

HINPw6 Workshop

Low energy reactions of halo nuclei

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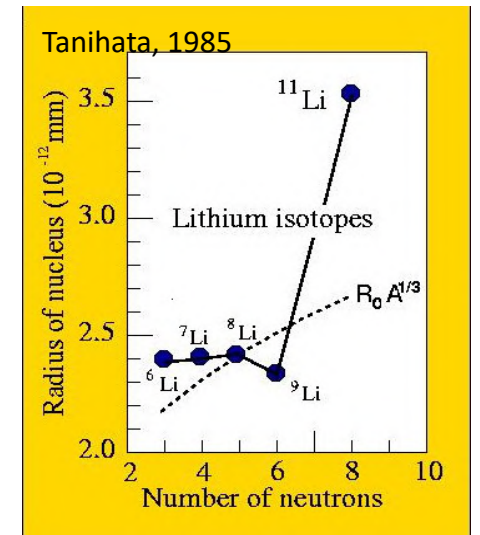
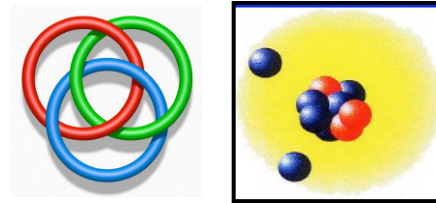
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Low energy reactions of Halo nuclei

Halo nuclei present common structural properties:

- Rather inert core plus one or two barely unbound extra neutrons.
- Often form 3-body borromean systems: ${}^6,8\text{He}$, ${}^{11}\text{Li}$.
- Extended neutron distribution, large "radius". \rightarrow "halo".
- Low binding energy.
- Few bound excited states.



Coulomb barrier energies are interesting to study halo dynamics

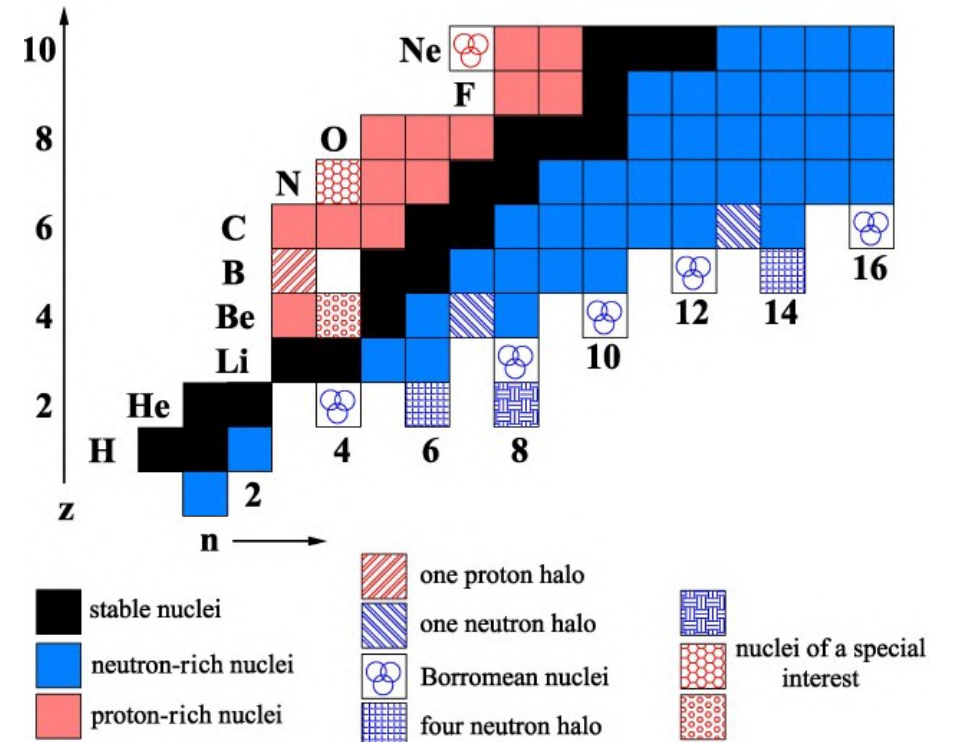
- important correlation between relative motion and internal degrees of freedom.
- strong couplings effects between elastic channel and inelastic, transfer, breakup and fusion channels.
- good energy range to study influence of halo on reaction dynamics.
- probe of theoretical models for few body systems and nucleon correlations.

Elastic Cross Sections

- Large yields at Coulomb barrier.
- Useful to get first information with low intensity RIBs $> 5 \cdot 10^3$ pps.
- Peripheral process, it probes the tail of the nuclear wave function.

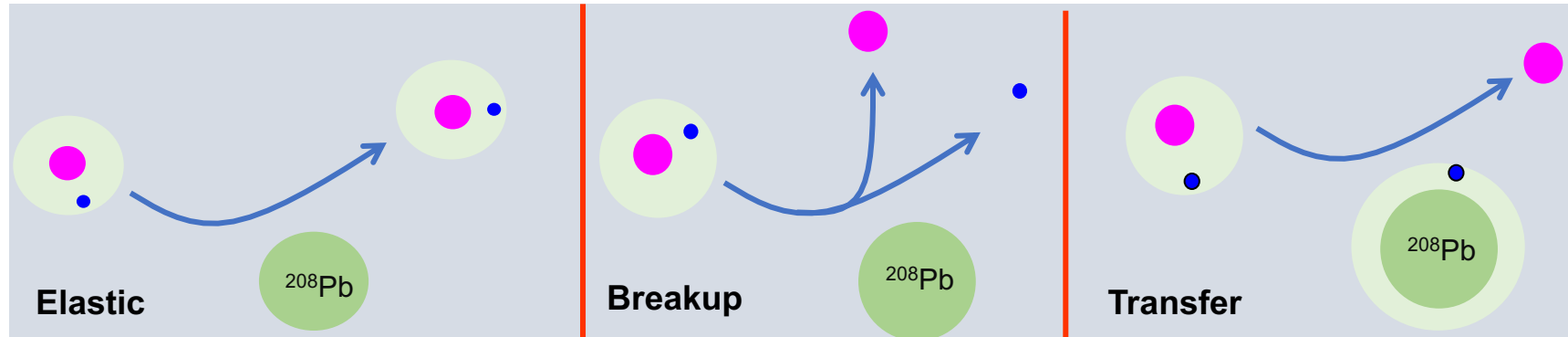
Weak binding + extended neutron distribution

- large coupling to continuum states.
- Soft dipole modes.
- Coulomb dipole polarizability.
- Large breakup yields.

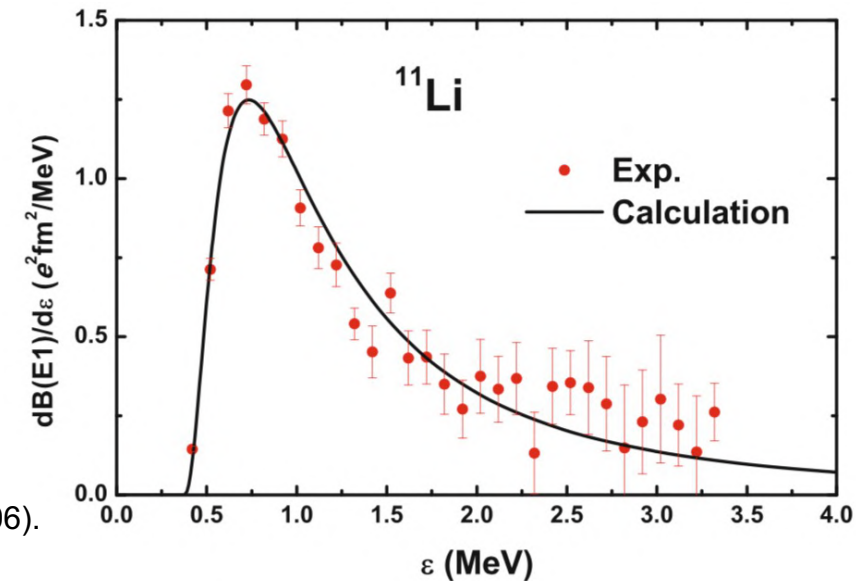
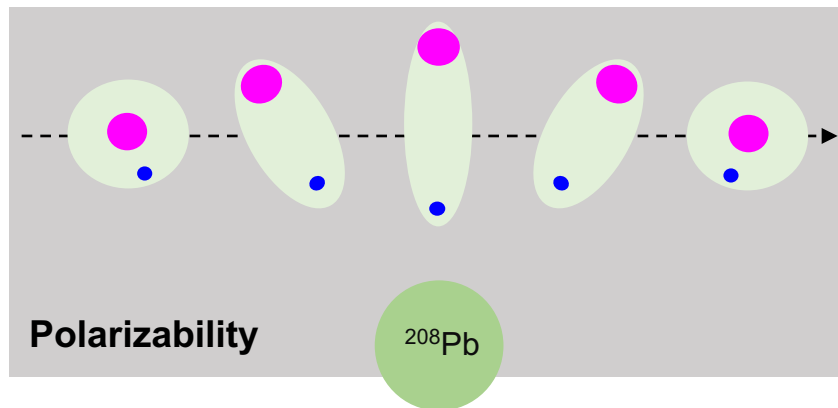


Coulomb barrier scattering of halo nuclei

- Coupling between relative motion and internal degrees of freedom
elastic – inelastic – transfer – breakup – fusion + effects of the continuum
- Strong absorption in elastic channel
- Large cross section for fragmentation



- They are easily polarizable: distortion of structure in the vicinity of target → Coulomb dip. polarizability



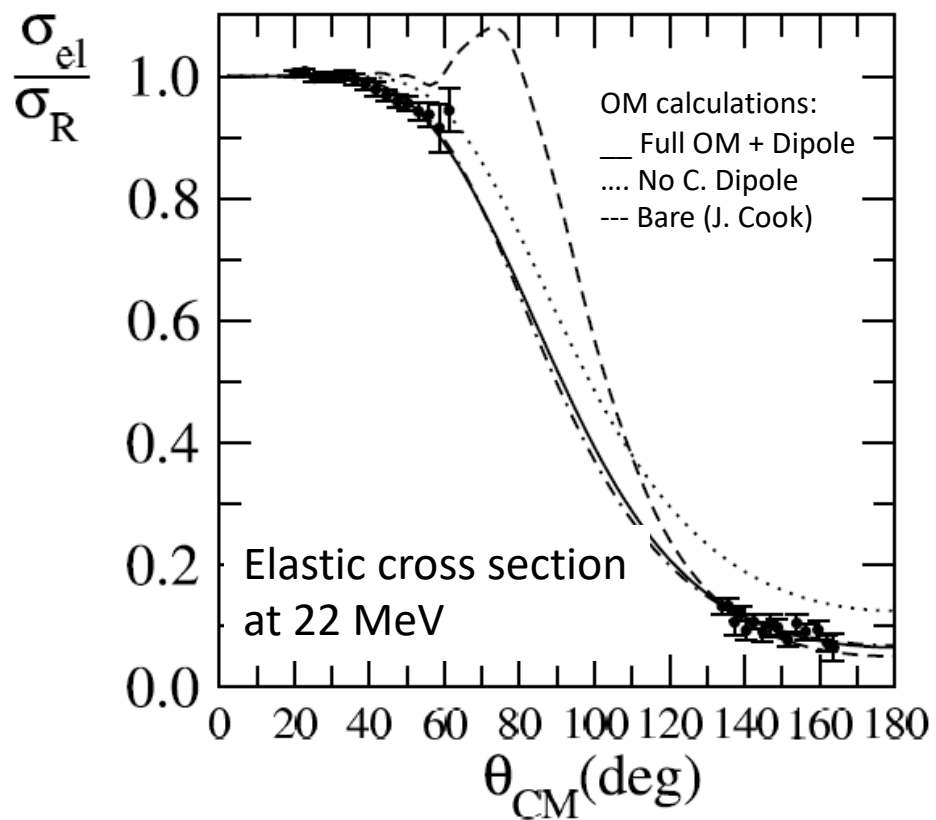
T. Nakamura et al., Phys. Rev. Lett. 96, 252502 (2006).
 T. H. Kim et al., Jour. Kor. Phys. Soc. 73 (2018) 553.

Scattering of ${}^6\text{He}$

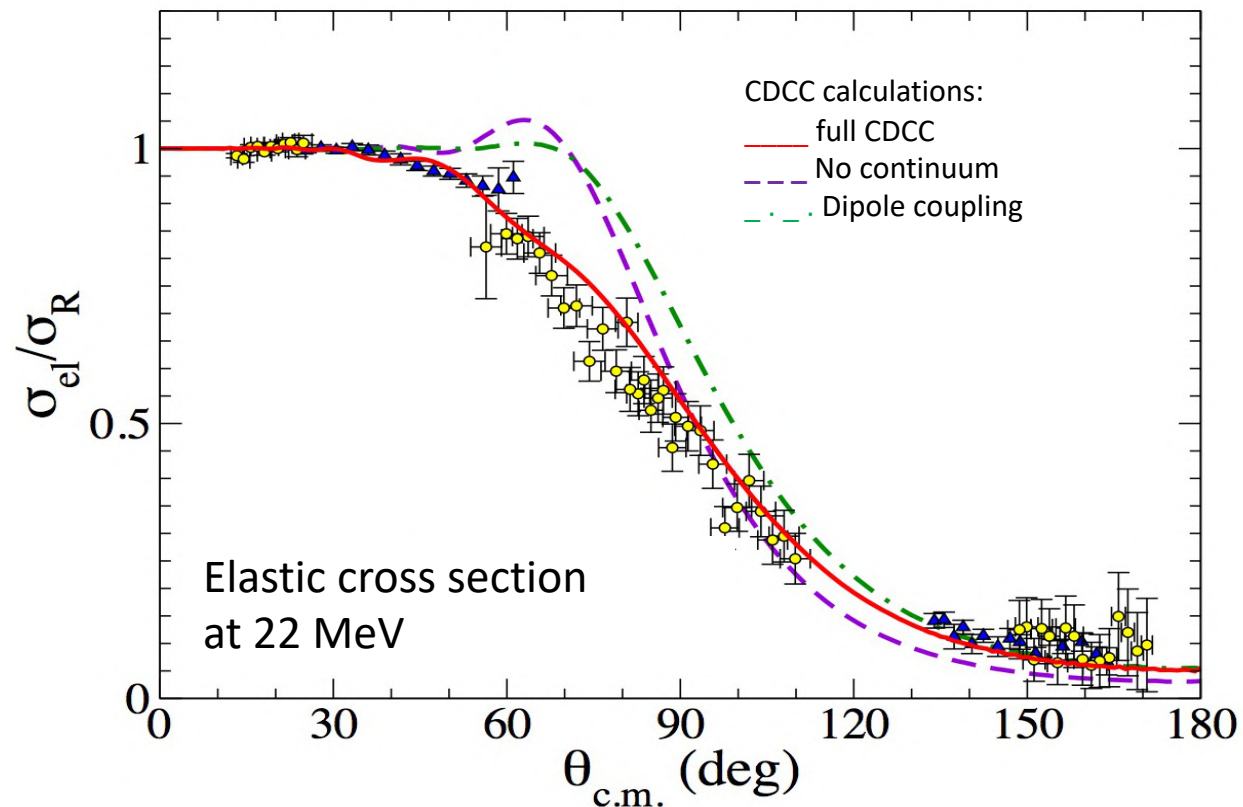
- Halo nucleus with Borromean structure: ($4\text{He} + n + n$); no bound states.
- Most investigated halo nucleus at Coulomb barrier energies (~ 50 data sets-EXFOR).
- ${}^6\text{He}+{}^{208}\text{Pb}$ @ 14,16,18, 22 MeV at CRC (Louvain-la-Neuve, Belgium).

L. Acosta et al., PRC 84(2011) 044604.

A.M. Sánchez-Benítez, et al. NPA 803, 30 (2008)



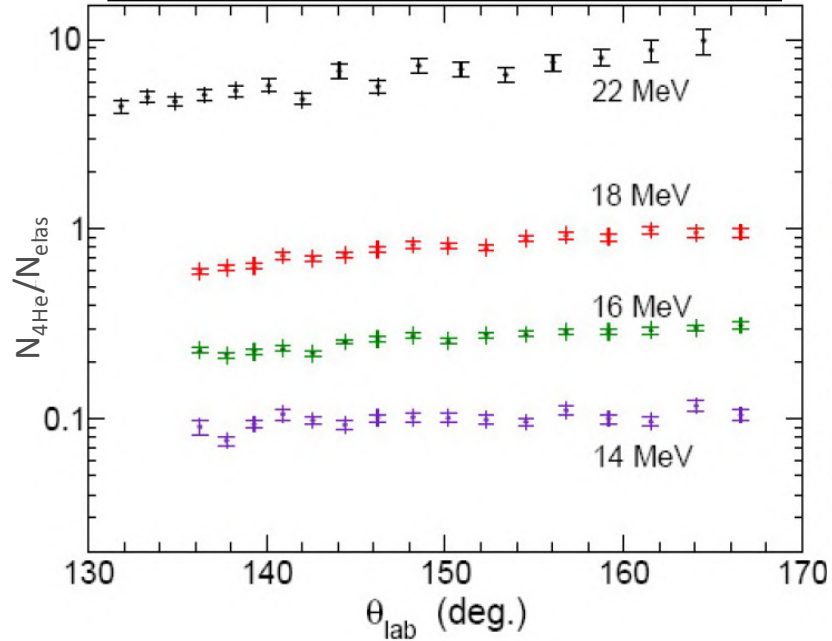
- Strong absorption up to small scattering angles, rainbow disappears.
- Large diffusivity of the OM imaginary potential ~ 1.8 fm
- Long range reaction mechanisms \rightarrow Strong dipole Coulomb couplings



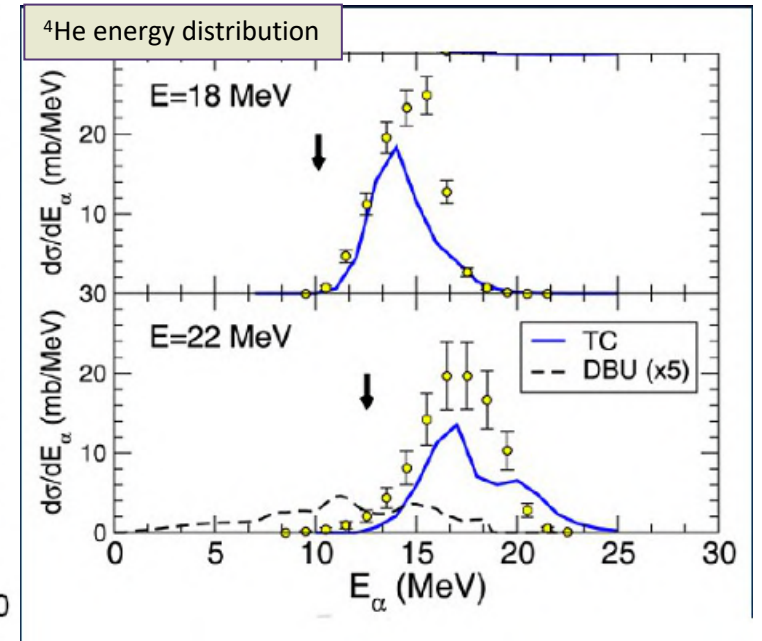
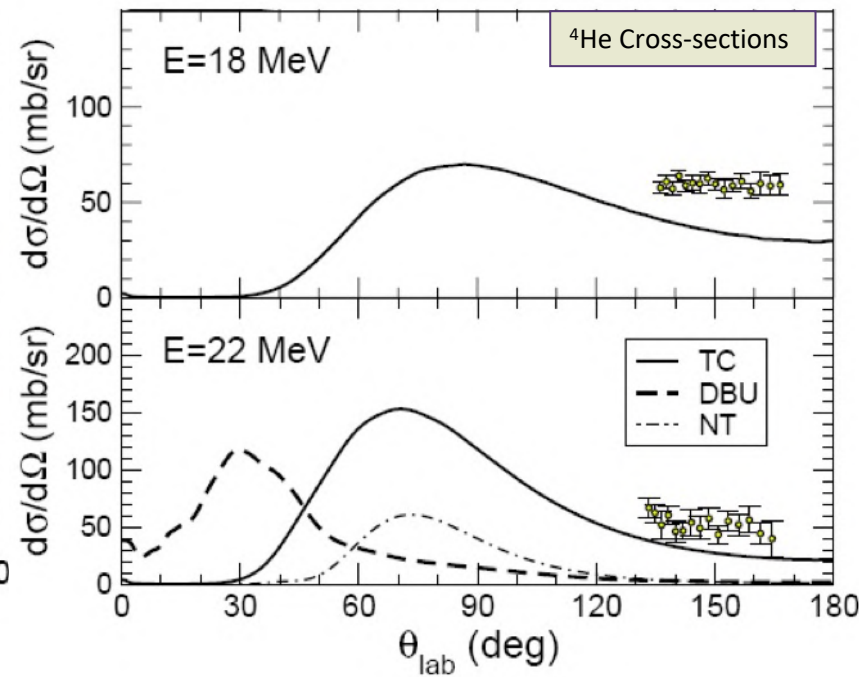
- CDCC calculations describe the data (2n-model)
- Scattering process dominated by: N. Keeley et al., PRC 68, 054601 (2003)
- Dipole couplings (coulomb + nuclear) K. Rusek et al., PRC 72, 037603 (2005).
- Coupling to continuum
- Strong Coulomb couplings due to the high target Z

Scattering of ${}^6\text{He}$

${}^4\text{He}$ Yield vs ϑ_{lab} (normalized to elastic)



D. Escrig et al, NPA 792 (2007), L. Acosta et al., PRC 84(2011) 044604.



- Large alpha yields even at sub-barrier energies (14 MeV, 10% of elastic)
- Large deviation from Rutherford scatt. well below the barrier.
- Forward angles dominated by direct breakup: CDCC calculations (DBU).
- Backward angles dominated by neutron transfer. DWBA calculations:
 - 1n – transfer (NT) gives small contribution.
 - 2n- transfer to the continuum (TC) gives main contribution.

- 2n-transfer describes properly the energy distribution.
- Strong coupling to breakup and transfer channels.
- Testbench for improving dynamic polarization potentials (breakup), polarizability, di-neutron and four body models.

R.S. Machintosh and N. Keley, Phys. Rev. C.79 (2009) 014611

N. Keeley, K.W. Kemper, K. Rusek. Phys. Rev. C.88.017602

A.M. Moro, et al, Phys. Rev. C 75, 064607 (2007)

M. Rodríguez-Gallardo et al., PRC 80, 051601(R)(2009)

V. Morcelle et al, PLB 732, 2014, 228

Scattering of ${}^6\text{He}$

Vast amount of data: systematics of low energy ${}^6\text{He}$ scattering:
[reaction cross sections](#)

A systematic behavior can be found in reactions with several targets and energies by using scaling parameters for energy and radius:

Radius scaling factor: $(A_p^{1/3} + A_t^{1/3}) \sim \text{size}$

Energy scaling factor: $Z_p Z_t / (A_p^{1/3} + A_t^{1/3}) \sim \text{coulomb barrier} \rightarrow E_{\text{reduced}}$

Xsection scaling factor: $R^2 \sim (A_p^{1/3} + A_t^{1/3})^2 \rightarrow \sigma_{\text{reduced}}$

Fit data with Wong's formula:

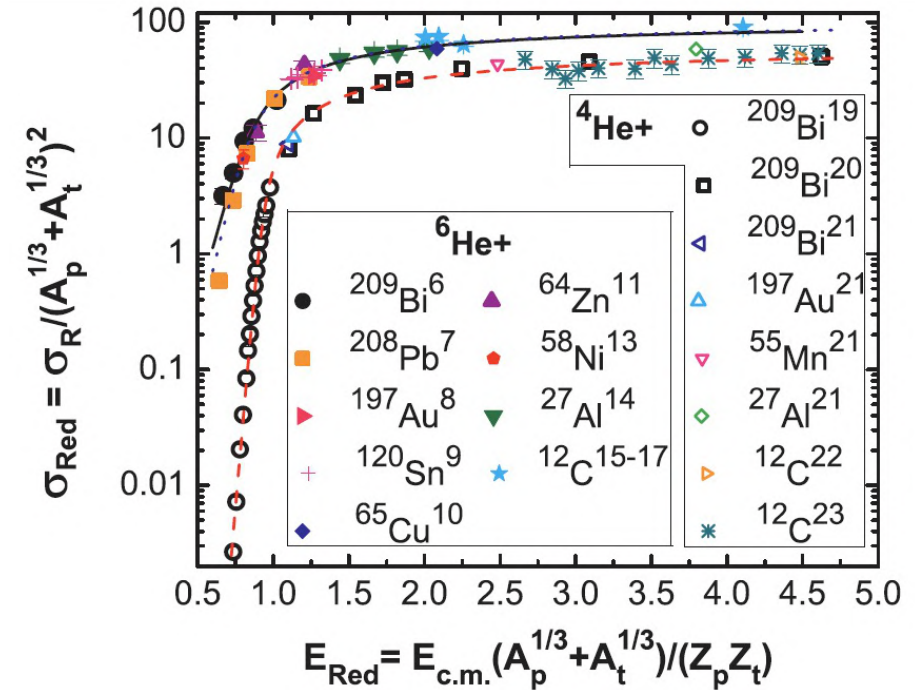
$$\sigma_{\text{Red}}^W = \frac{\epsilon_0 r_{0b}^2}{2E_{\text{Red}}} \ln \left\{ 1 + \exp \left[\frac{2\pi}{\epsilon_0} (E_{\text{Red}} - V_{\text{Red}}) \right] \right\}$$

Results:

Projectile	V_{Red}	r_{0b}	ϵ_0	N_{pts}	χ^2/N
${}^6\text{He}$	0.780 ± 0.014	1.79 ± 0.04	0.43 ± 0.06	28	4.3
${}^4\text{He}$	0.913 ± 0.005	1.39 ± 0.05	0.175 ± 0.006	43	3.4

E.F. Aguilera et al., PRC 83, 021601(R) (2011)

Reaction cross sections for ${}^6\text{He}$ and ${}^4\text{He}$ at several energies and targets



Conclusions:

- Halo effects \rightarrow Reaction barrier becomes lower and narrower \rightarrow increase of reaction Xsection
- "Universal" function for ${}^6\text{He}$ reactions
- Core + halo decoupling: $X_{\text{reac}} = X_{\text{core}} + X_{\text{halo}}$
- Classification of light nuclei: normal, weakly bound, halo

J.J. Kolata and E.F. Aguilera et al., PRC 83, 027603 (2009)

Scattering of ${}^6\text{He}$

Systematics of Elastic scattering angular distributions

The scattering of halo nuclei at low energy system ${}^6\text{He}+{}^{208}\text{Pb}$ also exhibits interesting regularities in the angular distributions of elastic and alpha production cross sections.

Scaling parameters:

- Cross section: \rightarrow Rutherford cross section
- Angle \rightarrow distance of closest approach in coulomb trajectory

$$r_{\max}(\theta) = e^2 (Z_p Z_t / 2 E) (1 + 1/\sin(\theta/2))$$

\rightarrow Semiclassical picture of the reaction process

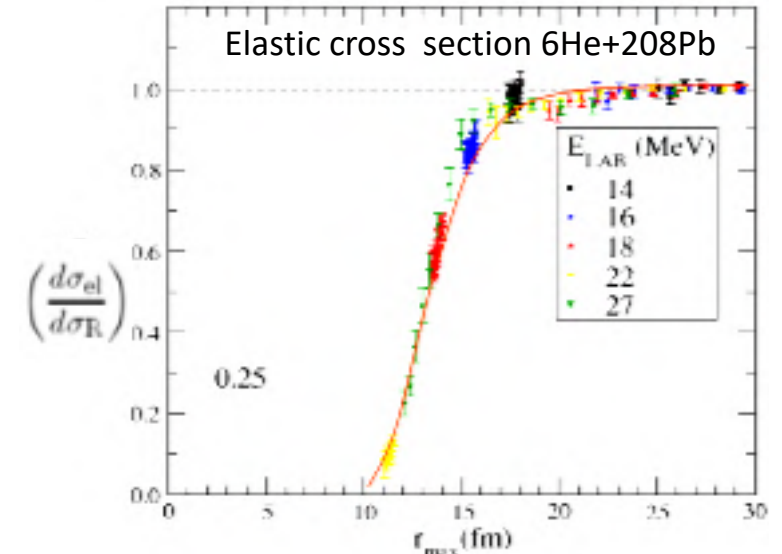
$$\text{Survival probability } \frac{d\sigma_{\text{el}}}{d\sigma_{\text{R}}} = P_{\text{el}} = \exp \left[-\frac{2}{\hbar} \int_{-\infty}^{\infty} W(r(t)) dt \right]$$

- Proximity potential + Coulomb trajectories $W(r) = -W_0 \exp - \left(\frac{r - R}{a} \right)$

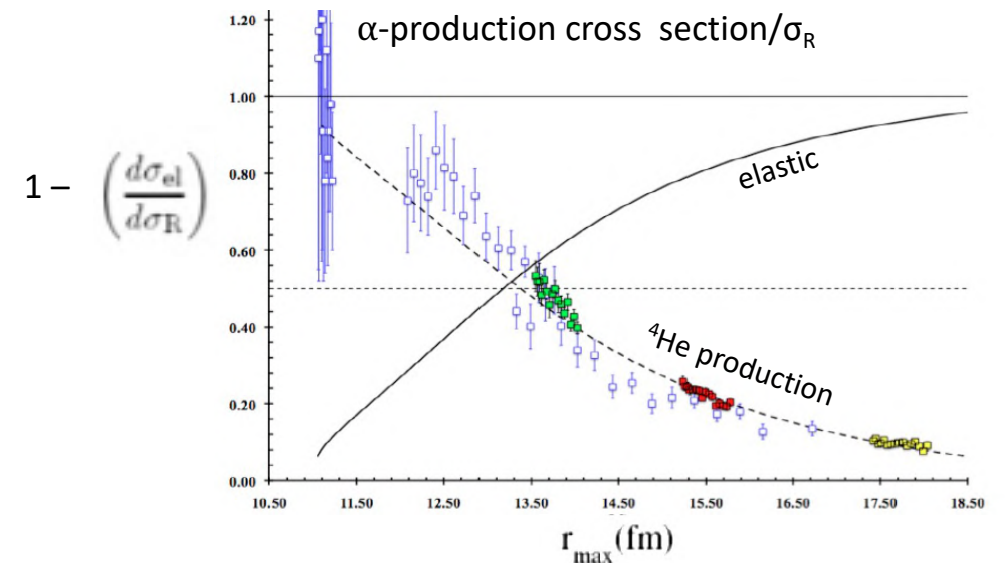
- Analytic result: $\log \left(\frac{d\sigma_{\text{el}}}{d\sigma_{\text{R}}} \right) = -4W_0 \frac{a_0}{\hbar v} \exp \left(\frac{R - a_0}{a} \right) \left[K_0 \left(\frac{a_0}{a} \epsilon \right) + \epsilon K_1 \left(\frac{a_0}{a} \epsilon \right) \right]$

- Systematics \rightarrow Reaction, Elastic and ${}^4\text{He}$ yield
- Reaction dominated by alpha production channels (n-transfer, breakup...)
- Semi-classical picture: reactions produced at distance of closest approach
- "Universal" function for ${}^6\text{He}$ scattering

A.M. Sánchez-Benítez et al., Acta Phys. Pol. B 37 (2006) 1



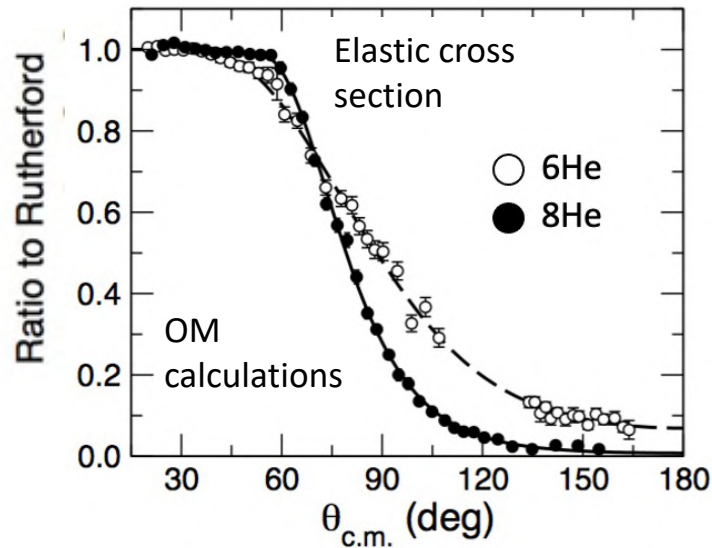
I. Martel, et al. Eur. Phys. Jour. (2011)



Scattering of ^8He

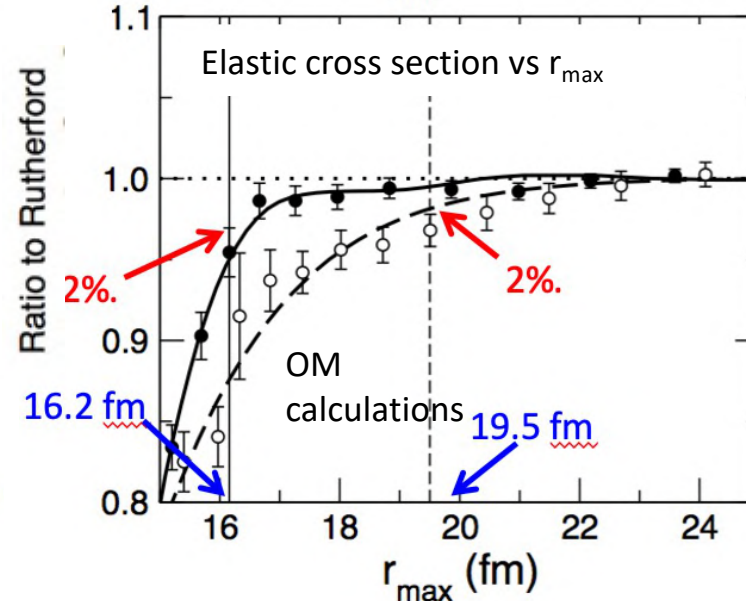
- ^8He is the most neutron-rich particle-stable nucleus with $N/Z = 3 \rightarrow$ borromean neutron skin ($^4\text{He} + n + n + n + n$).
- $^8\text{He} + ^{208}\text{Pb}$ @ 22 MeV at SPIRAL1/GANIL (Caen, France)

G. Marquinez-Durán et al., PRC 94, 064618 (2016), PRC 95 (2018)024602



Elastic cross sections show clear structural effects due to difference between skin and halo

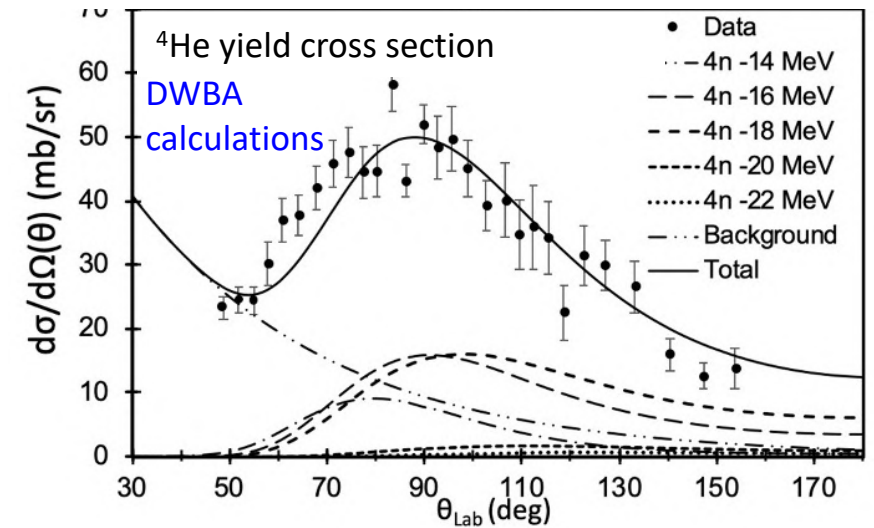
- Suppression of the Coulomb rainbow
- For ^8He (skin): sharp fall-off of the elastic Xsection with with angle; but for ^6He (halo): larger suppression of the Coulomb rainbow, smooth fall-off of elastic Xsec.
- Similar reaction cross sections for $^6\text{He}, ^8\text{He}$ (1500/1400 mb).
- ^8He OP has larger radius and smaller imaginary diffusivity \rightarrow neutron transfer; ^6He : dipole coupling to continuum and breakup;



Semi-classical plot using distance of closest approach in Coulomb trajectories

- Large absorption for $^6\text{He}/^8\text{He}$ at radii well beyond the strong absorption radius, but for ^6He has a much longer range than for ^8He
- Absorption for ^8He has an abrupt decrease with distance whereas for ^6He is very smooth
- ^8He : dominated by neutron stripping at the proximity of the target. ^6He : dipole coupling to continuum and breakup at large distances to the target.

I. Martel et al., PRC 102 (2020) 34609



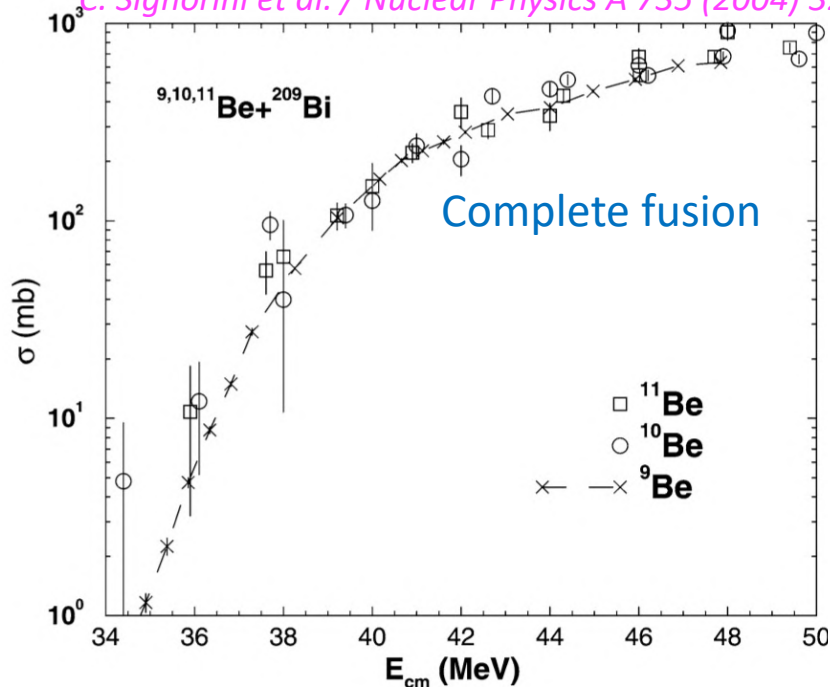
DWBA calculations

- Large cross section for $^6\text{He}, ^4\text{He}$ production (900/400 mb) \rightarrow little room for complete fusion.
- Angular distributions consistent with n transfer.
- ^6He yield (DWBA): Dominated by $1n$ transfer to excited states in ^{209}Pb at $E_x \sim 4$ MeV, small contribution of direct $2n$ transfer.
- ^4He yield (DWBA): Can be described by direct $4n$ transfer at $E_x \sim 18$ MeV.

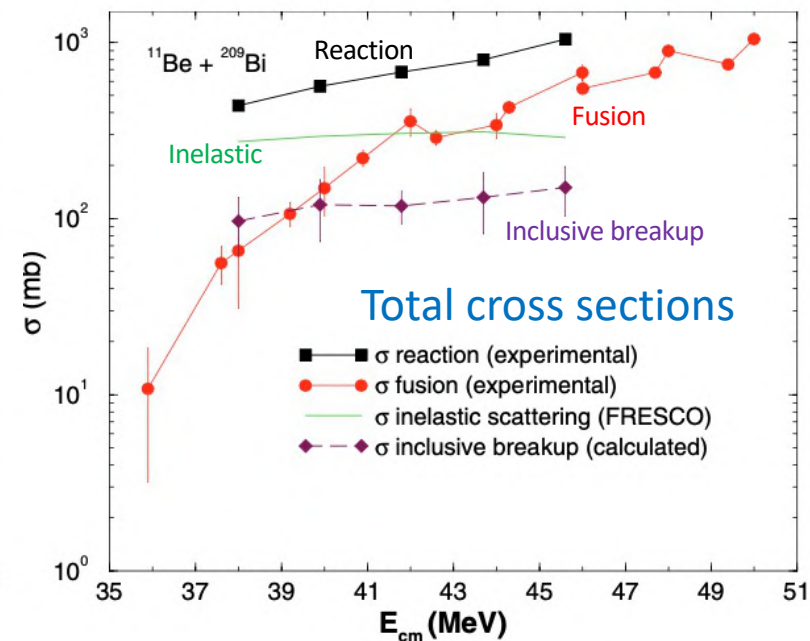
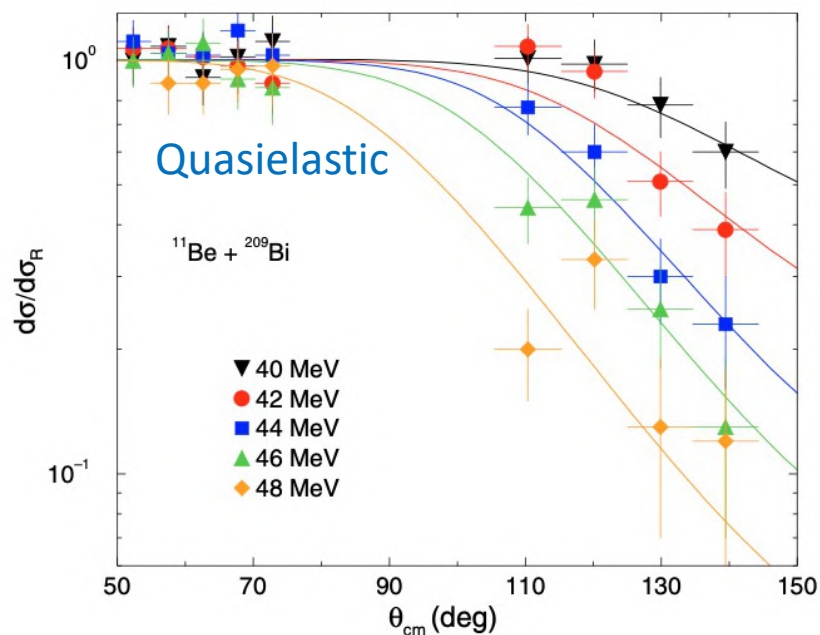
Scattering of ^{11}Be

- ^{11}Be : 1n halo ($^{10}\text{Be}+n$), one bound excited state ($1/2^-$, 320 keV), largest known $B(E1)$ ($ex \rightarrow gs$) \rightarrow first halo discovered
- $^{11}\text{Be}+^{209}\text{Bi}$ @ 35 - 50 MeV at RIKEN RIPS facility
- Inflight method + degraders \rightarrow beam energy event by event via Time-Of-Flight (TOF).

C. Signorini et al. / Nuclear Physics A 735 (2004) 377



M. Mazzocco et al., Eur. Phys. J. A 28, 295 (2006)



- Puzzling result:** very similar data for $^{9,10,11}\text{Be}$.
- Reproduced** by CCFULL, CDCC calculations.
- No sub-barrier hindrance** for ^{11}Be due (expected from halo).
- No sub-barrier hindrance** ^{10}Be (coupling to 1^{st} ex. state, large β_2).
- $^{11}\text{Be} \rightarrow$ competition halo (hindrance) – breakup.
- Similar effects to ^6He fusion.

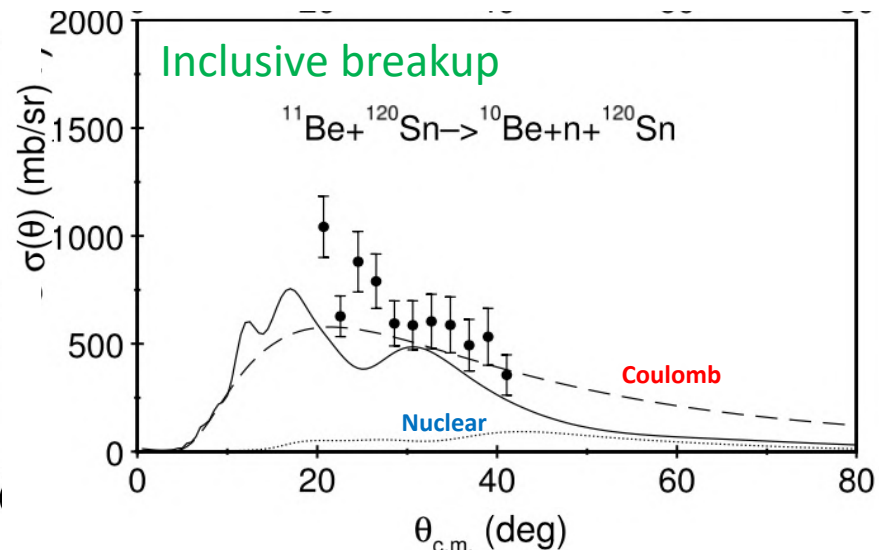
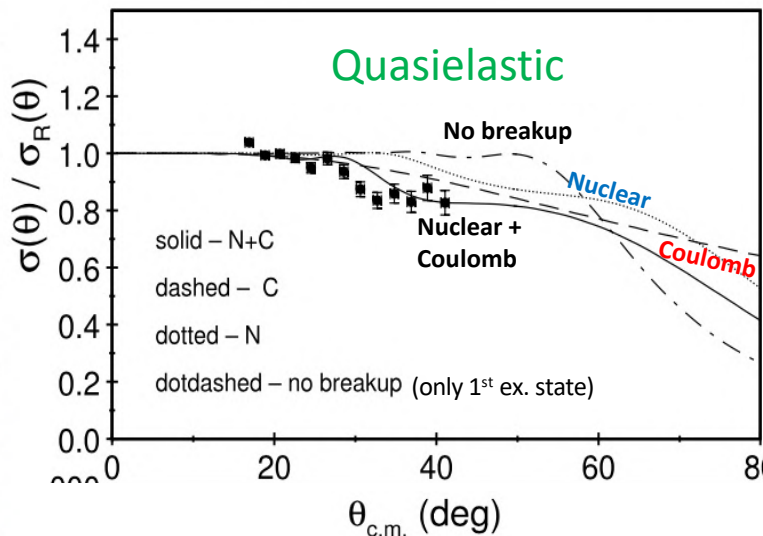
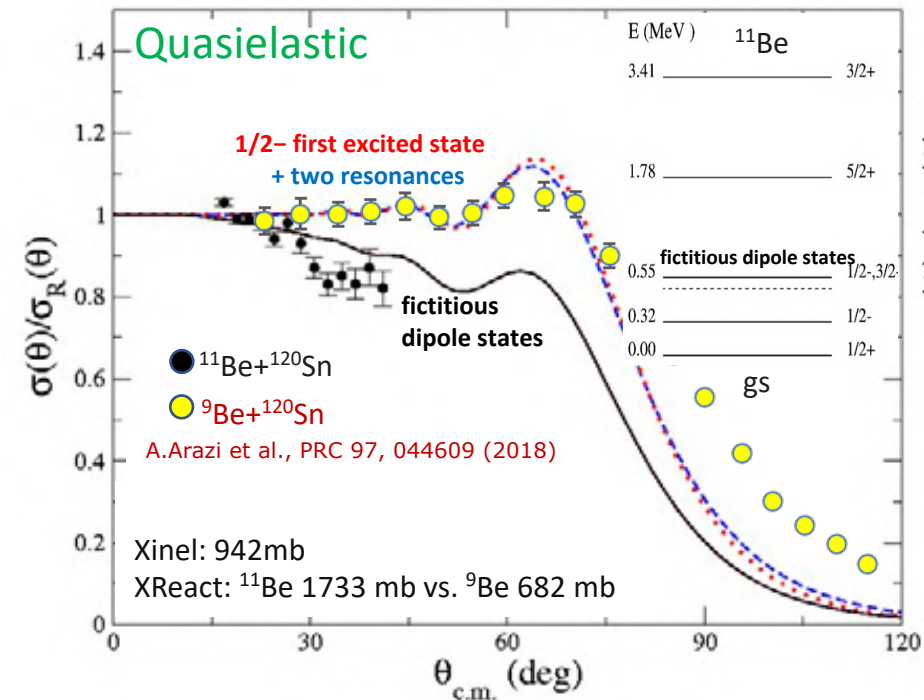
- Data well described** by OM, DWBA and Coupled-Channel formalism with deformation from $B(E1)$.
- Calculated** inelastic cross sections.
- Reaction cross section** $\sim 10 \times$ fusion cross section.
- Derived inclusive breakup cross sections** $\sim 100\text{-}150 \text{ mb}$ \sim relatively small.
- Slightly larger fusion cross sections** for ^{11}Be than ^9Be below the barrier \rightarrow halo effects.

Scattering of ^{11}Be

$^{11}\text{Be} + ^{120}\text{Sn}$ @ 32 MeV (REX-ISOLDE/CERN) \rightarrow ^{11}Be quasielastic and ^{10}Be fragments (breakup)

L. Acosta et al., Eur. Phys. J. A 42, 461 (2009).

K. Rusek et al. 43 (2012) ACTA PHYSICA POLONICA B



- **Coulomb-nuclear interference** is strongly damped.
- **Deviation** from Coulomb $\sim 30^\circ$ cm \rightarrow long range reaction mechanism (CC) calculations: simple vibrational model + Inert target.
- **Deformation** length from $B(E1)$.
- **Two resonant** states at 1.78MeV and 3.41MeV.
- **Coupling to $^{10}\text{Be} + n$ continuum** \rightarrow two fictitious dipole states.
- **Most important effect** is the coupling to the (dipole) continuum.
- No effect of $1/2^-$ state on elastic despite relative large cross section.
- **Small** effect of resonances.

- **CDCC calculations:** weak dependence on $n + ^{10}\text{Be}$ potentials
- **Large transfer/breakup yield** $\sim 50\%$ total.
- **Strong Coulomb-nuclear** interference effect: competition of BOTH Coulomb and **nuclear contributions**; for ^{11}Be 1st excited state \sim destructive interference.
- **Important for BOTH** quasielastic and breakup.
- **Coulomb post-acceleration:** the whole Coulomb potential energy of ^{11}Be is taken by ^{10}Be : larger kinetic energy than predicted from kinematics by ~ 1.8 MeV

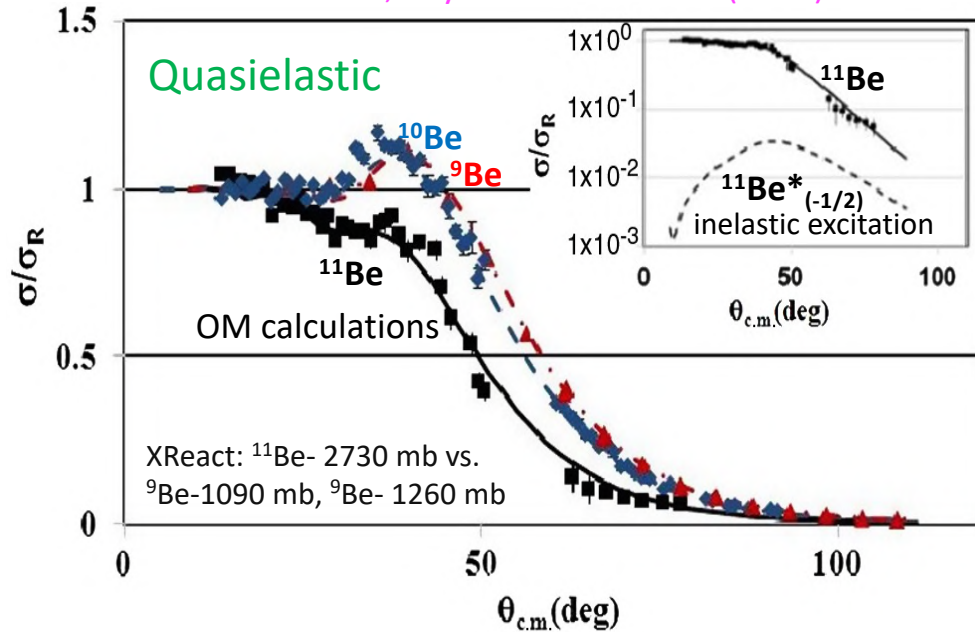
$$\Delta E = \frac{m_n}{m_n + m_c} \frac{Z_c Z_t e^2}{R_{bu}}$$

- \rightarrow ^{11}Be breaks at about ~ 20 fm from the target
- \rightarrow Much larger than strong absorption radius
- \rightarrow large Coulomb effect on breakup

Scattering of ^{11}Be

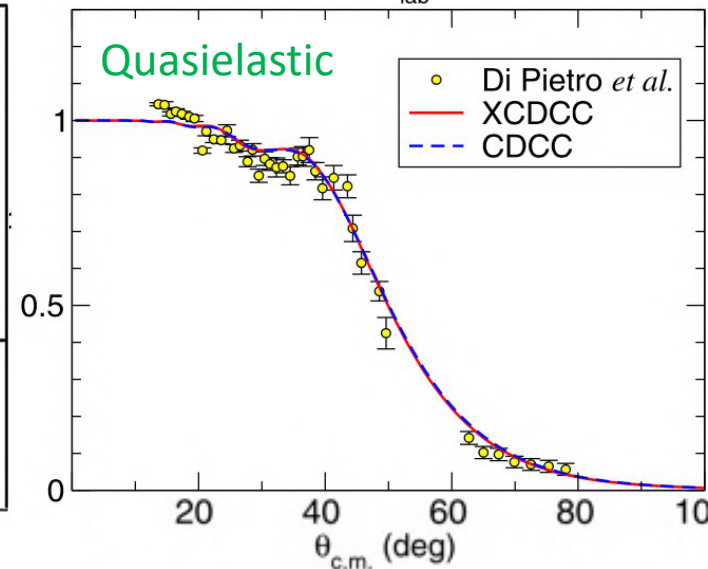
$^{11}\text{Be} + ^{64}\text{Zn}$ @ 28.7 MeV (REX-ISOLDE/CERN) \rightarrow ^{11}Be quasielastic and ^{10}Be fragments (breakup)

A. Di Pietro et al., Physics Letters B 798 (2019) 134954

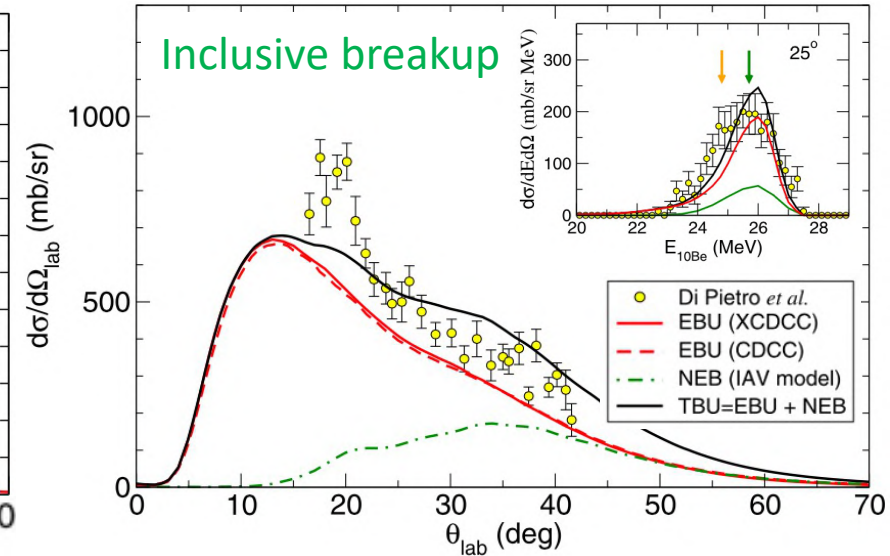


- $^{11}\text{Be} \rightarrow$ Coulomb-nuclear interference is strongly damped.
- Deviation from Coulomb $\sim 30^\circ$ cm \rightarrow long range reaction mechanism.
- Low Z target (Z=30): Coulomb breakup not too strong \rightarrow strong absorption associated with the halo structure.
- Small inelastic contribution \sim COULEX using B(E1).
- ^{11}Be : OM calculations with large imaginary surface term \sim polarization potential to account for the strong reduction of the Coulomb-nuclear interference ($a_i=3.5$ fm) \rightarrow diffuse halo structure \rightarrow long range absorption \sim dynamic polarizability.
- Large transfer/breakup cross section \sim 40% of the reaction cross sections. \sim factor 2 \times $^{9,10}\text{Be}$.

A. Di Pietro et al., Physics Letters B 798 (2019) 134954



- Elastic and non-elastic BU calculations (EBU, NEB)
- EBU: XCDCC calculations \sim effect of core excitation \rightarrow ^{10}Be deformation.
- n- ^{10}Be system particle-plus-rotor model + deformed central potential (^{10}Be ex.)
- Standard CDCC with same parameter to compare effects
- NEB: participant-spectator IAV model (M. Ichimura, N. Austern, C.M. Vincent, PRC32 (1985)431)
- Both XCDCC and CDCC reproduce the Quasielastic cross sections, but the inelastic cross sections differ by $\sim 50\%$ (940mb/450 mb) could only be tested by measuring inelastic.
- Both XCDCC and CDCC underpredict the inclusive BU 20%, the NEB makes an important contribution.
- EBU+NEB consistent with angular and energy distributions of ^{10}Be fragments.
- Coulomb post-acceleration: larger kinetic energy ~ 1 MeV ~ 15 fm angle-independent, consistent with the result of ^{120}Sn scatt. \rightarrow included in EBU+NEB formulation.



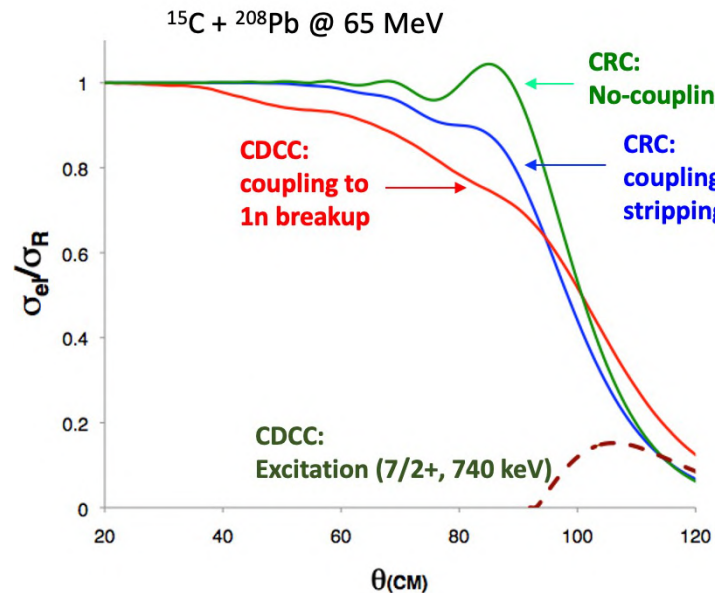
Scattering of ^{15}C

- ^{15}C : 1n-halo ($^{14}\text{C}+n$). **Unique ground** state characterized by $2s_{1/2}$ single-particle configuration. First excited state ($E= 740$ keV).
- Coulomb barrier scattering of $^{15}\text{C} + ^{208}\text{Pb}$ @ 65 MeV
- Recent experiment at HIE-ISOLDE (CERN)

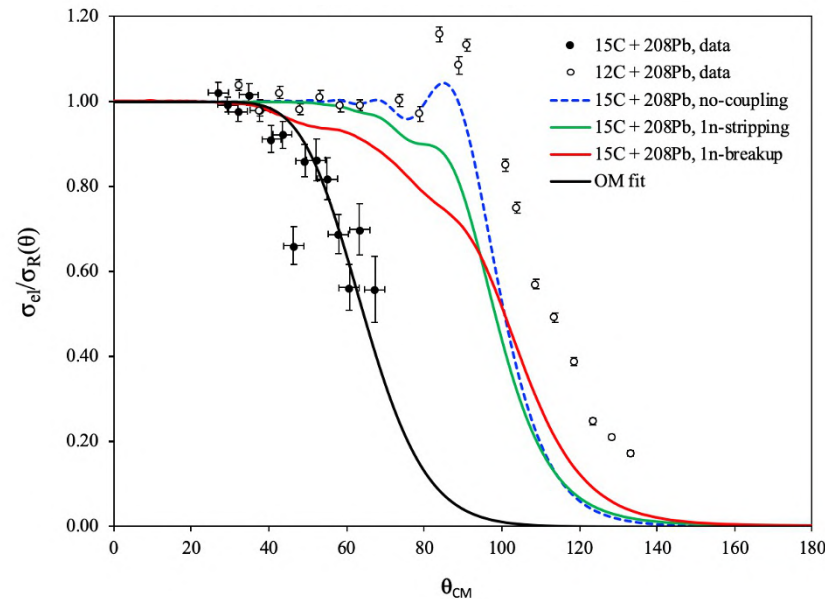
Theoretical studies for the system $^{15}\text{C}+^{208}\text{Pb}$ at Coulomb barrier $\sim E= 65$ MeV.

- 1n-stripping channel: Coupled Reaction Channel calculations (CRC).
- Breakup: Continuum Discretized Coupled Channel Calculations (CDCC).
- Inelastic ($7/2+$, 740 keV): CDCC.

N. Keeley et al., Phys. Rev. C 75 (2007) 054610
 N. Keeley et al., Eur. Phys. J. A 50 (2014) 145.



Preliminary results



Scattering dominated by the competition of one-neutron stripping and breakup.

OM parameters

$$^{15}\text{C} \rightarrow a_w = 1.5 \text{ fm (!!)}$$

- ✓ Stable: ^{12}C , $a_w = 0.4$ fm
- ✓ 1n-halo: ^{11}Be , $a_w = 3.5$ fm
- ✓ 2n-halo: ^6He , $a_w = 2$ fm

Reaction cross sections

$$\sigma_{\text{exp}}(^{15}\text{C}) \sim 3000 \text{ mb} \rightarrow 8 \times \sigma_{\text{exp}}(^{12}\text{C})$$

- ✓ $3 \times \sigma_{\text{th}}(\text{1n-stripping})$
- ✓ $2 \times \sigma_{\text{th}}(\text{1n-breakup})$

CRC/ 1n stripping		CDCC/ direct breakup	
Total reaction (mb)	927	Total reaction (mb)	1379
1-n stripping (mb)	265	Breakup (mb)	462
		Excitation($5/2+$,740keV) (mb)	45

Seems to be an extraordinary result, but:

- Data analysis suffered from low statistics \sim shift forward angular distribution $\sim 20^\circ$
- Requesting more beam time to improve/review the measurement

Summary and conclusions

- Brief summary of relevant results involving Coulomb barrier scattering of ${}^6\text{He}$ (2n-halo), ${}^8\text{He}$ (2n/4n-skin) and ${}^{11}\text{Be}$ (1n-halo), ${}^{11}\text{C}$ (1n-halo).
- Larger reaction cross sections than stable nuclei, dipole polarizability and coupling to the continuum.
- Systematics of reaction cross sections, angular distributions of elastic and core-production cross sections.
- Difference between halo and skins.
- More neutrons do not produce much more fusion \rightarrow breakup.
- Reaction dynamics depends on the particular halo system and target: for large target Z Coulomb effects are more important.
- Core deformation, elastic and inelastic breakup.
- Simpler 3 body models can describe gross properties, core deformation and 4 body models are needed for accurate descriptions.
- Good workbench to test few-body models and nucleon-nucleon correlations, leading to new interesting discoveries.