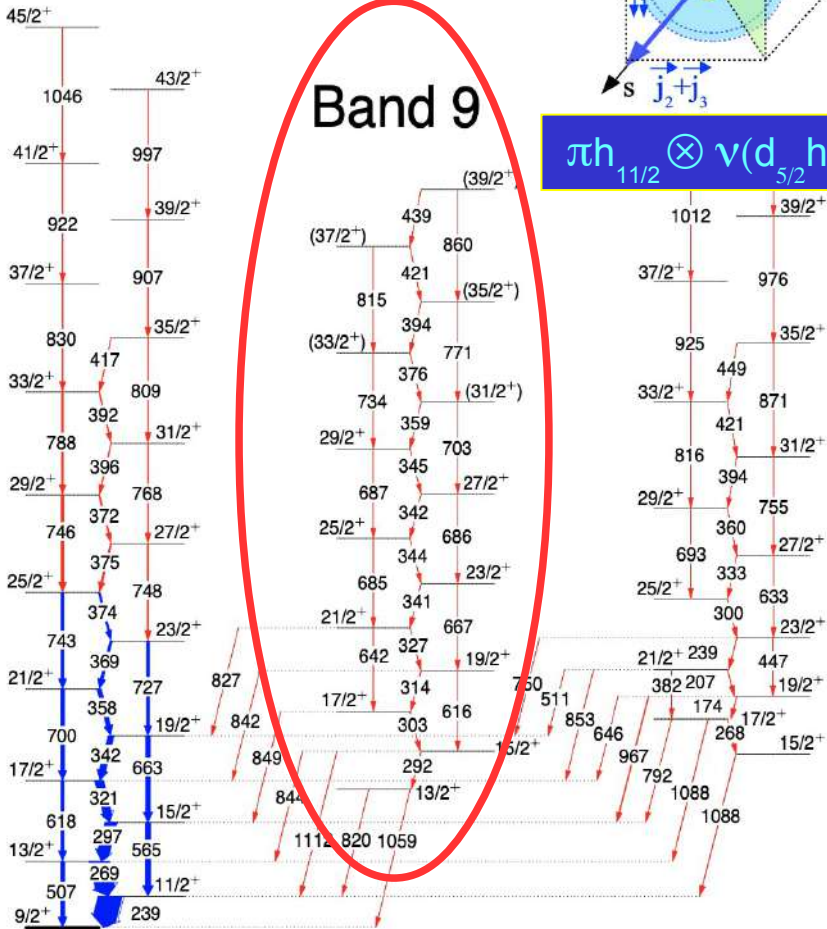
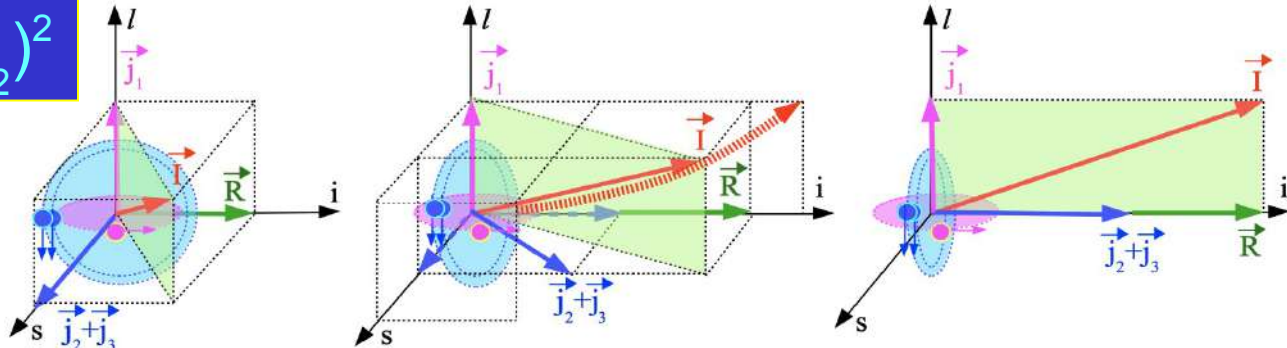
$$\pi[404]9/2^+ \otimes \pi(h_{11/2})^2$$

Band 8

<sup>119</sup>Cs

Band 9

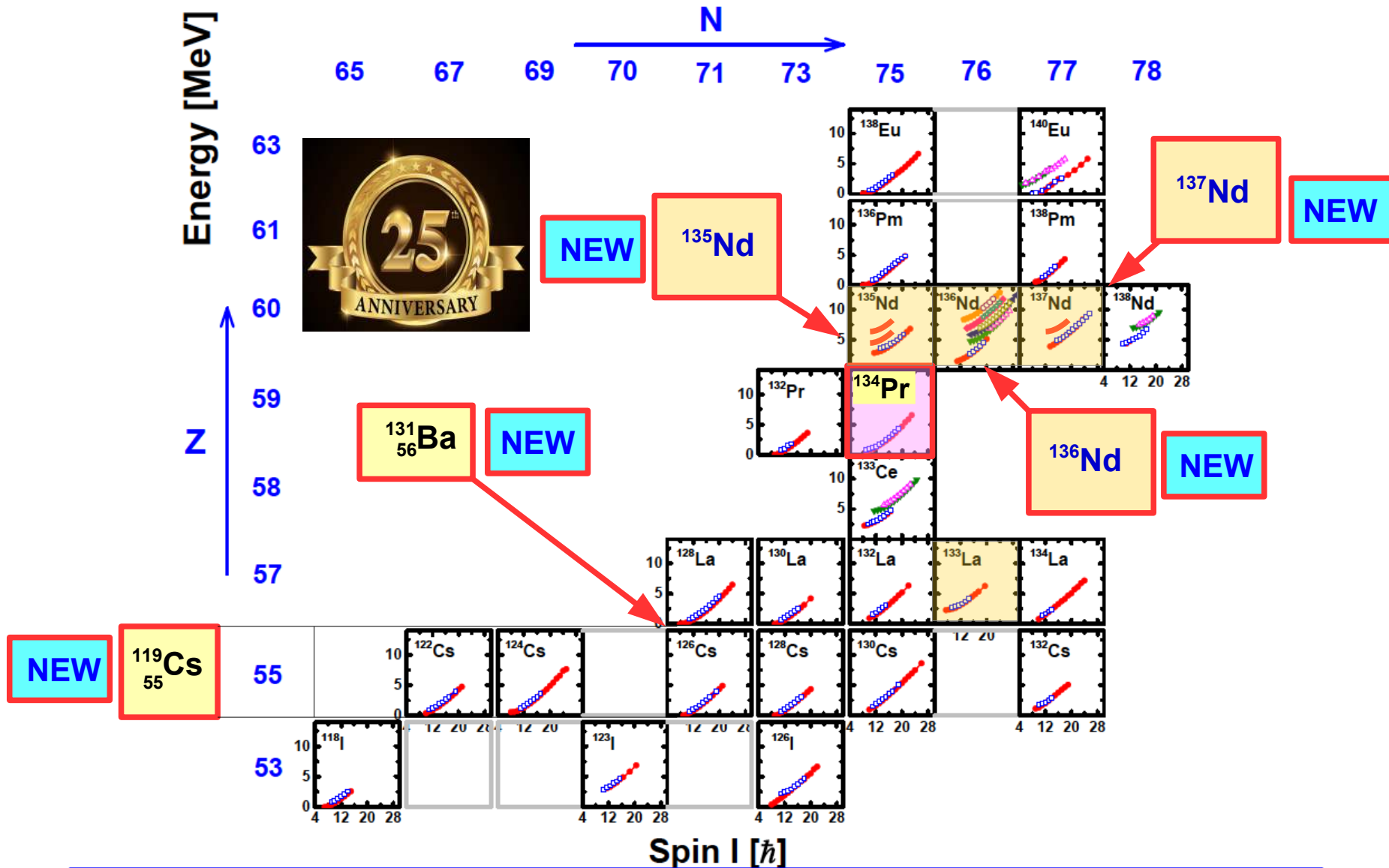
$$\pi h_{11/2} \otimes \nu(d_{5/2} h_{11/2})$$



Submitted to PRL



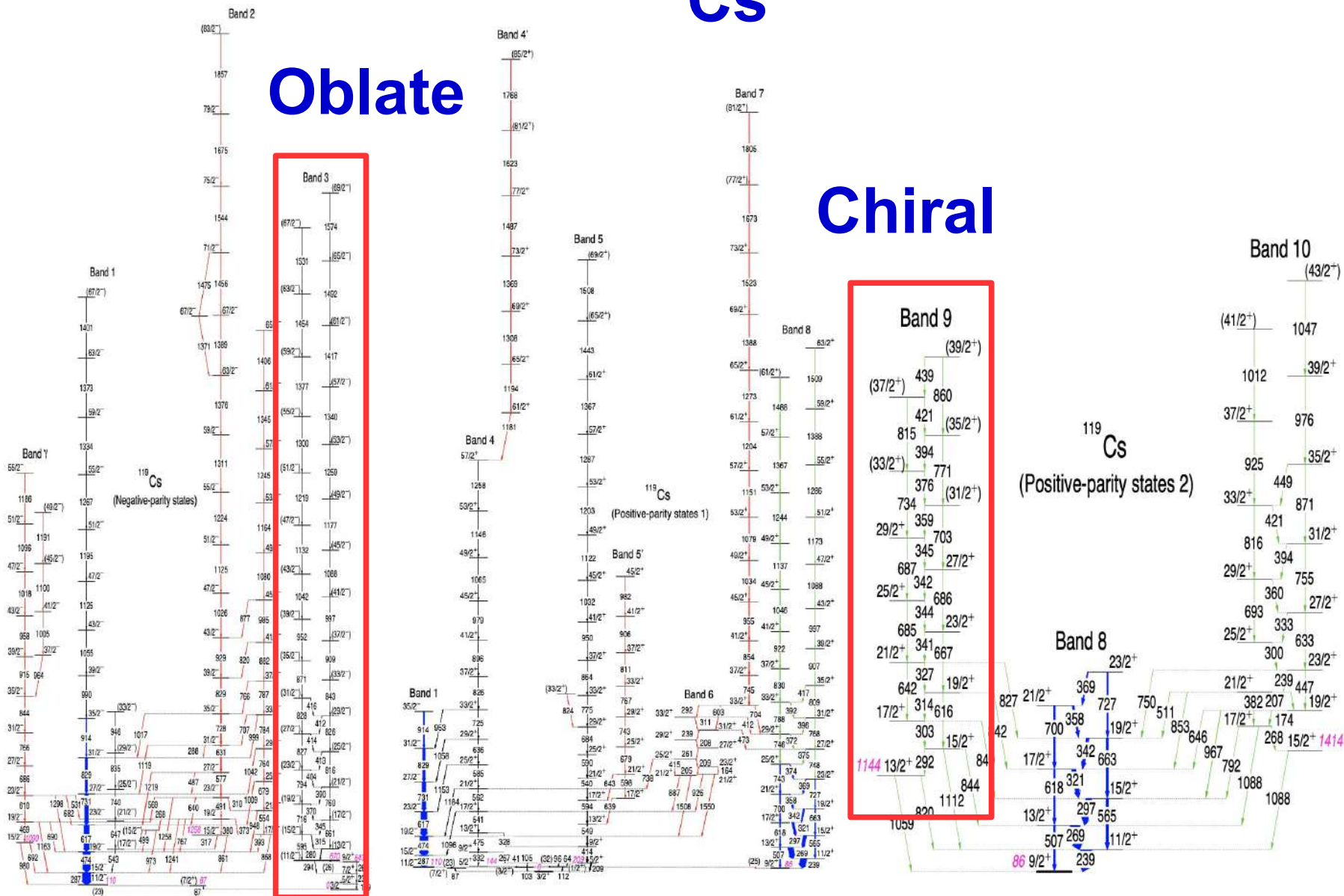
# New chiral bands in A=130 region



# $^{119}\text{Cs}$

## Oblate

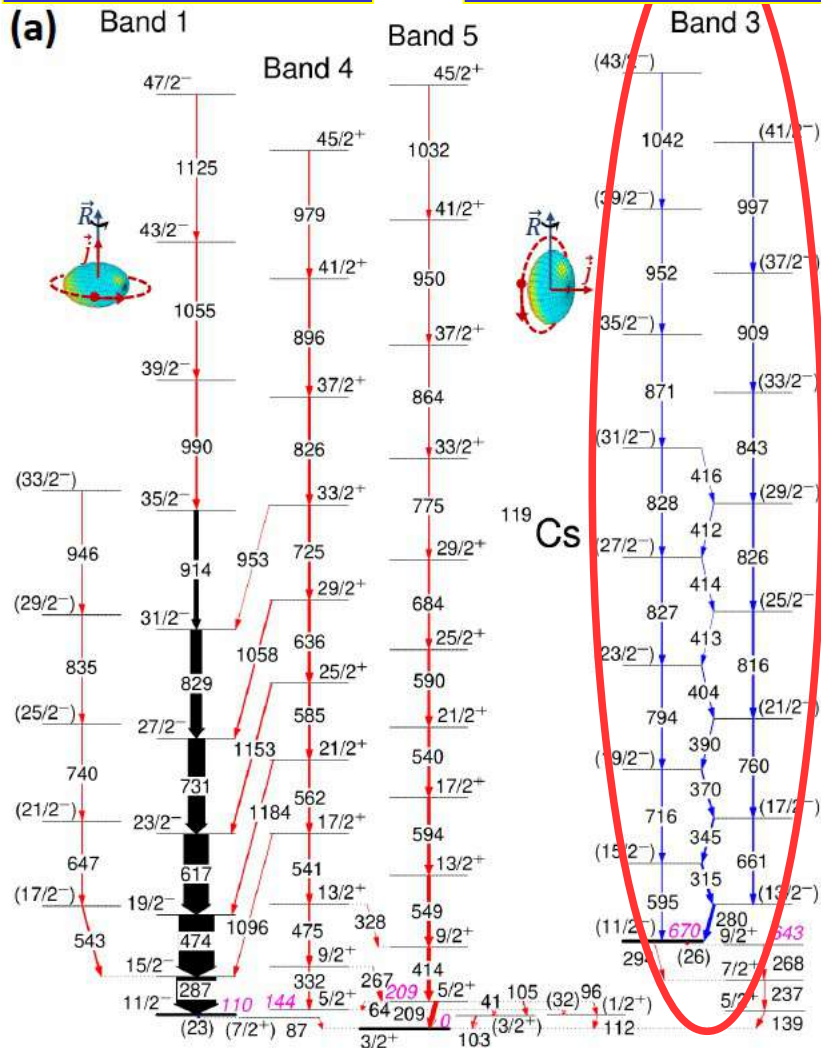
## Chiral



# Oblate-prolate coexistence at the limits

$\pi[541]3/2^-$

$\pi[505]11/2^-$



submitted to PLB

TAC-CDFT

PNC-CSM

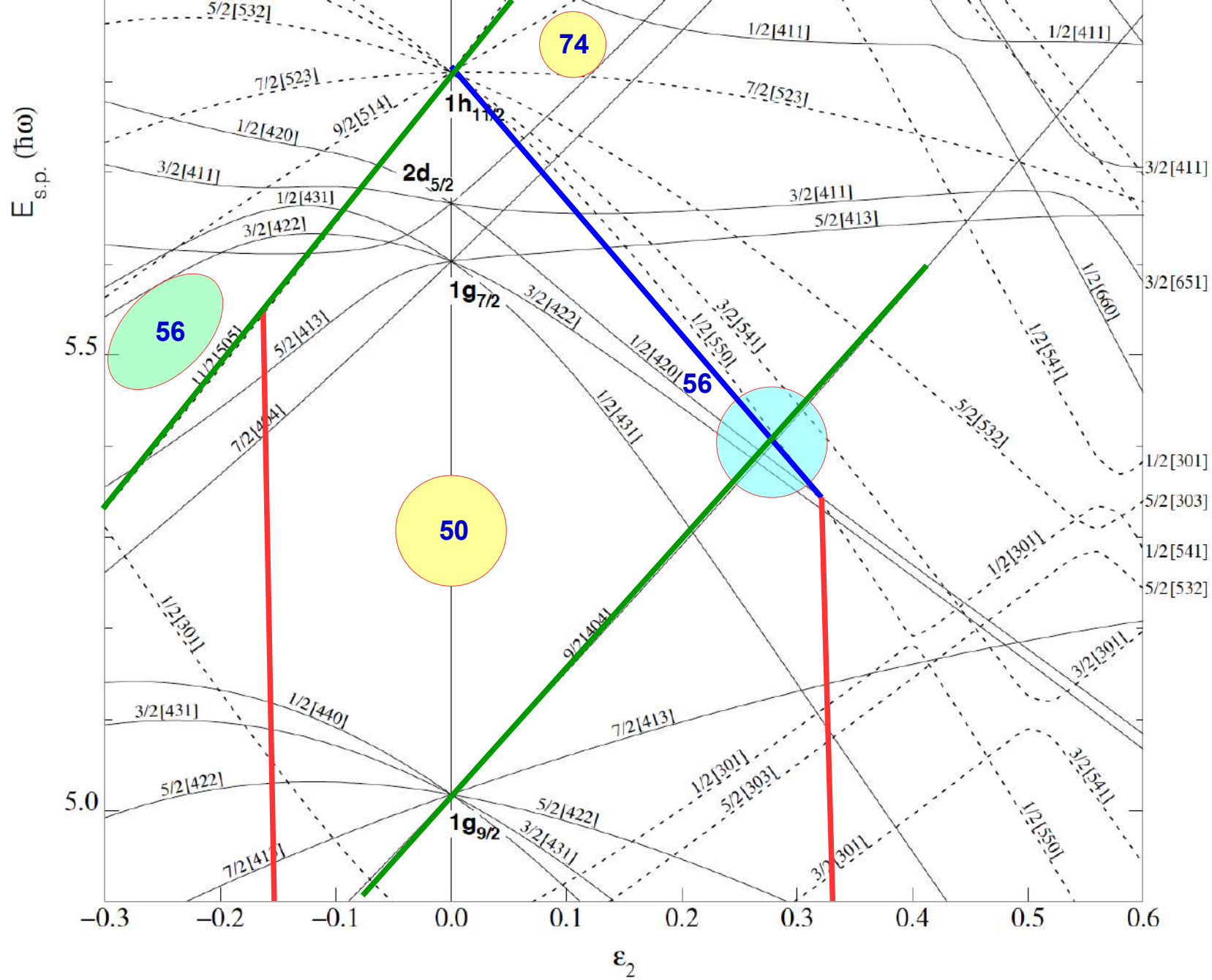


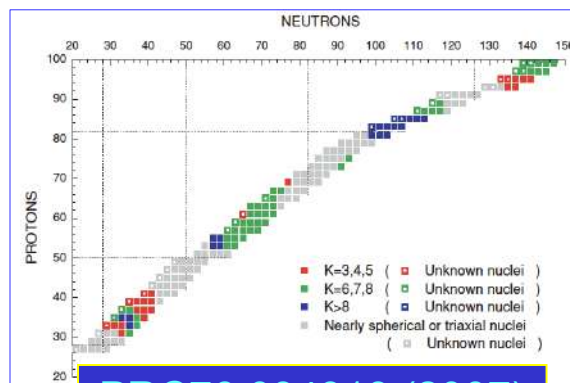
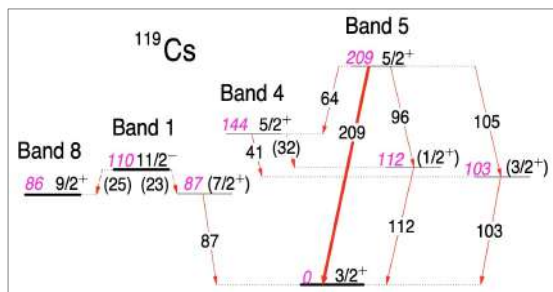
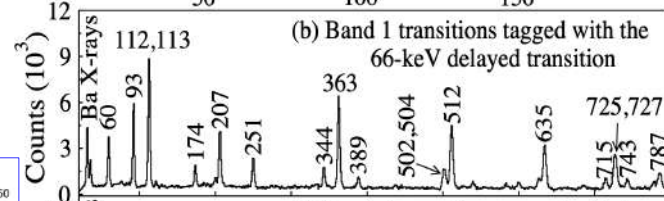
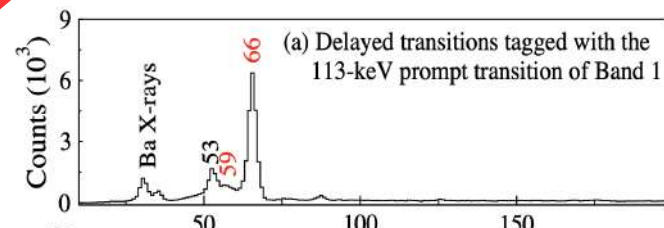
Figure 11. Nilsson diagram for protons,  $50 \leq Z \leq 82$  ( $\epsilon_4 = \epsilon_2^2/6$ ).

$^{119}\text{Cs } \pi[541]3/2^-$

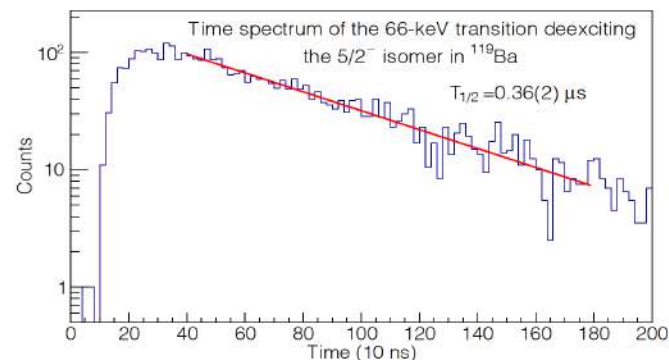
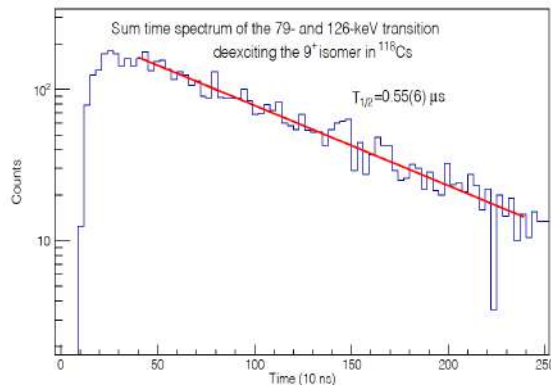
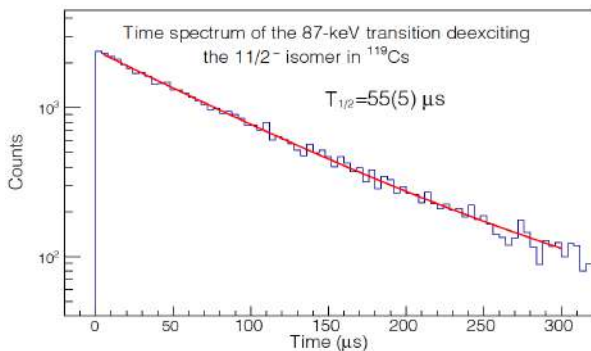
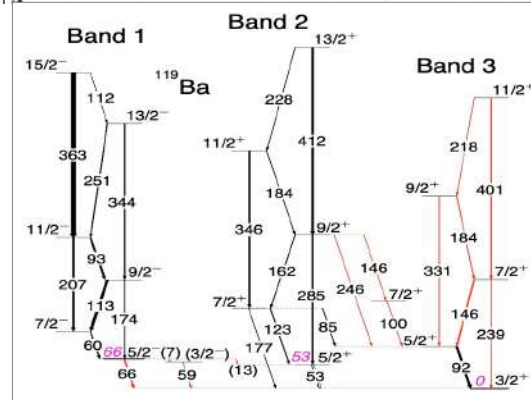
**Isomerism**  
at the proton drip line

$^{119}\text{Ba } \nu[532]5/2^-$

$^{118}\text{Cs}$   
 $\pi[541]3/2^-$   
 $\nu[532]5/2^-$



PRC76,034313 (2007)



# Wobbling outside of the A=160 mass region

- low-spin 1-qp bands: NO
- high-spin 1,2-qp bands: YES

# Wobbling bands ■ theoretical predictions and calculations

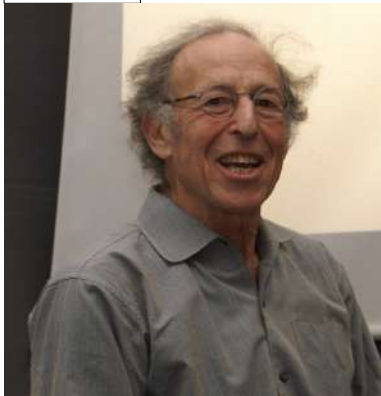
1975, Bohr-Mottelson, Chapter 4,  
States with large  $I$  ( $I^2 \gg I_2^2 + I_3^2$ )

$$E(I, n_{\text{wobb}}) = \frac{I(I+1)}{2\mathcal{J}_x} + \hbar\omega_{\text{wobb}} \left( n_{\text{wobb}} + \frac{1}{2} \right)$$

1975

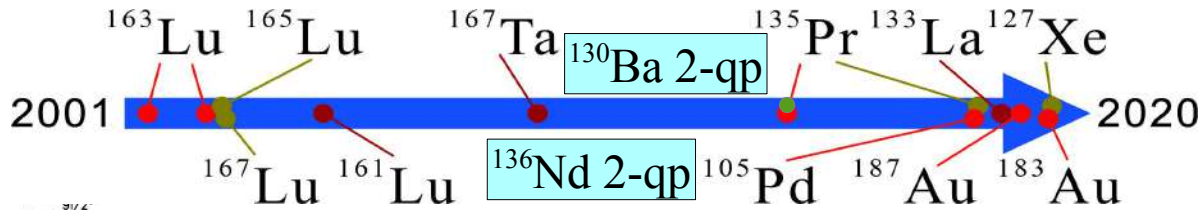
2001

2020

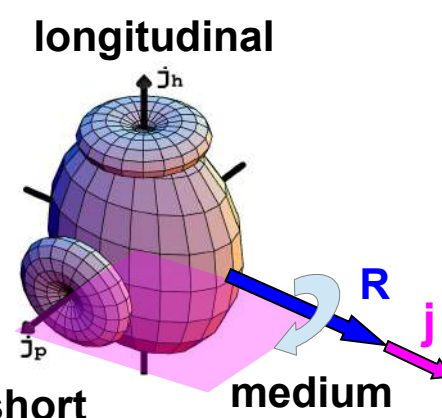
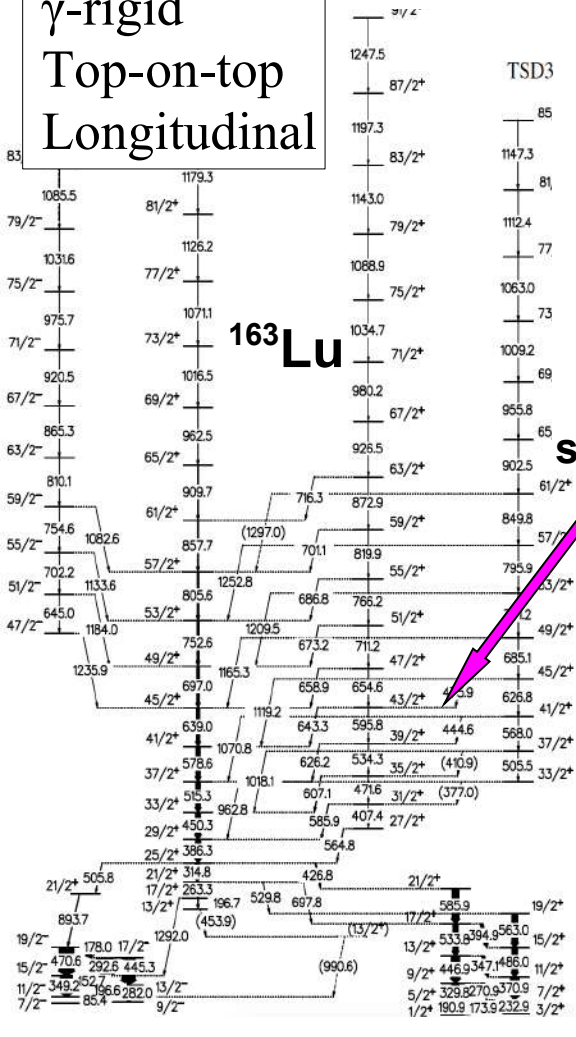


# Reported wobbling bands

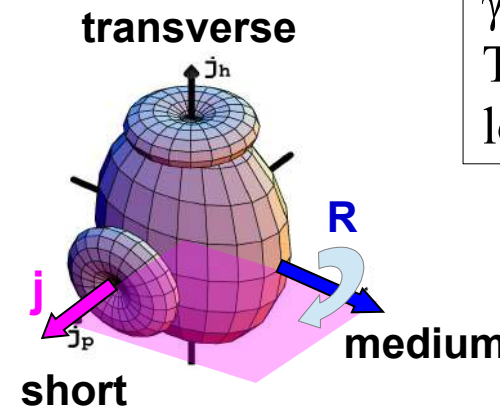
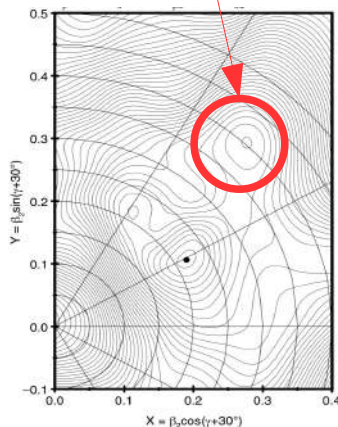
High spins  
Large  $\beta_2$   
 $\gamma$ -rigid  
Top-on-top  
Longitudinal



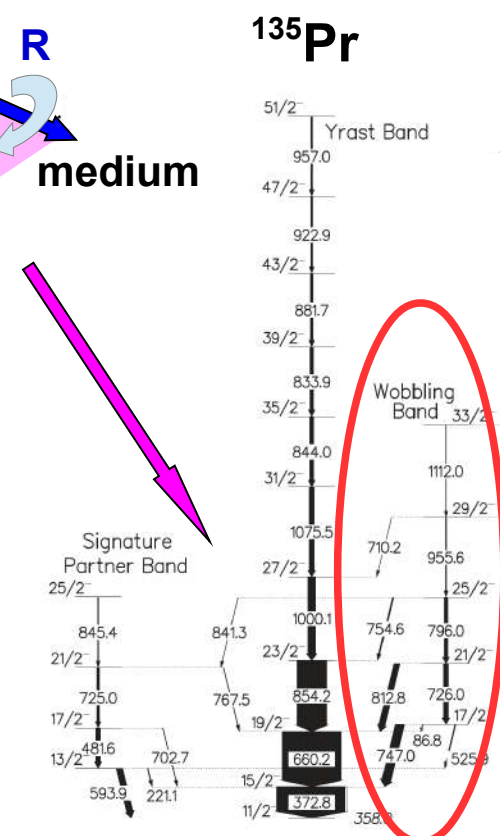
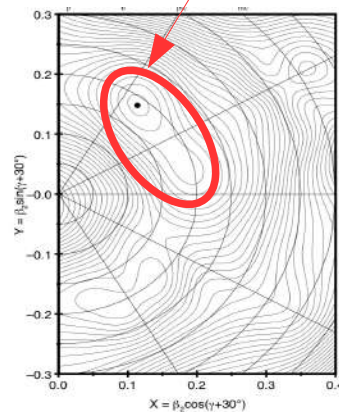
Low spins  
Moderate  $\beta_2$   
 $\gamma$ -soft  
Transverse or longitudinal



$$\beta_2 \sim 0.4$$



$$\beta_2 \sim 0.2$$

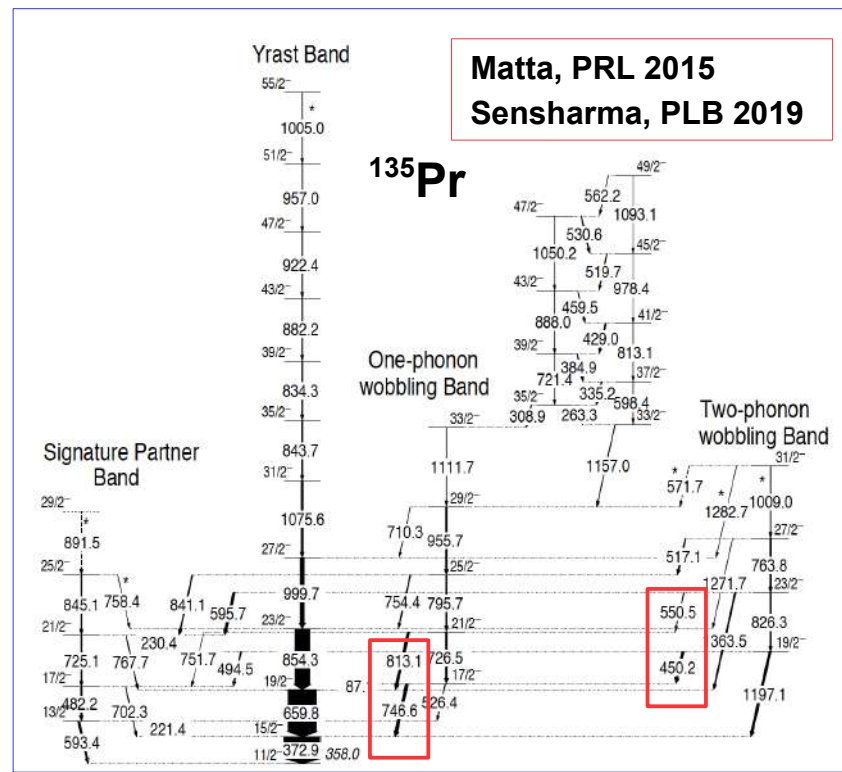
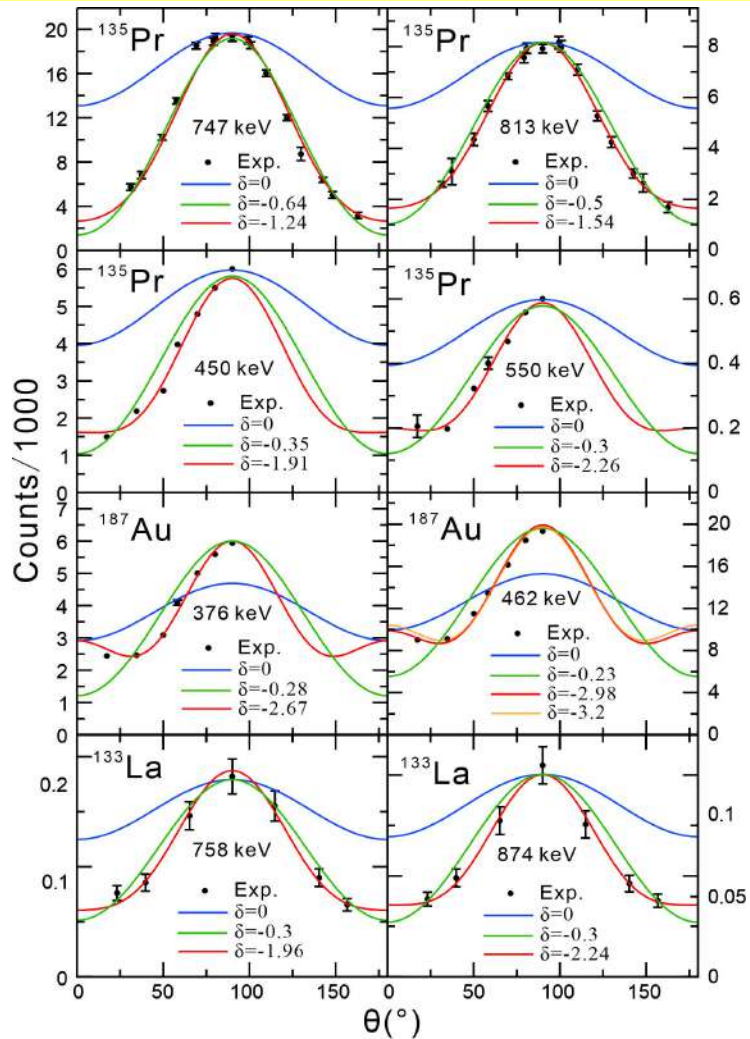




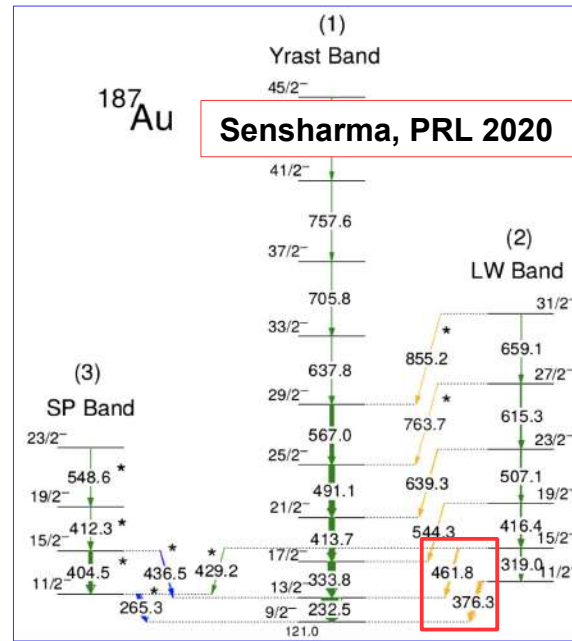
# No wobbling at low spin !

Not easy to extract convincing mixing ratios from angular distributions of transitions with 10% relative intensities!

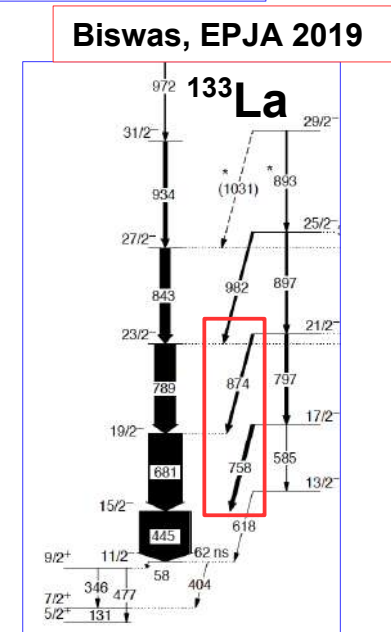
Polarization asymmetry has very large errors for weak transitions!



Matta, PRL 2015  
Sensharma, PLB 2019



Sensharma, PRL 2020



Biswas, EPJA 2019



No wobbling at low spins,  
high risk of misinterpretation

PHYSICAL REVIEW C **101**, 034306 (2020)

**Tilted precession and wobbling in triaxial nuclei**

E. A. Lawrie<sup>1,2,\*</sup>, O. Shirinda<sup>1,†</sup> and C. M. Petrache<sup>3,‡</sup>

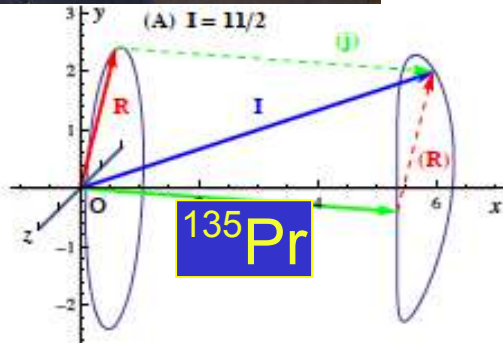
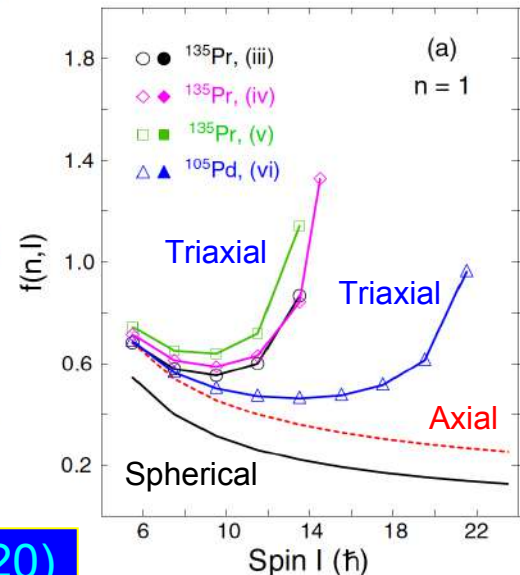
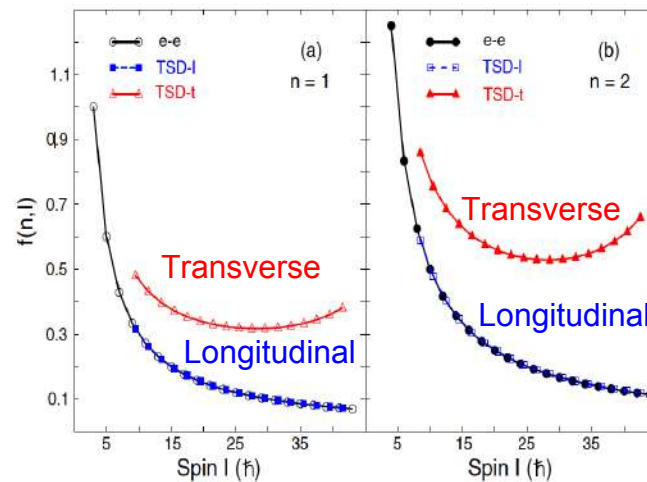
The wobbling approximation is valid if the rotational angular momenta around the two axes with lower MoI is small [16]:

$$I_2^2 + I_3^2 \ll I^2, \tag{15}$$

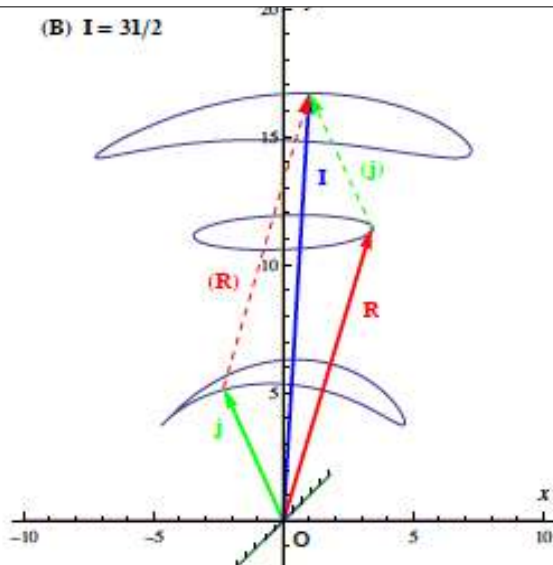
a condition that can be rewritten as

$$f(n, I) = (2n + 1) \frac{(A_2 + A_3 - 2A_1)}{2I\sqrt{(A_2 - A_1)(A_3 - A_1)}} \ll 1. \tag{16}$$

$A_1 = 1, A_2 = 4,$  and  $A_3 = 4$  are used



Revolving towards the medium axis  
No stable transverse geometry !!!



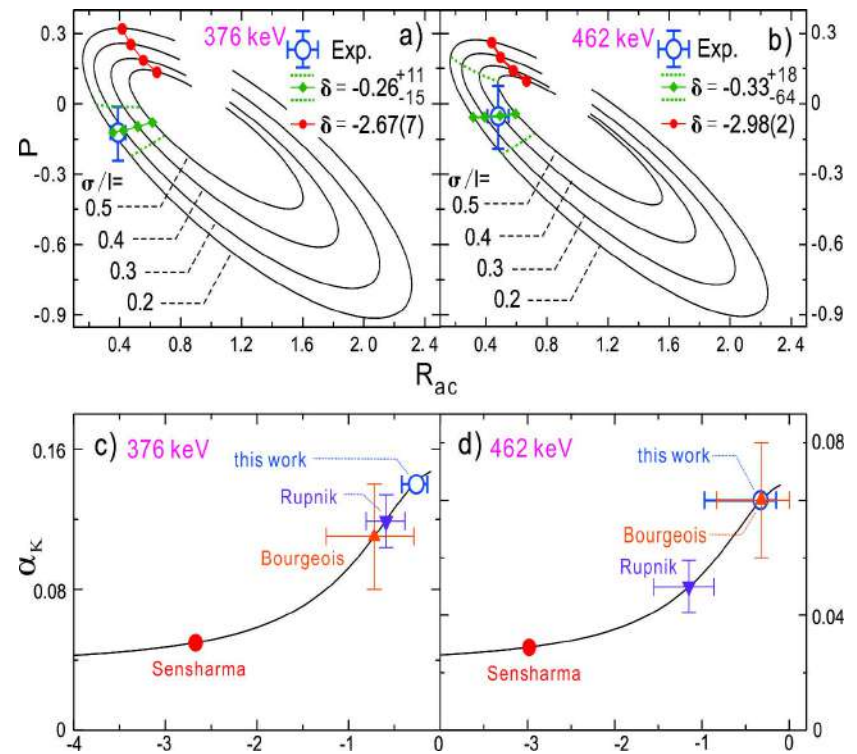
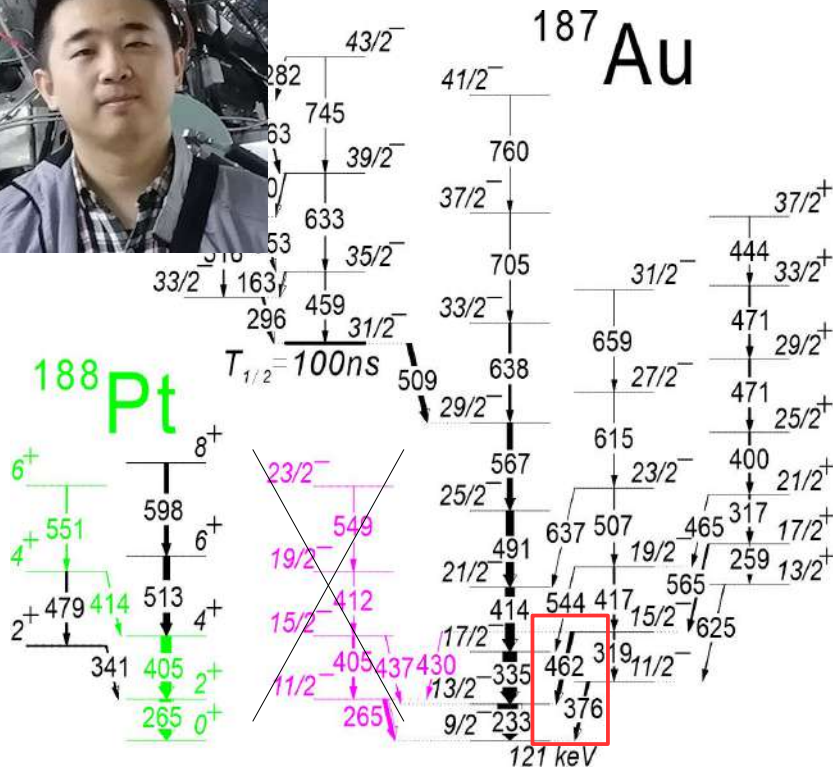
Tanabe, PRC 95 (2017)

Lawrie, PRC 101 (2020)

# No wobbling in $^{187}\text{Au}$ !

## Longitudinal Wobbling Motion in $^{187}\text{Au}$

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 M. P. Carpenter,<sup>3</sup> P. Copp,<sup>3</sup> F. G. Kondev,<sup>3</sup> T. Lauritsen,<sup>3</sup> J. Li,<sup>3</sup> D. Seweryniak,<sup>3</sup> J. Wu,<sup>3</sup> A. D. Ayangeakaa,<sup>4</sup>  
 D. J. Hartley,<sup>4</sup> R. V. F. Janssens,<sup>5,6</sup> A. M. Forney,<sup>7</sup> W. B. Walters,<sup>7</sup> S. S. Ghugre,<sup>8</sup> and R. Palit<sup>9</sup>



# Transverse wobbling in an even-even nucleus $^{130}\text{Ba}$

Q. B. Chen<sup>a,1,\*</sup>, S. Frauendorf<sup>2,†</sup> and C. M. Petrache<sup>3,‡</sup>

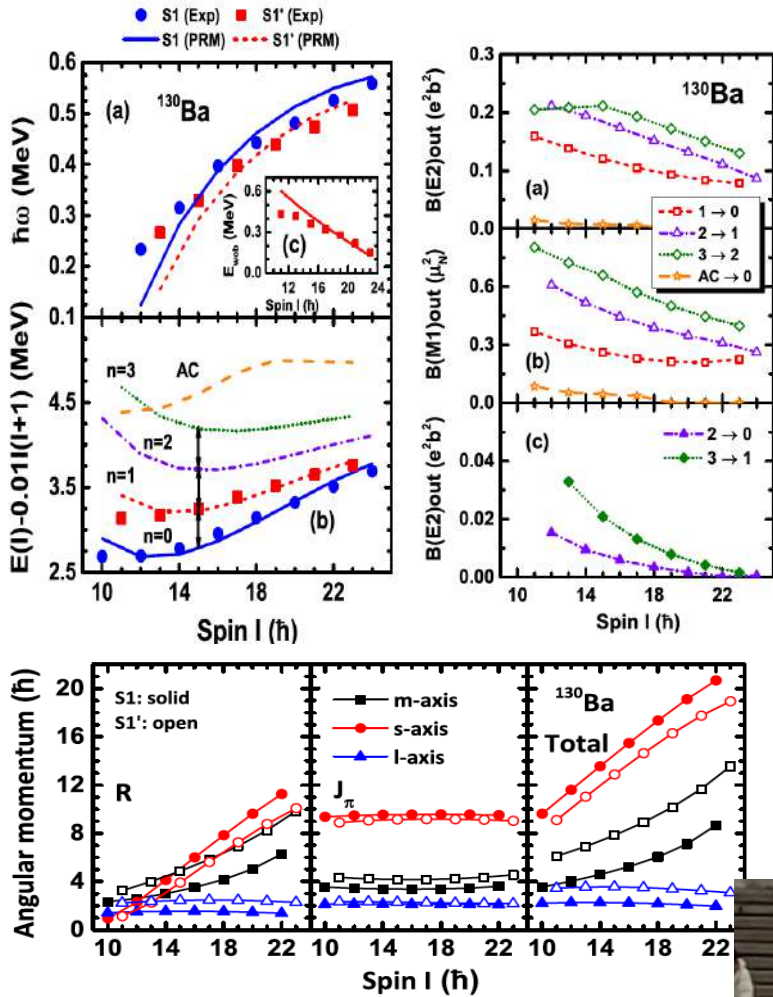
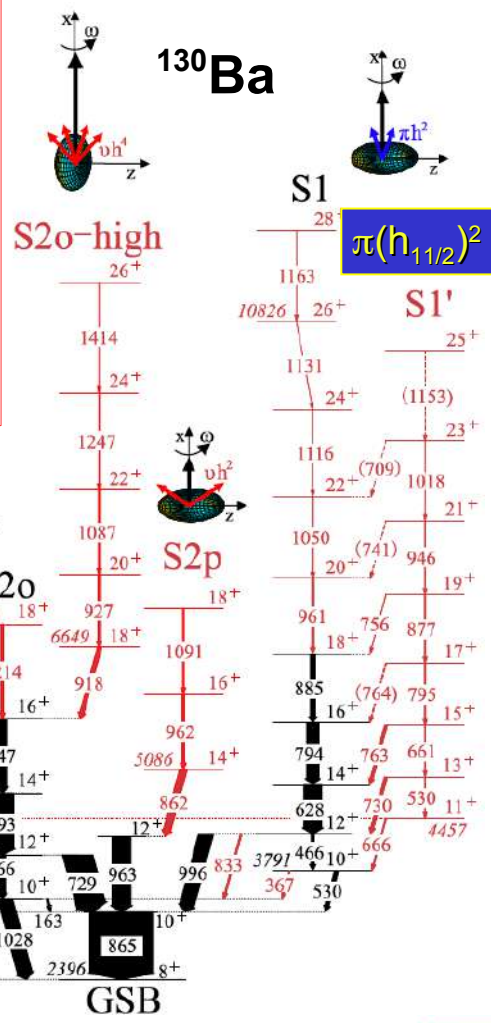
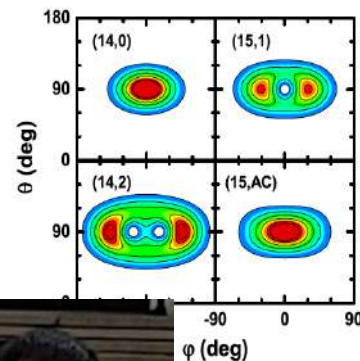
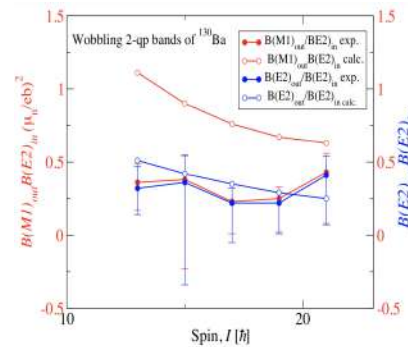


TABLE I. Experimental and theoretical mixing ratios  $\delta$  as well as the transition probability ratios  $B(M1)_{out}/B(E2)_{in}$  and  $B(E2)_{out}/B(E2)_{in}$  for the transitions from band S1' to band S1 of  $^{130}\text{Ba}$ .

$I(\hbar)$	$\delta$		$B(M1)_{out}/B(E2)_{in}$ ( $\mu_N^2/e^2b^2$ )		$B(E2)_{out}/B(E2)_{in}$	
	Expt	PRM	Expt	PRM	Expt	PRM
13	$-0.58^{+13}_{-13}$	-0.67	$0.36^{+19}_{-15}$	1.11	$0.32^{+18}_{-15}$	0.51
15	$-0.62^{+10}_{-10}$	-0.68	$0.38^{+61}_{-16}$	0.90	$0.36^{+70}_{-19}$	0.42
17	$-0.62^{+10}_{-10}$	-0.68	$0.23^{+22}_{-09}$	0.76	$0.22^{+27}_{-10}$	0.35
19	-0.60	-0.66	$0.25^{+23}_{-13}$	0.67	$0.22^{+21}_{-07}$	0.29
21	-0.60	-0.63	$0.43^{+35}_{-13}$	0.63	$0.41^{+34}_{-13}$	0.25



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Two quasiparticle wobbling in the even-even nucleus  $^{130}\text{Ba}$   
 Y.K. Wang<sup>a</sup>, F.Q. Chen<sup>b</sup>, P.W. Zhao<sup>a,\*</sup>



Diversity of shapes and rotations in the  $\gamma$ -soft  $^{130}\text{Ba}$  nucleus: First observation of a  $t$ -band in the  $A = 130$  mass region

C.M. Petrache<sup>a,\*</sup>, P.M. Walker<sup>b</sup>, S. Guo<sup>c,d,\*</sup>, Q.B. Chen<sup>e</sup>, S. Frauendorf<sup>f</sup>, Y.X. Liu<sup>g</sup>, R.A. Wyss<sup>h</sup>, D. Mengoni<sup>i</sup>, Y.H. Qiang<sup>c</sup>, A. Astier<sup>3</sup>, E. Dupont<sup>3</sup>, R. Li<sup>2</sup>, B.F. Lv<sup>2</sup>, K.K. Zheng<sup>a</sup>, D. Bazzacco<sup>1</sup>, A. Boso<sup>1</sup>, A. Goasduff<sup>1</sup>, F. Recchia<sup>1</sup>, D. Testov<sup>1</sup>, F. Gallarossa<sup>1</sup>, G. Jaworski<sup>1</sup>, D.R. Napoli<sup>1</sup>, S. Riccetto<sup>1</sup>, M. Siciliano<sup>j,k</sup>, J.J. Valiente-Dobon<sup>l</sup>, M.L. Liu<sup>c,d</sup>, X.H. Zhou<sup>c,d</sup>, J.G. Wang<sup>c</sup>, C. Andreoiu<sup>1</sup>, F.H. Garcia<sup>1</sup>, K. Ortner<sup>1</sup>, K. Whitmore<sup>1</sup>, T. Bäck<sup>h</sup>, B. Cederwall<sup>h</sup>, E.A. Lawrie<sup>m</sup>, I. Kuti<sup>n</sup>, D. Sohler<sup>n</sup>, J. Timár<sup>n</sup>, T. Marchlewski<sup>o</sup>, J. Srebrny<sup>o</sup>, A. Tucholski<sup>o</sup>

# Microscopic investigation on the existence of transverse wobbling under the effect of rotational alignment: the $^{136}\text{Nd}$ case

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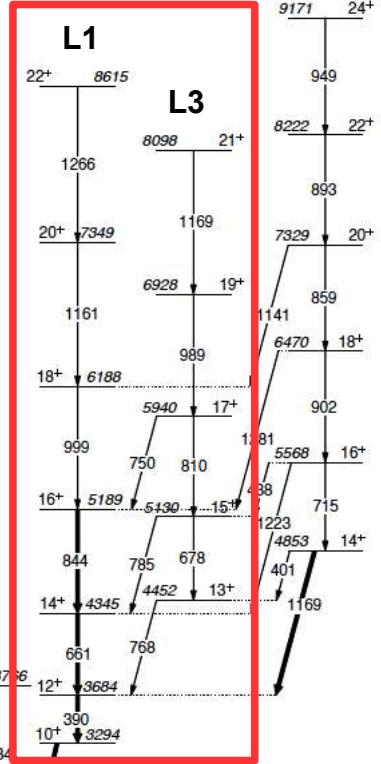
<sup>2</sup>Centre de Sciences Nucléaires et Sciences de la Matière, CNRS/IN2P3,

Université Paris-Saclay, Bâtiment 104-108, 91405 Orsay, France

(Dated: November 11, 2020)

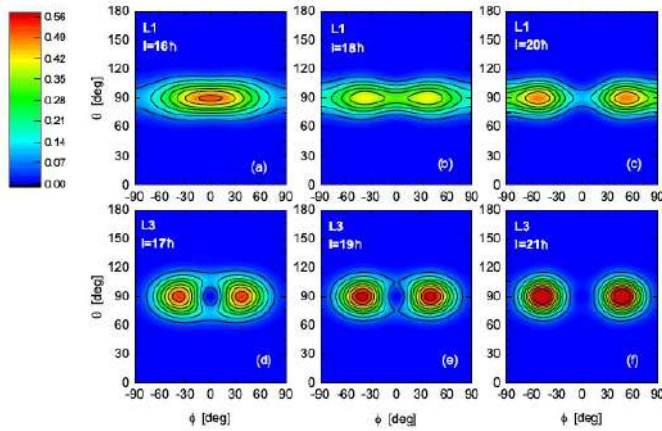
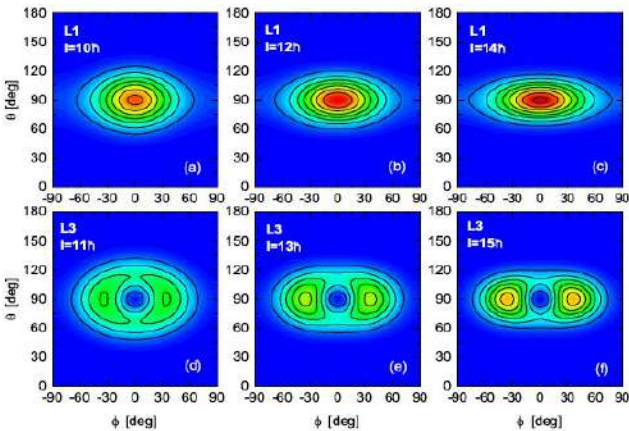
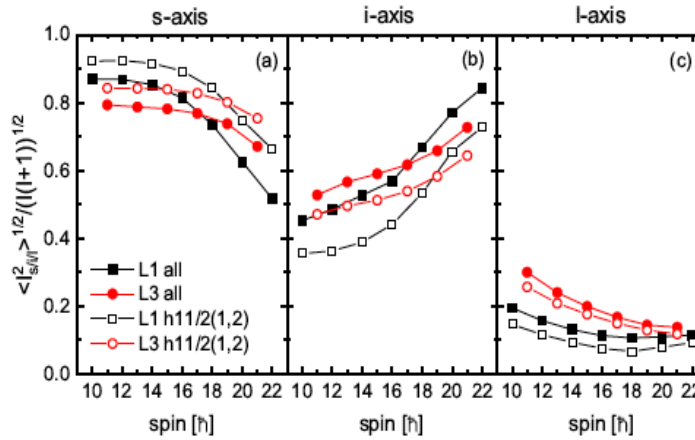
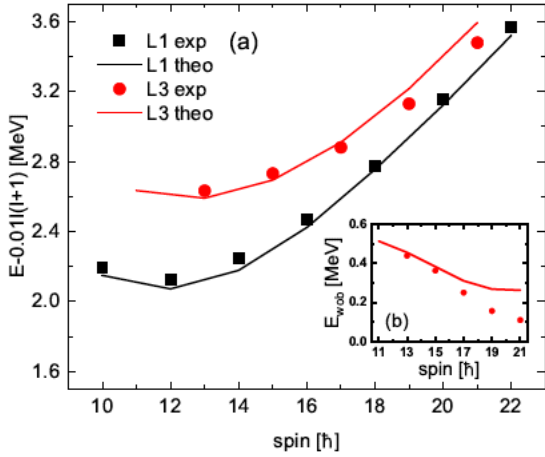
$$\pi(h_{11/2})^2$$

L4



$^{136}\text{Nd}$

L7



# Risk of misinterpretation of low-spin bands in odd-even nuclei as wobbling bands instead of Tilted Precession (TiP) bands

Wobbling at low spins? => NO: not supported by experiment and by theory

$^{135}\text{Pr}$  – no wobbling (1 PLB & 1 PRL submitted)

$^{187}\text{Au}$  – no wobbling (1 PLB submitted)

Tilted Precession at low spin in general – PRC 101, 034306 (2020)

Tilted Precession at low spin in  $^{135}\text{Nd}$  – PRC 103, 044308 (2021)

2-qp wobbling at high spins => YES

2-qp wobbling in  $^{130}\text{Ba}$  – PRC 100, 061301(R) (2019)

2-qp wobbling in  $^{136}\text{Nd}$  – PRC submitted

# Challenges and perspectives for chiral and wobbling bands, and shape coexistence

## Chirality

New types of chiral motion.

Robustness of chirality against other broken symmetries.

## Wobbling

- Consolidate the experimental results, which at present are NOT conclusive, but only SUGGEST the possible existence of low-spin wobbling bands!
- Measurement of mixing ratios with very high precision, therefore high statistics, which imply long beam times and/or very high efficiency setups.

Shape coexistence — new regions, global view

Thank you !