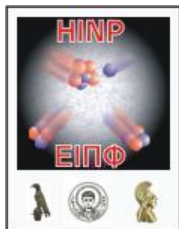




# Model Independent Analysis of the $\gamma^*p \rightarrow \Delta$ Transition with Polarized Electron Scattering Data

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One-Day Workshop on New Aspects and Perspectives in Nuclear Physics  
September 8, 2012  
University of Ioannina, Greece

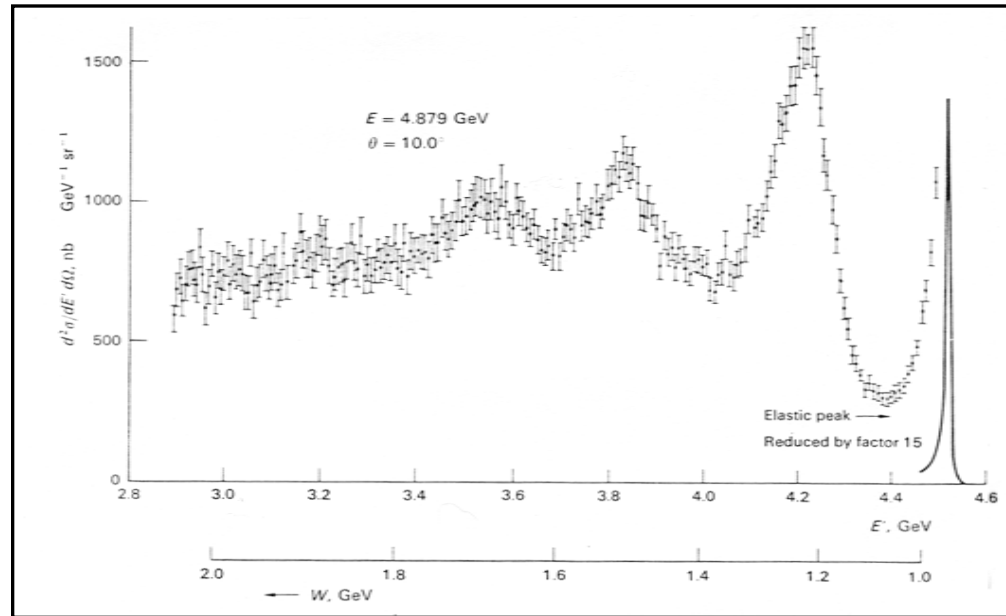


# The signal for deformation in the $\gamma^* N \rightarrow \Delta$ transition

$p(qqq)$

$$I = \frac{1}{2} \quad J = \frac{1}{2}$$

938 MeV



$\Delta(qqq)$

$$I = \frac{3}{2} \quad J = \frac{3}{2}$$

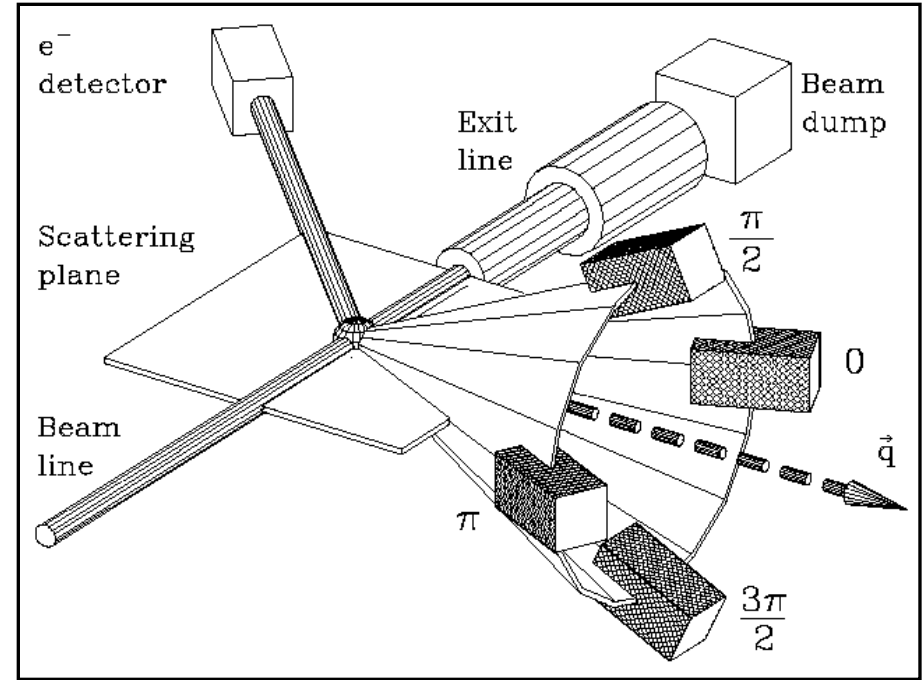
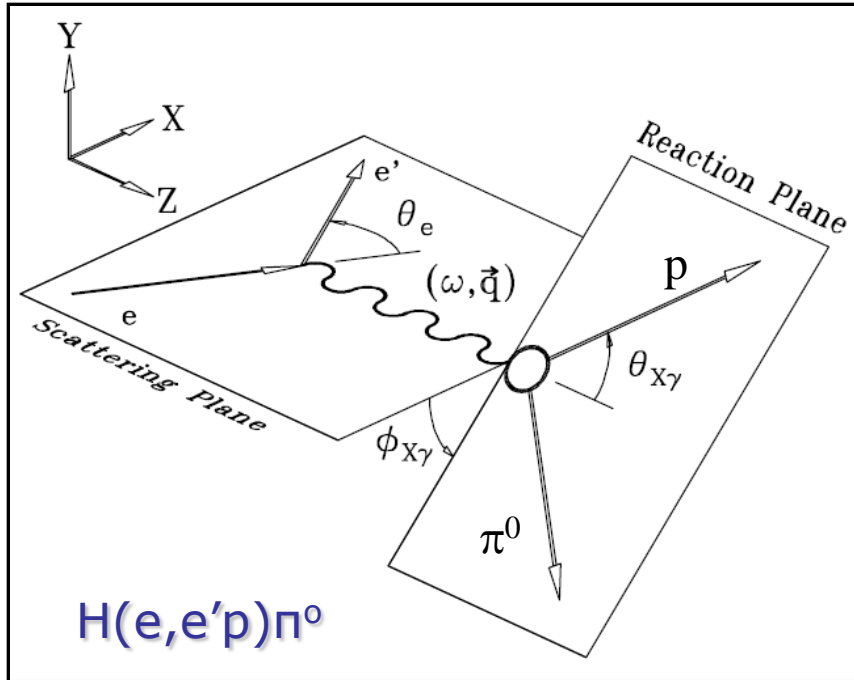
1232 MeV

Spherical  $\Rightarrow$  M1

Deformed  $\Rightarrow$  M1, E2, C2      Deformation signal

$$\left\{ \begin{array}{l} \text{CMR} = \text{Re} \left( \frac{S_{1+}^{3/2}}{M_{1+}^{3/2}} \right) \\ \text{EMR} = \text{Re} \left( \frac{E_{1+}^{3/2}}{M_{1+}^{3/2}} \right) \end{array} \right.$$

# Out of Plane Spectroscopy



$$\sigma = J_{\Omega} \Gamma_v \frac{p_{\text{cm}}}{k_{\text{cm}}} \left( R_T + \epsilon_L R_L + \epsilon R_{TT} \cos 2\phi_{X\gamma} - v_{LT} R_{LT} \cos \phi_{X\gamma} - h v'_{LT} R'_{LT} \sin \phi_{X\gamma} \right)$$

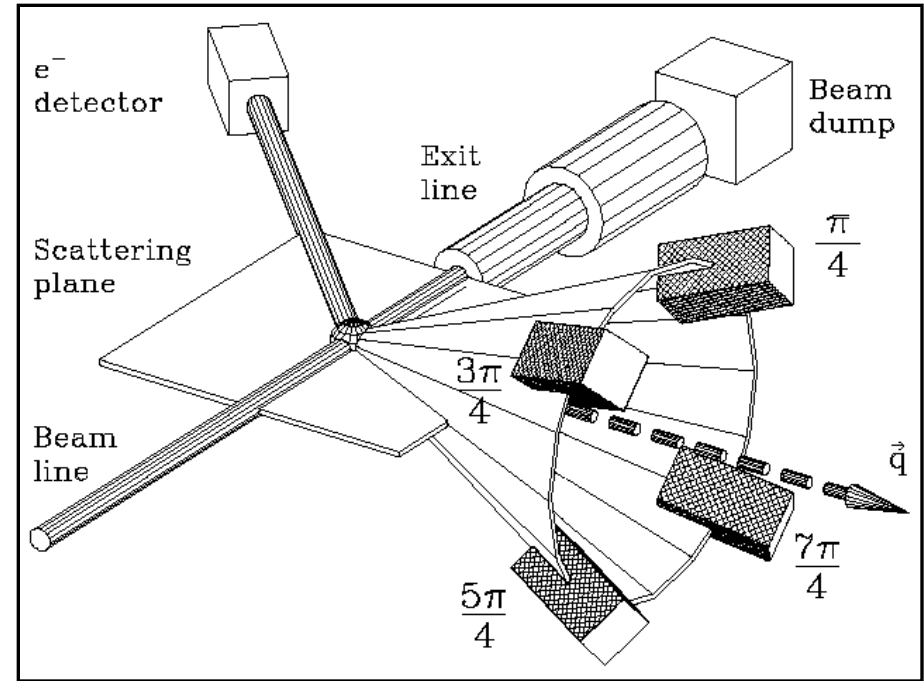
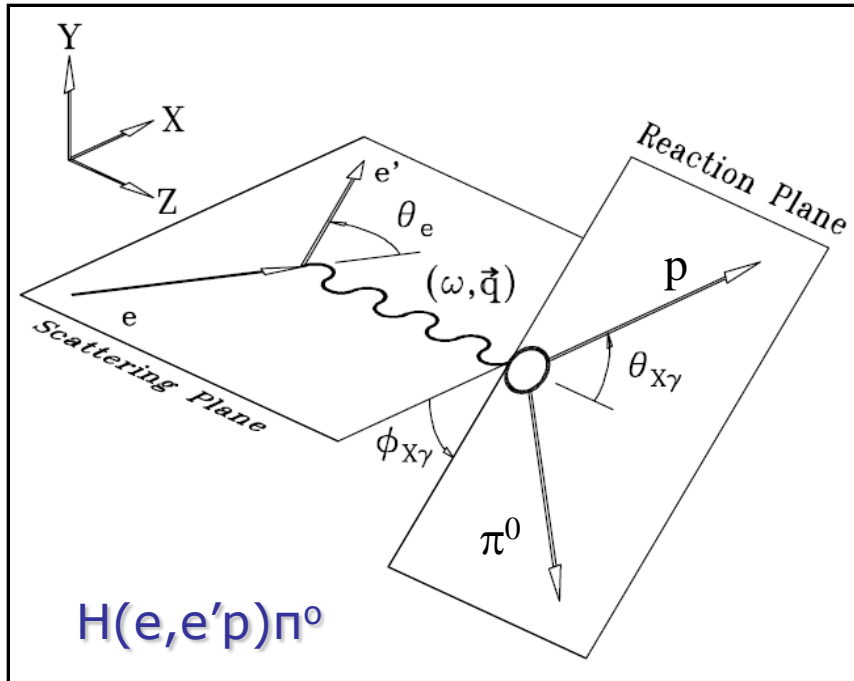
$$R_T + \epsilon_L R_L = \frac{\sigma_0 + \sigma_{\pi/2} + \sigma_{\pi} + \sigma_{3\pi/2}}{4K}$$

$$R_{TT} = \frac{\sigma_0 - \sigma_{\pi/2} + \sigma_{\pi} - \sigma_{3\pi/2}}{4K\epsilon}$$

$$R_{LT} = \frac{\sigma_{\pi} - \sigma_0}{2K v_{LT}}$$

$$R'_{LT} = \frac{\sigma_{3\pi/2} - \sigma_{\pi/2}}{2K h v'_{LT}}$$

# Out of Plane Spectroscopy



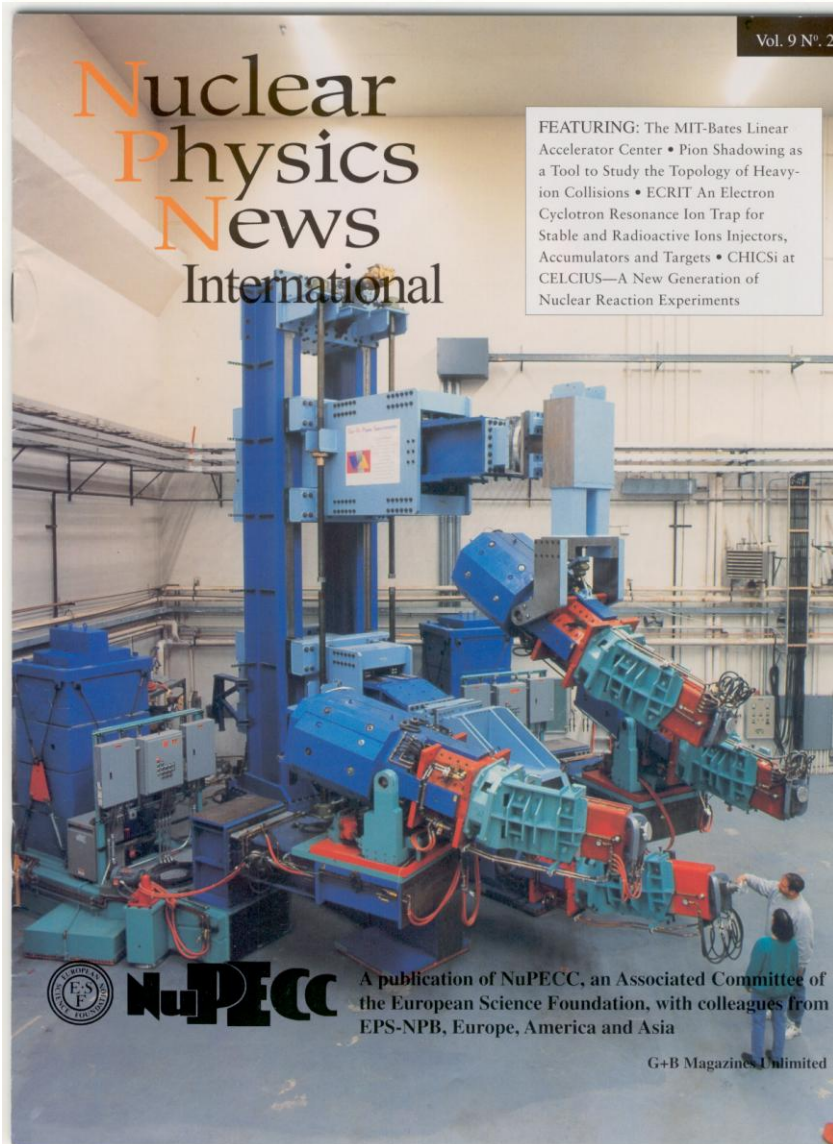
$$\sigma = J_{\Omega} \Gamma_v \frac{p_{\text{cm}}}{k_{\text{cm}}} \left( R_T + \epsilon_L R_L + \epsilon R_{TT} \cos 2\phi_{X\gamma} - v_{LT} R_{LT} \cos \phi_{X\gamma} - h v'_{LT} R'_{LT} \sin \phi_{X\gamma} \right)$$

$$R_T + \epsilon_L R_L = \frac{\sigma_{\pi/4} + \sigma_{5\pi/4}}{2K}$$

$$R_{LT} = \frac{\sigma_{3\pi/4} - \sigma_{\pi/4}}{\sqrt{2}K v_{LT}}$$

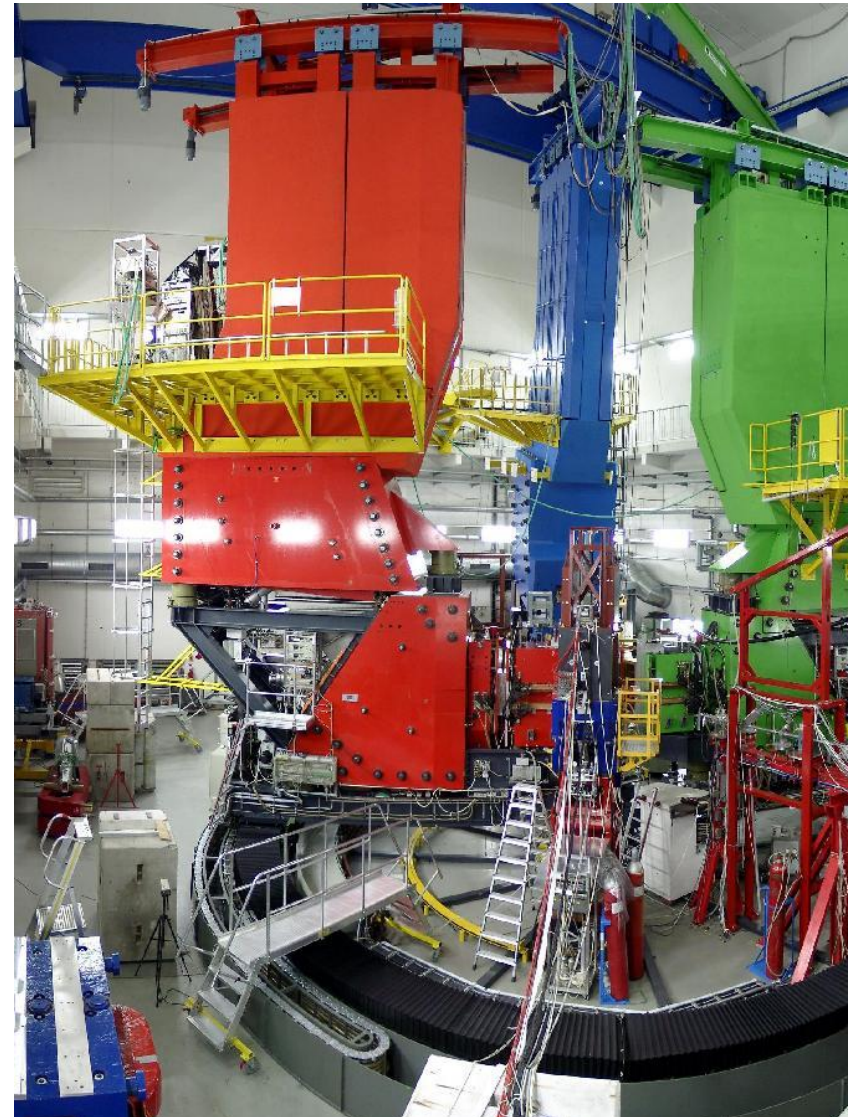
$$R'_{LT} = \frac{\sigma_{5\pi/4} - \sigma_{3\pi/4}}{\sqrt{2}K h v'_{LT}}$$

# OOPS Spectrometer MIT-Bates Linear Accelerator



Proposed and designed by C.N. Papanicolas

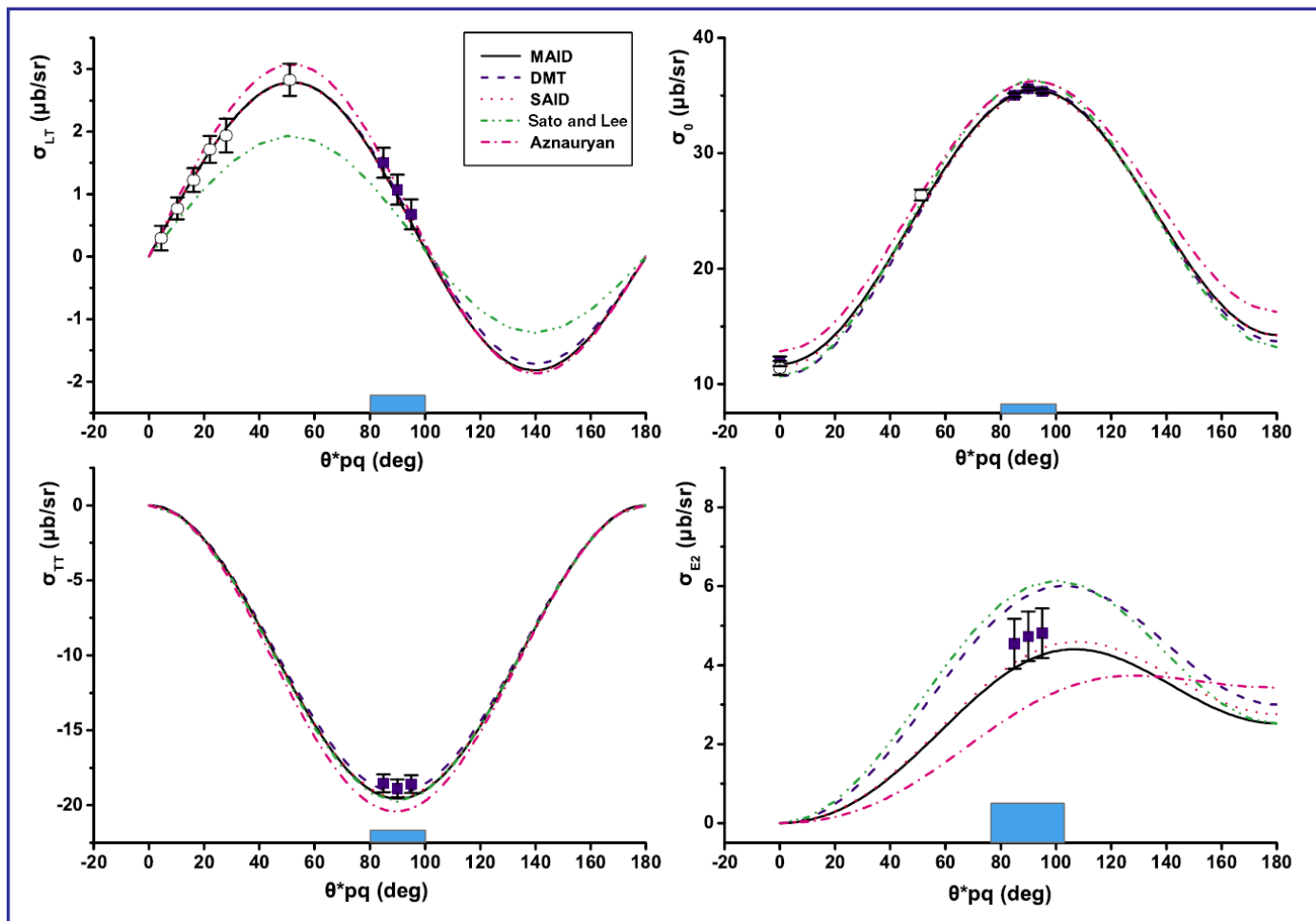
# A1 Spectrometer MAMI – Mainz, Germany



alignment precision: 1 mm , 1 mrad

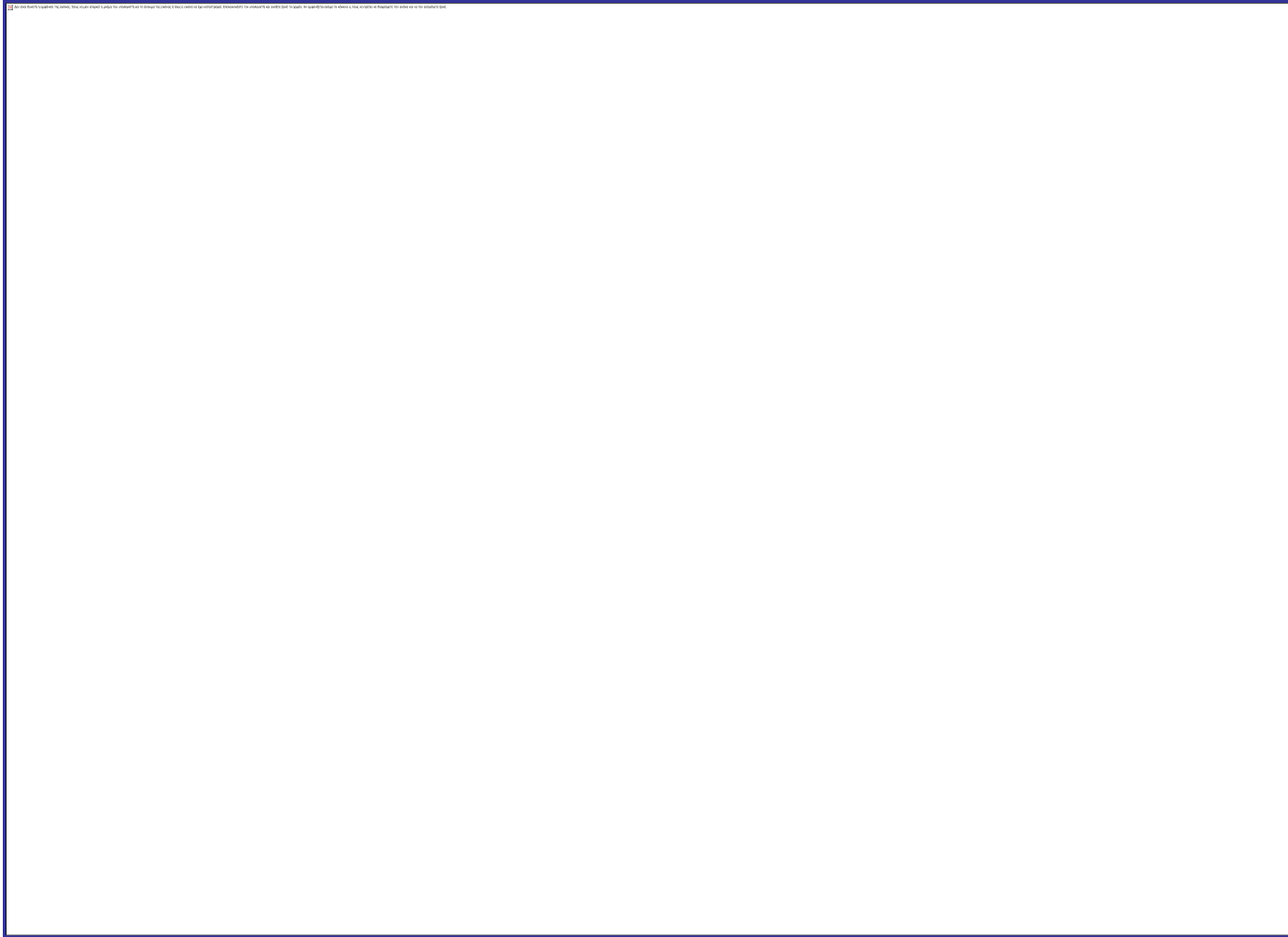
# H(e,e'p) $\pi^0$ Measurements at the $\Delta(1232)$ Resonance

OOPS Collaboration,  $Q^2=0.127$  (GeV/c) $^2$



# H(e,e'p) $\pi^0$ Measurements at the $\Delta(1232)$ Resonance

A1 Collaboration,  $Q^2=0.200$  (GeV/c)<sup>2</sup>



# Model Errors

- Extracted amplitudes and their ratios (EMR, CMR) are characterized by statistical, systematic and model error.
- Model error often dominates.
- So far we have only guestimates, at best!

## A Model Independent Analysis Scheme

### AMIAS

Based on statistical concepts and Monte Carlo techniques

- **E. Stiliaris and C.N. Papanicolas:** *"Multipole Extraction: A Novel, Model Independent Method"*, AIP Vol. **904** (2007) 257-268.
- **C.N. Papanicolas and E. Stiliaris:** *"A Novel Method of Data Analysis for Hadronic Physics"*, <http://arxiv.org/abs/1205.6505v1>, submitted for publication.



# Multipole Expansion

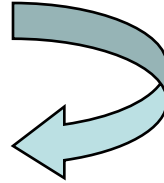
$$\begin{aligned}
 F_1(W, z) &= \sum_0^{\infty} \gamma \left\{ \left[ \gamma M_{\gamma+}(W) + E_{\gamma+}(W) \right] P_{\gamma+1}'(z) + \left[ (\gamma+1) M_{\gamma-}(W) + E_{\gamma-}(W) \right] P_{\gamma-1}'(z) \right\} \\
 F_2(W, z) &= \sum_1^{\infty} \gamma \left[ (\gamma+1) M_{\gamma+}(W) + \gamma M_{\gamma-}(W) \right] P_{\gamma}'(z), \\
 F_3(W, z) &= \sum_1^{\infty} \gamma \left\{ \left[ (E_{\gamma+}(W) - M_{\gamma+}(W)) \right] P_{\gamma+1}''(z) + \left[ E_{\gamma-}(W) + M_{\gamma-}(W) \right] P_{\gamma-1}''(z) \right\}, \\
 F_4(W, z) &= \sum_2^{\infty} \gamma \left[ M_{\gamma+}(W) - E_{\gamma+}(W) - M_{\gamma-}(W) - E_{\gamma-}(W) \right] P_{\gamma}''(z), \quad (C.7) \\
 F_5(W, z) &= \sum_0^{\infty} \gamma \left[ (\gamma+1) L_{\gamma+}(W) P_{\gamma+1}'(z) - \gamma L_{\gamma-}(W) P_{\gamma-1}'(z) \right] \\
 F_6(W, z) &= \sum_1^{\infty} \gamma \left[ \gamma L_{\gamma-}(W) - (\gamma+1) L_{\gamma+}(W) \right] P_{\gamma}'(z).
 \end{aligned}$$

## Chew-Goldberger-Low-Nambu (CGLN) Amplitudes

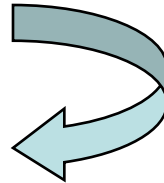
E. Amaldi, S. Fubini and G. Furlan: *Pion-Electroproduction* (1979) Springer Verlag

$E_L^+, E_L^-, M_L^+, M_L^-, L_L^+, L_L^-$

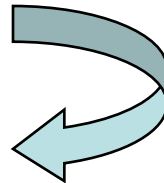
$0 \leq L \leq L_{\text{cut}}$



$F_1, F_2, F_3, F_4, F_5, F_6$  (CGLN)

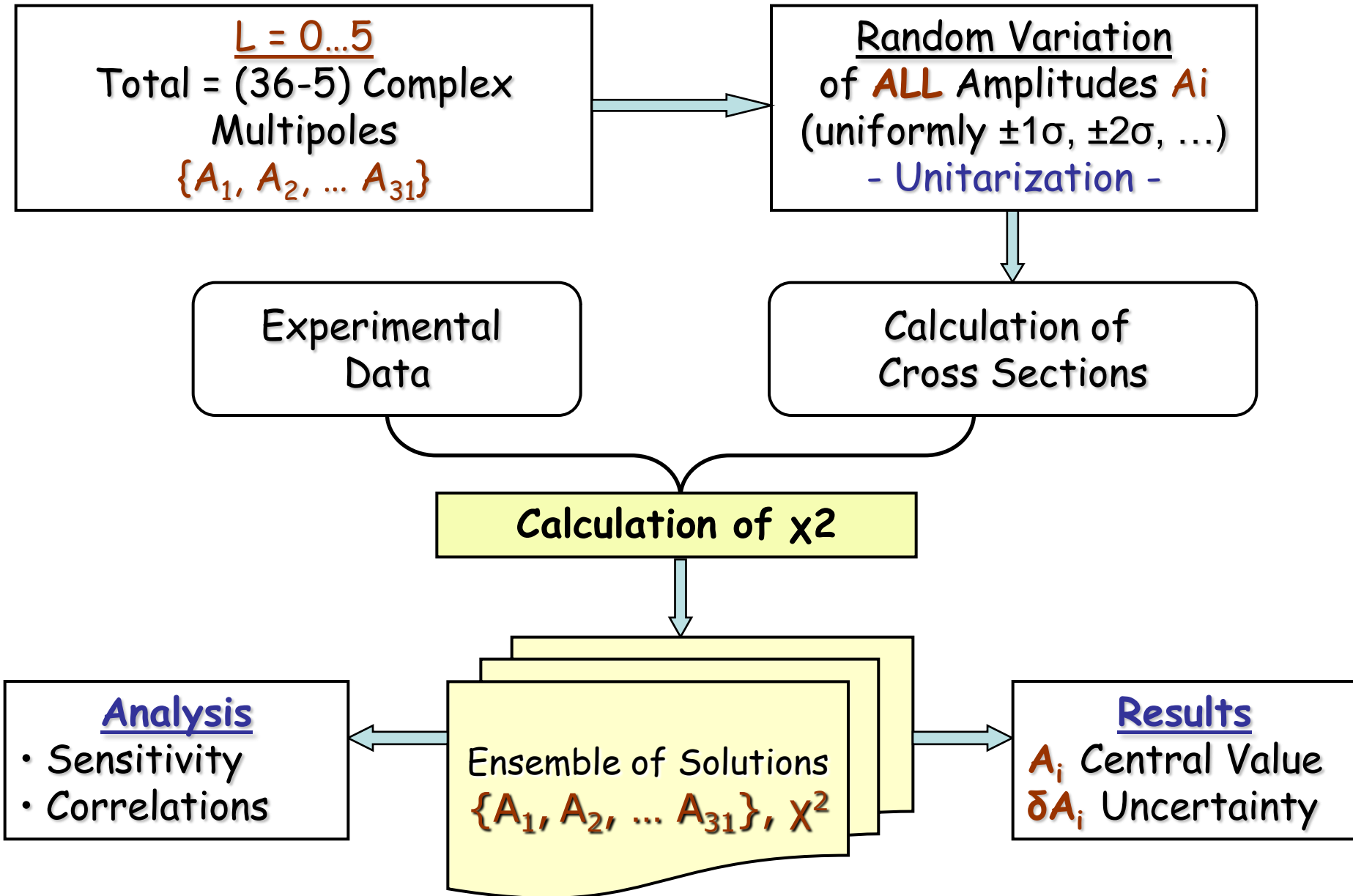


Response Functions:  $R_T, R_L, R_{TT}, R_{LT}, \dots$



OBSERVABLES

# AMIAS Flowchart (Multipole Extraction)



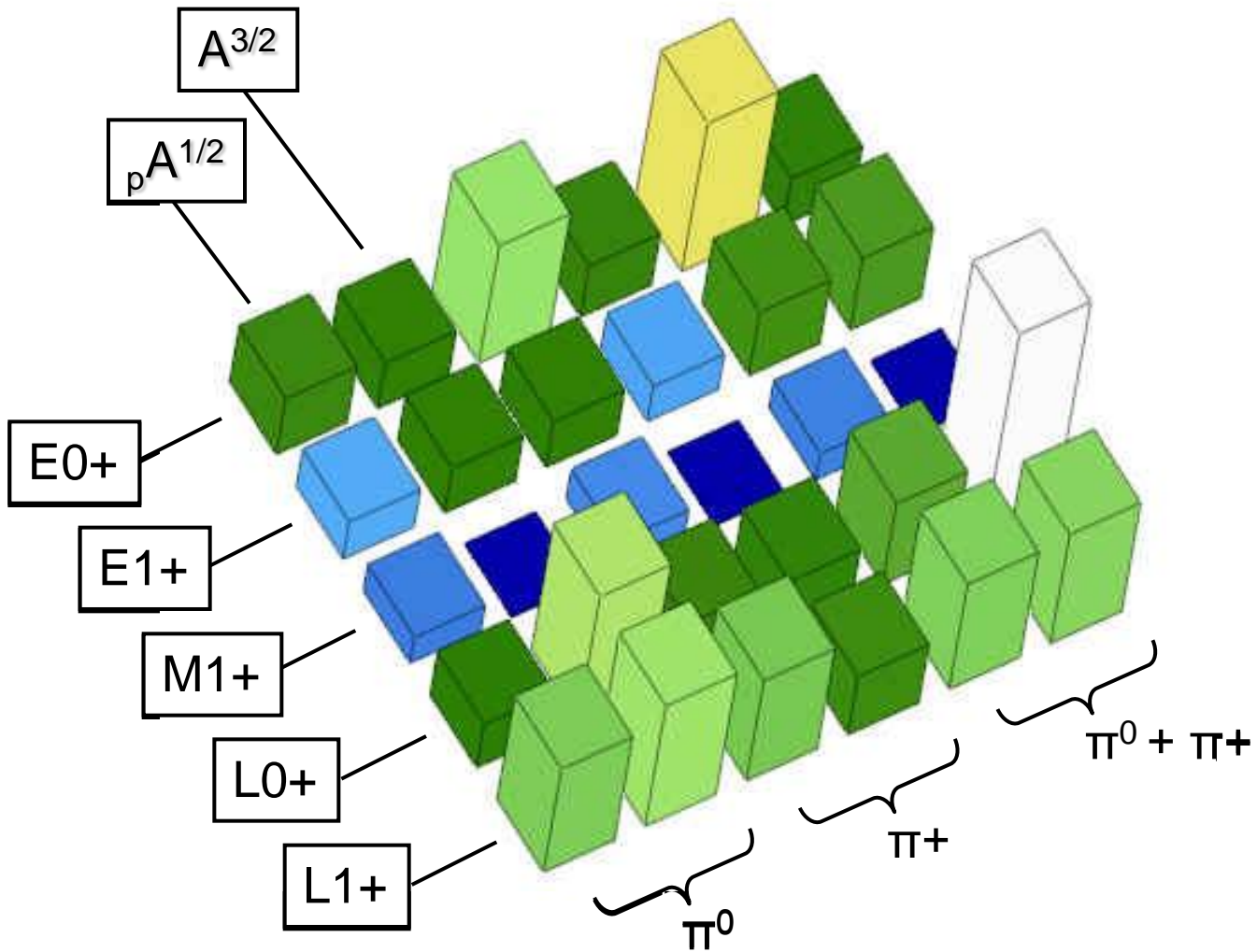
E0+	E0-	M0+	M0-	L0+	L0-
E1+	E1-	M1+	M1-	L1+	L1-
E2+	E2-	M2+	M2-	L2+	L2-
E3+	E3-	M3+	M3-	L3+	L3-
E4+	E4-	M4+	M4-	L4+	L4-
E5+	E5-	M5+	M5-	L5+	L5-

**N** FREE PARAMETER  
**m**: fitted  
**n**: fixed  
**N-m-n**: randomly varying

MODEL DEPENDENT FIT  
**m=3**  
**n=N-3**  
**0** randomly varying

MODEL INDEPENDENT ANALYSIS  
**m=0**  
**n=0**  
**N**: randomly varying

# AMIAS: Sensitivity Analysis

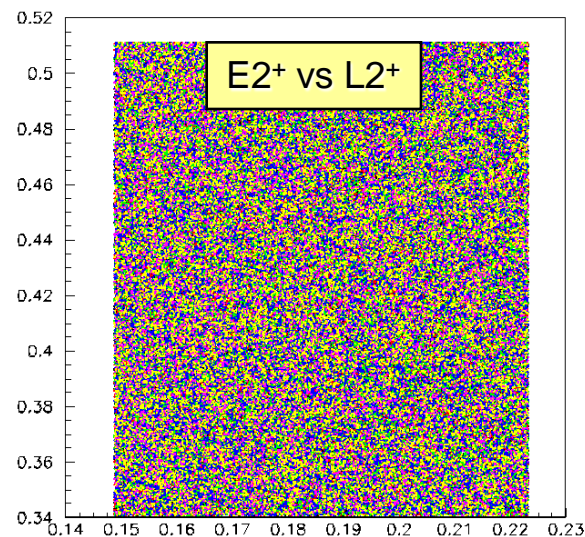
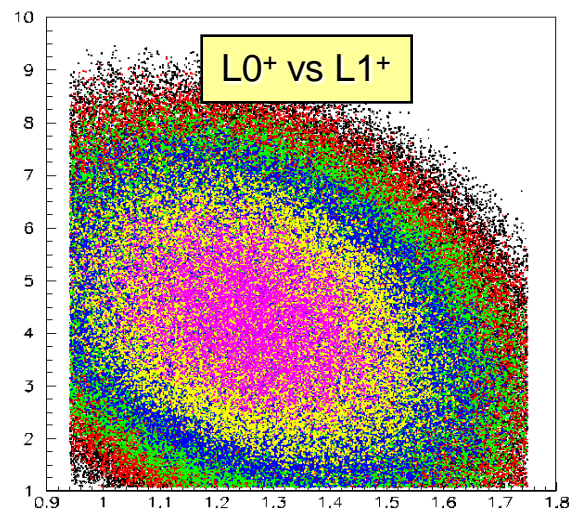


# Bates-Mainz Data ( $Q^2=0.127 \text{ (GeV/c)}^2$ , $W=1232 \text{ MeV}$ )

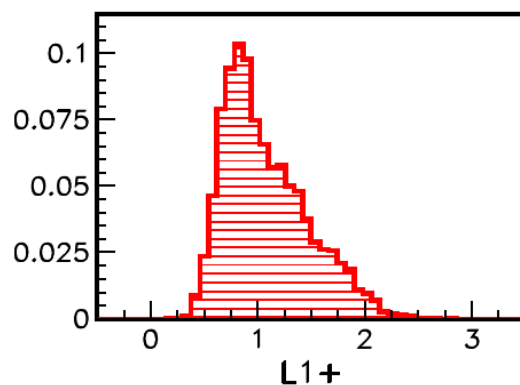
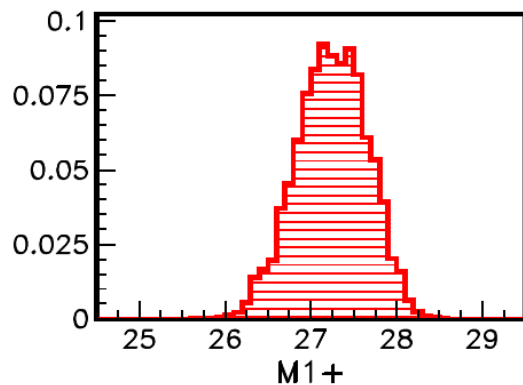
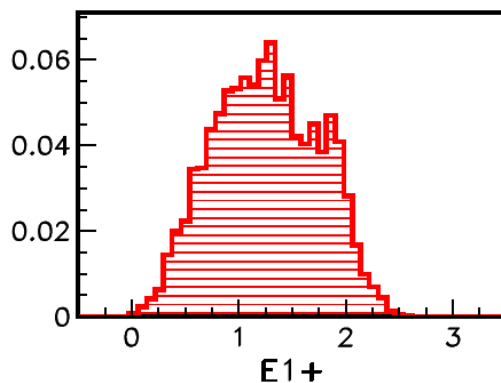
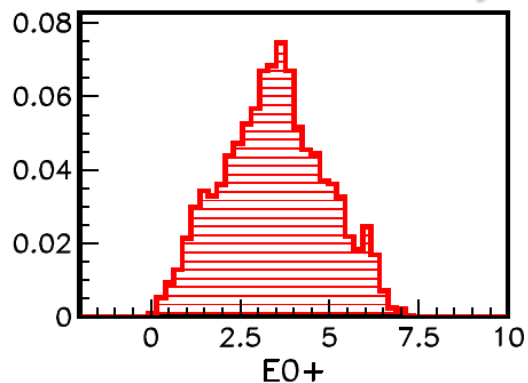
## Extracted Values

Multipole	Extracted Value	Relative Error	MAID-2003	Sato & Lee	DMT
$M_{1+}$	$27.24 \pm 0.20$	0.73 %	27.464	27.661	27.489
$L_{1+}$	$0.82^{+0.20}_{-0.09}$	17.7 %	1.000	0.672	0.986
$L_{0+}$	$2.23 \pm 0.41$	18.4 %	2.345	1.008	1.994
$E_{0+}$	$3.44 \pm 0.70$	20.3 %	2.873	2.213	3.206
$E_{1+}$	$1.16^{+0.32}_{-0.24}$	24.1 %	1.294	1.288	1.401

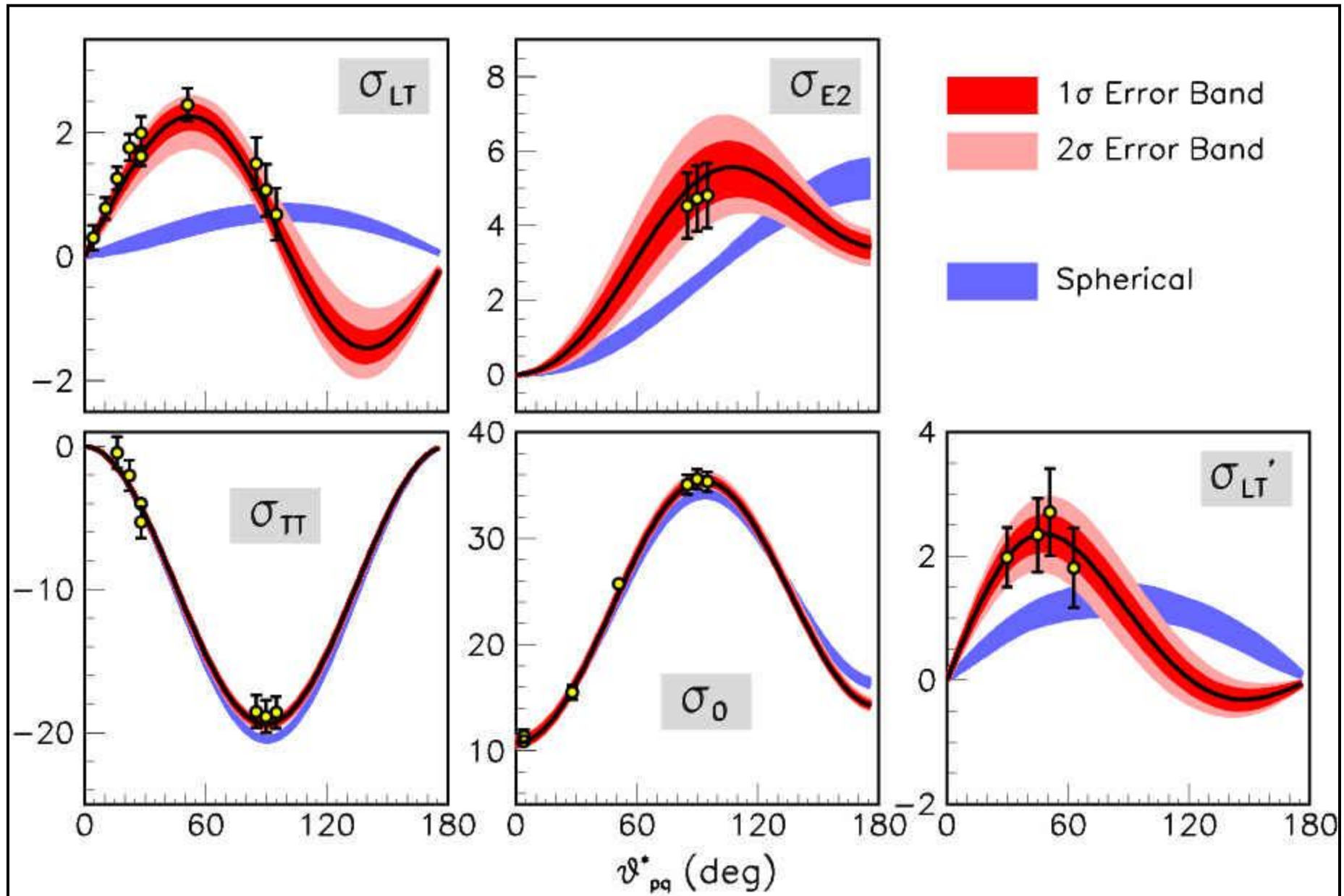
## Correlations



## Probability Distributions

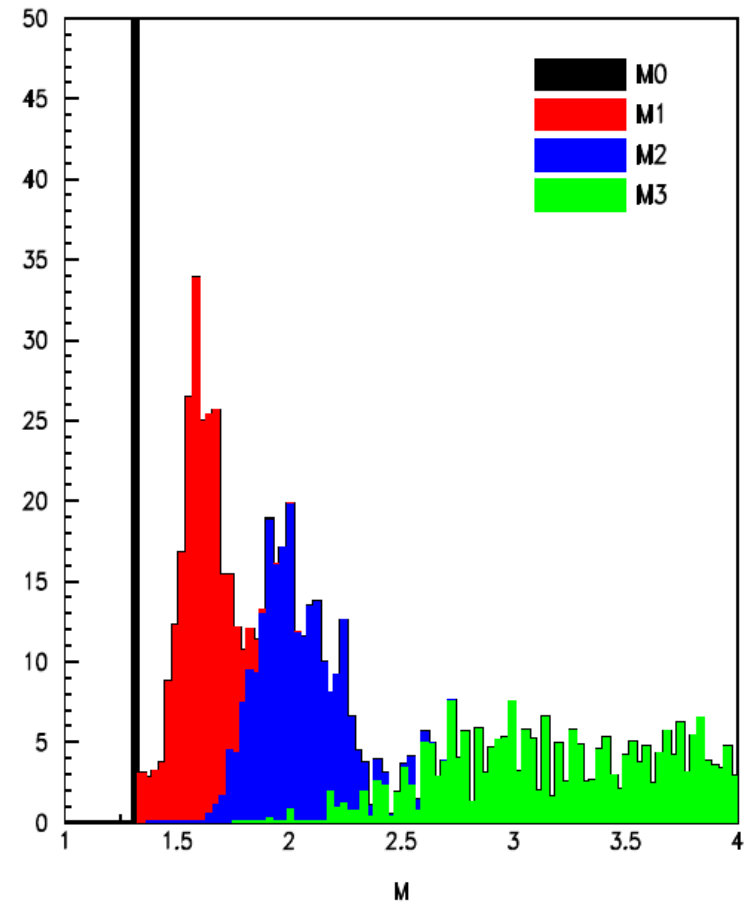
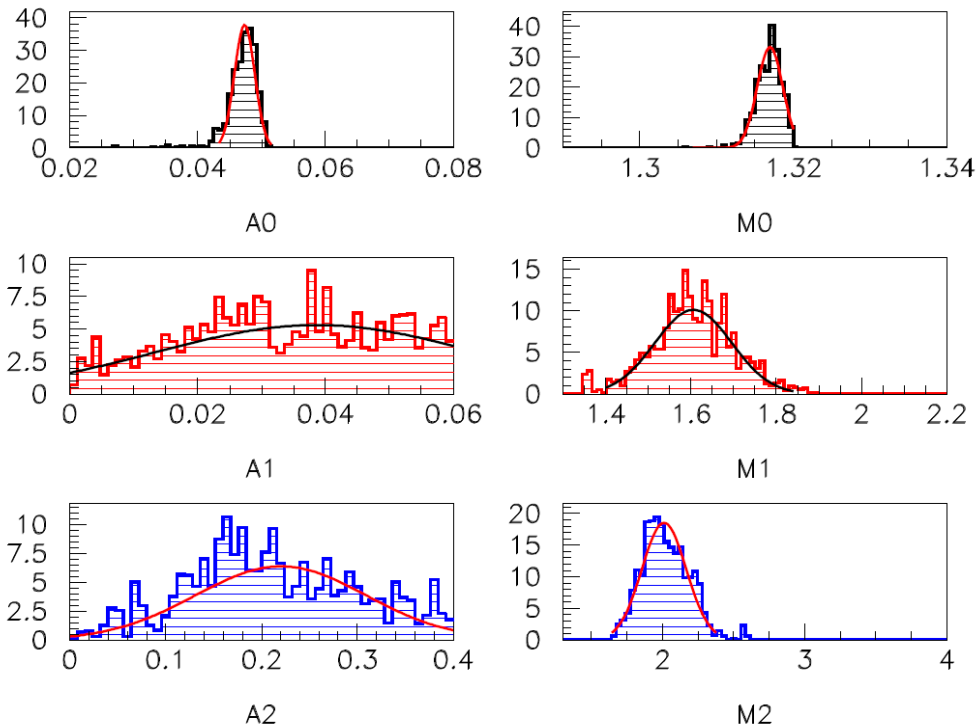


# Bates-Mainz Data ( $Q^2=0.127 \text{ (GeV/c)}^2$ , $W=1232 \text{ MeV}$ )



# AMIAS and Lattice QCD

AMIAS has been successfully tested in the determination of hadron excited states in Lattice QCD applied to the nucleon.



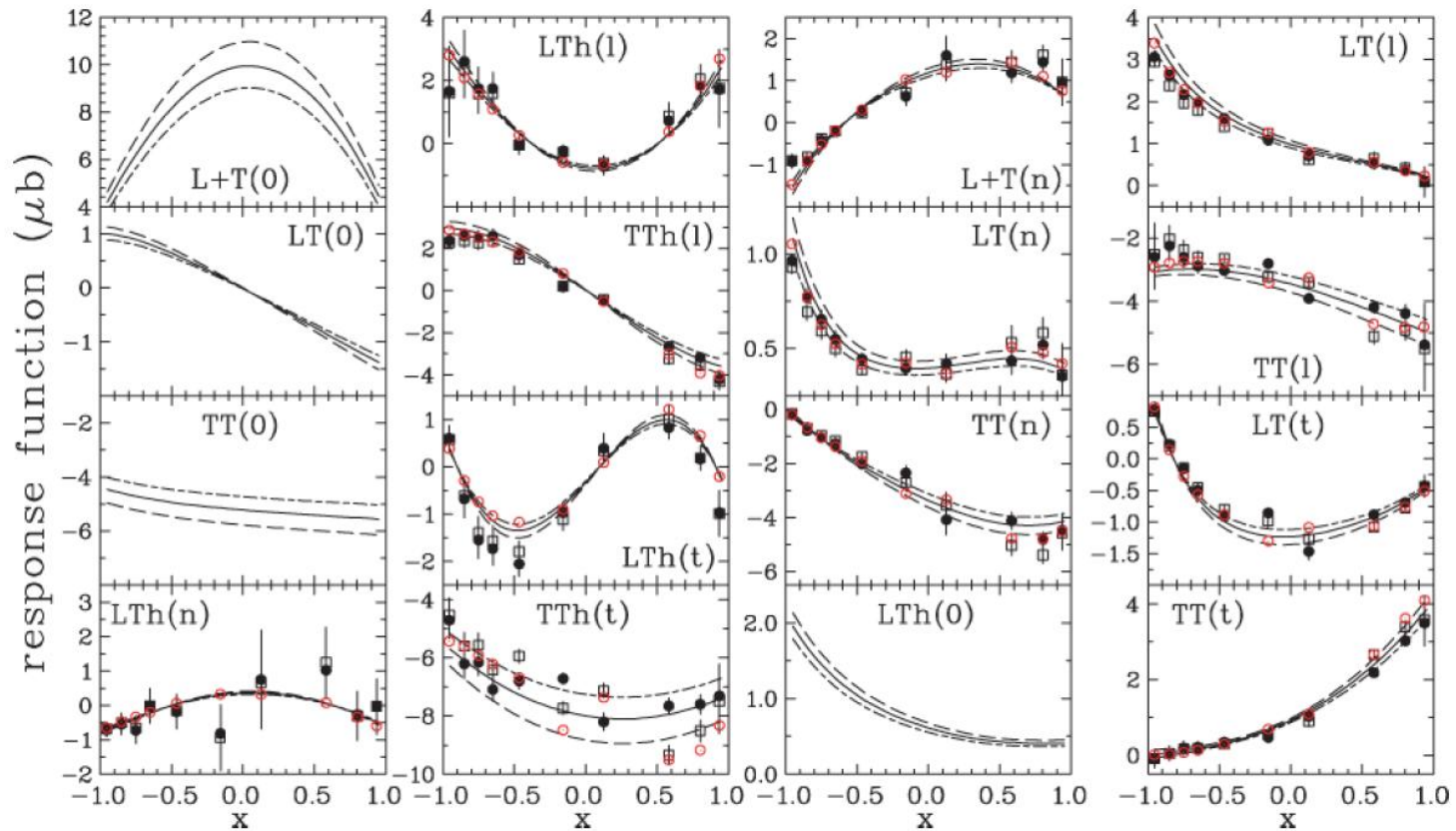
C. Alexandrou, C.N. Papanicolas and E. Stiliaris:  
*A novel fitting scheme – Nucleon excited states*  
PoS (Lattice 2008) 099



# Future Plans: Model Independent Analysis of JLab Data

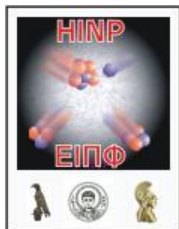
PHYSICAL REVIEW C **75**, 025201 (2007)

## Recoil polarization measurements for neutral pion electroproduction at $Q^2 = 1 \text{ (GeV}/c)^2$ near the $\Delta$ resonance





# Thank You!



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