

# MICROSCOPIC DESCRIPTION OF NEUTRON-INDUCED FISSION WITH THE CONSTRAINED MOLECULAR DYNAMICS (CoMD) MODEL: RECENT PROGRESS

**Sofia Papadimitriou, George A. Souliotis**

Physical Chemistry Laboratory,  
Department of Chemistry  
University of Athens, Athens, Greece

**Aldo Bonasera**

INFN, Catania, Italy,  
Texas A&M University, Texas, USA

**Martin Veselský**

IoP, Bratislava, Slovakia



ΕΘΝΙΚΟ ΚΑΙ  
ΚΑΠΟΔΙΣΤΡΙΑΚΟ  
ΠΑΝΕΠΙΣΤΗΜΙΟ  
ΑΘΗΝΩΝ

# OUTLINE

- Contemporary studies in nuclear fission
- Description of the theoretical model CoMD
- Theoretical results
- Summary and conclusions
- Future work plan



# CONTEMPORARY STUDIES IN NUCLEAR FISSION

## Proton induced fission theoretical studies

- [1] N. Vonta, G.A. Souliotis et al, *Phys. Rev. C* 92, 024616 (2015)
  - Study of the above reactions:  $p + {}^{232}\text{Th}$ ,  ${}^{235}\text{U}$ ,  ${}^{238}\text{U}$  with Code CoMD and comparison with experimental data
- [2] P. Demetriou et al *Phys. Rev. C* 82, 054606 (2010)
  - experimental and theoretical study of the above reactions:  $p + {}^{232}\text{Th}$ ,  ${}^{237}\text{Np}$ ,  ${}^{238}\text{Pu}$  and  ${}^{239}\text{Am}$
  - Comparison with Code Talys



## CONTEMPORARY STUDIES IN NUCLEAR FISSION

- **Neutron induced fission and theoretical studies**
- [3] R. Yanez, W. Loveland et al, arXiv: 1605.09690v2 [nucl-ex] (2016)
  - Total kinetic energy release in the fast neutron-induced fission of  $^{235}\text{U}$  for En 2-100 MeV
- [4] **The n\_TOF Collaboration (F. Belloni et al.): Eur. Phys. J. A (2011) 47:2**
  - neutron induced fission cross-section of  $^{235}\text{U}$  at the CERN n\_Tof facility relative to  $^{235}\text{U}$  between 0.5 and 20 MeV.



# DESCRIPTION OF THE THEORETICAL CoMD MODEL

## CoMD: Quantum Molecular Dynamics Model (Semiclassical)

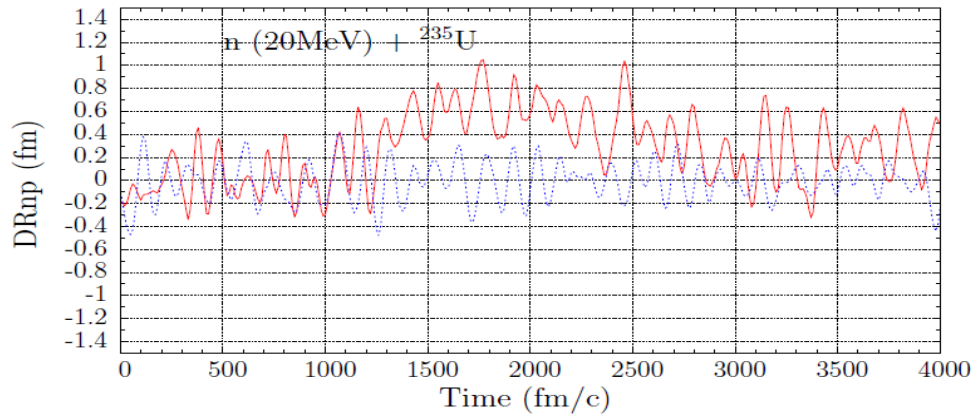
- ❑ The nucleons considered as gaussian wavepackets
- ❑ Phenomenological interaction N-N (effective interaction):  $V_{eff}$ 
$$V_{eff} = V_{vol} + V_{surf} + V_{Coul} + V_{sym}$$
- ❑ Symmetry potential N-N depending on the nuclear density
  - $V_{sym} \propto \rho$  (“standard”)
  - $V_{sym} \propto \sqrt{\rho}$  (“soft”)
- ❑ Application of Pauli Principle through appropriate restriction in the phase space
- ❑ Recognition of fragment formation ( $R_{N-N} < 3.0$  fm)
- ❑ Simulation of successive events (**Monte Carlo approach**)
- ❑ Maximum time  $t=15000$  fm/c
- ❑ Special choice of the surface term
  - Correct configuration of the ground state (Cs=-2) → NO FISSION
  - In order to get fission we set Cs=0



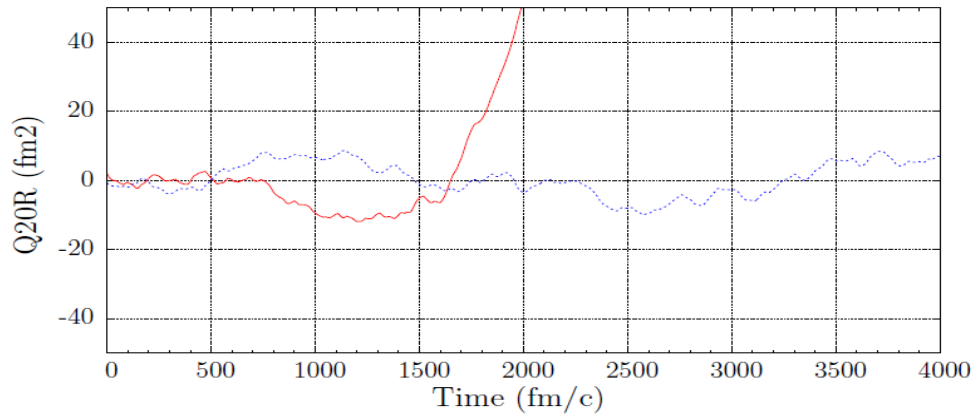
# DEPENDENCES

Blue line:  $C_s = -2$

Red line:  $C_s = 0$

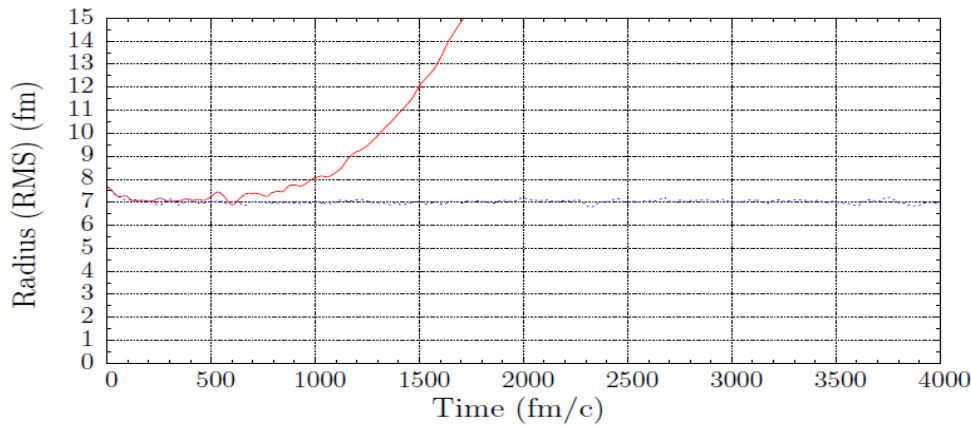


(a)  $\Delta z \rightarrow \text{GDR}$



(b)  $Q_{20} \rightarrow \text{GQR}$

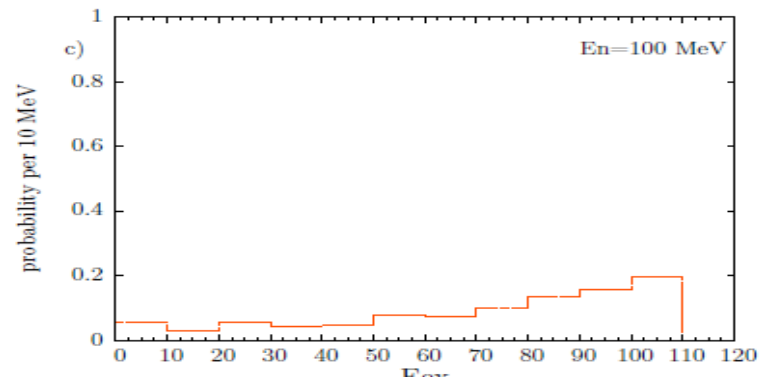
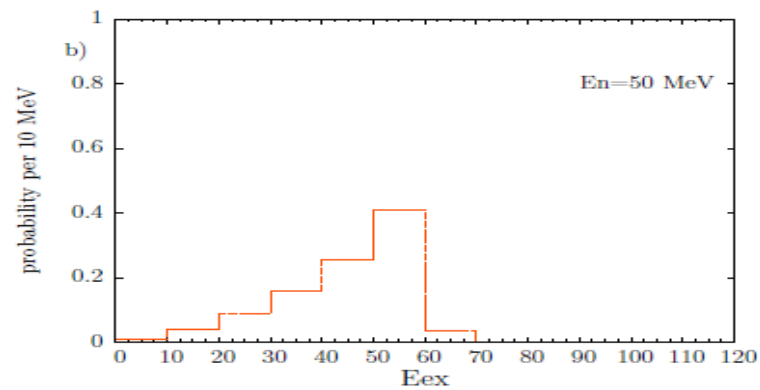
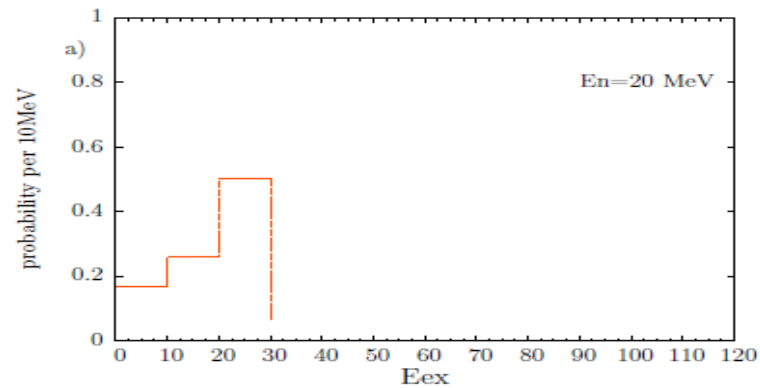
$$Q_{20} = 3z^2 - x^2 - y^2$$

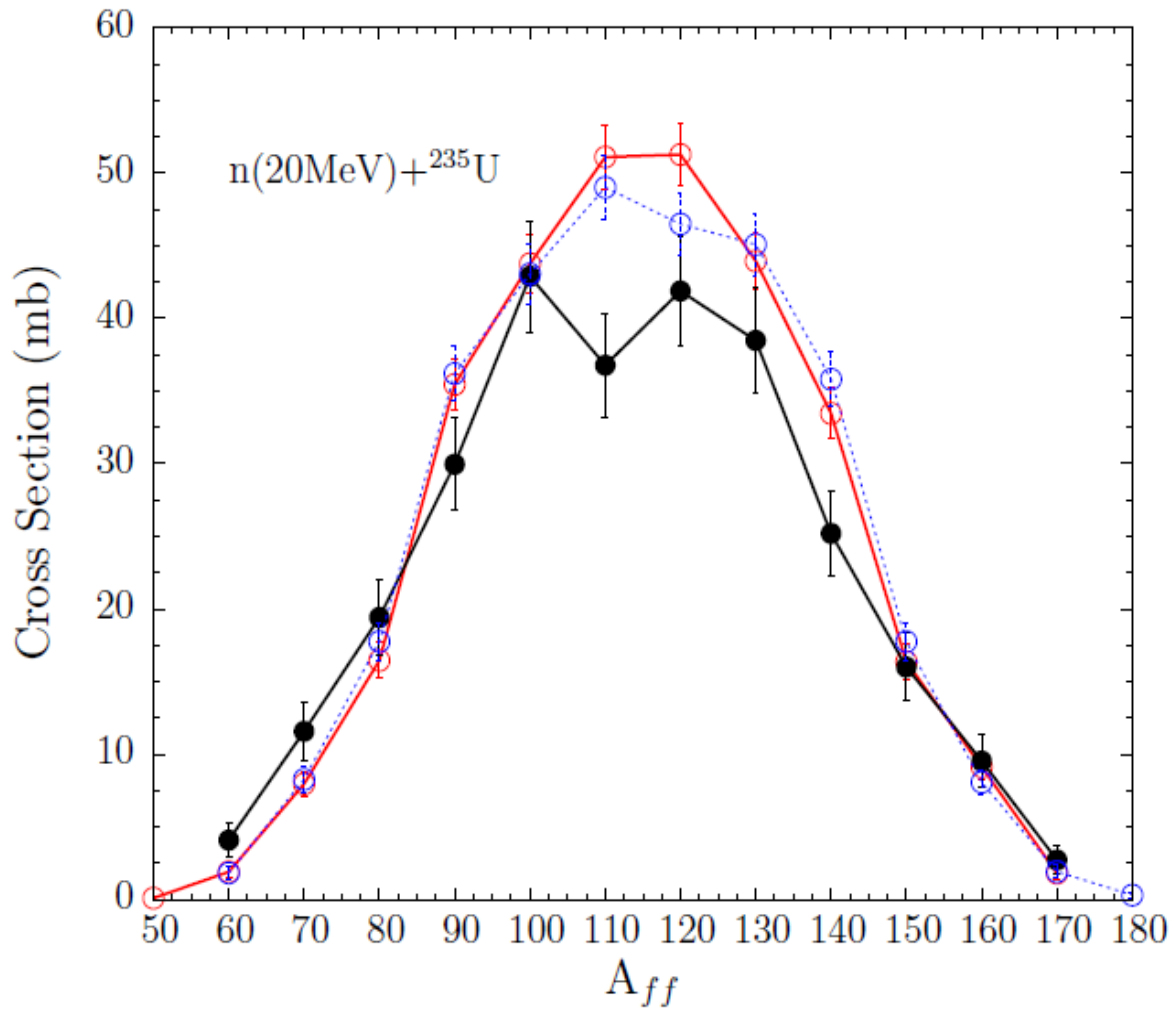


(c)  $R \rightarrow \text{GMR}$



# PRIMARY STAGE: EXCITATION ENERGY OF $^{236}\text{U}^*$





**YIELD CURVE: N(20MEV) + <sup>235</sup>U**

**Red line:  
standard**

**$V_{sym} \sim \rho, C_s=0$  \***

**Blue line: soft**

**$V_{sym} \sim \rho^{1/2},$   
 $C_s=0^*$**

**NEW  
APPROACH**

**Black line:  
standard**

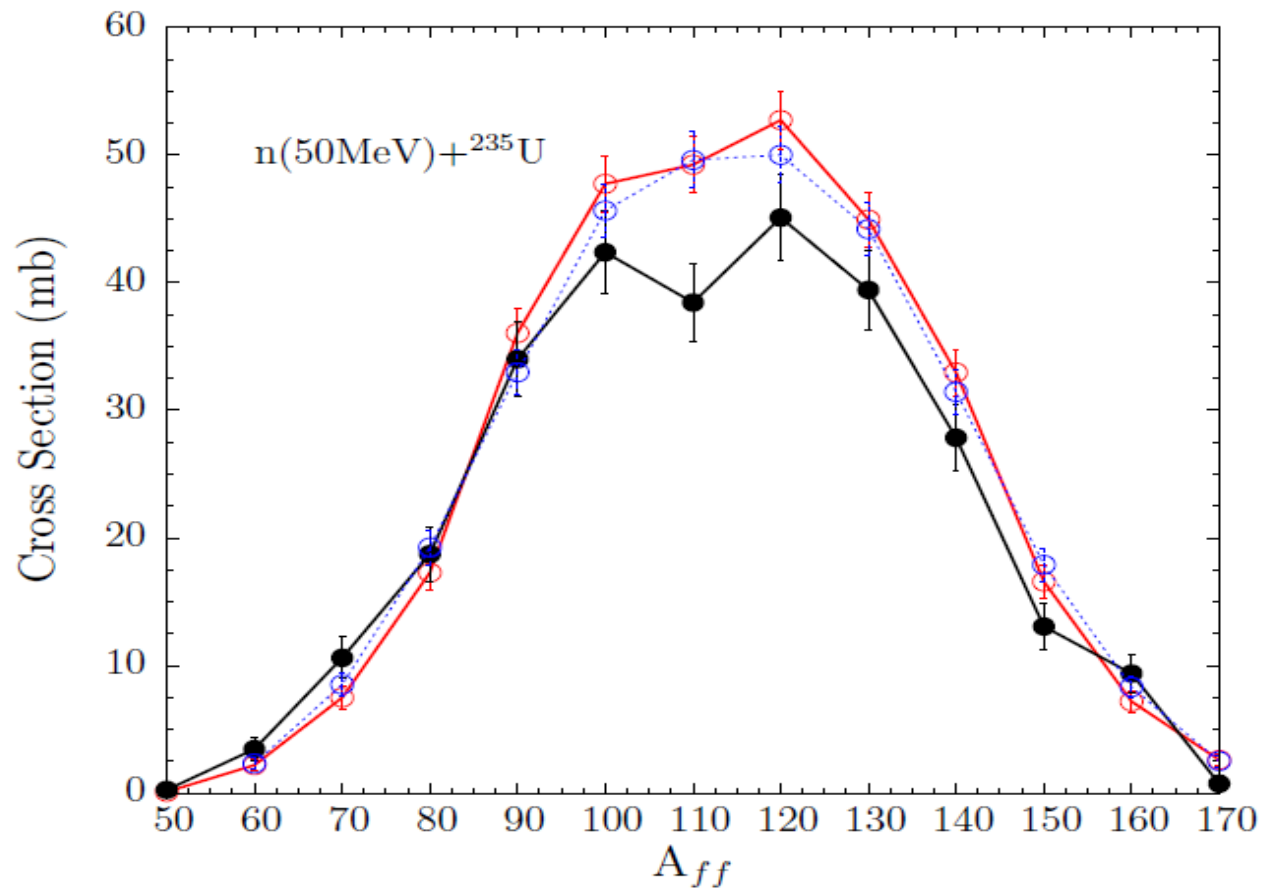
**$V_{sym} \sim \rho, C_s=f(t)$**

\*Method similar to N. Vonta, G.A. Souliotis et al, Phys. Rev. C92, 024616 (2015)





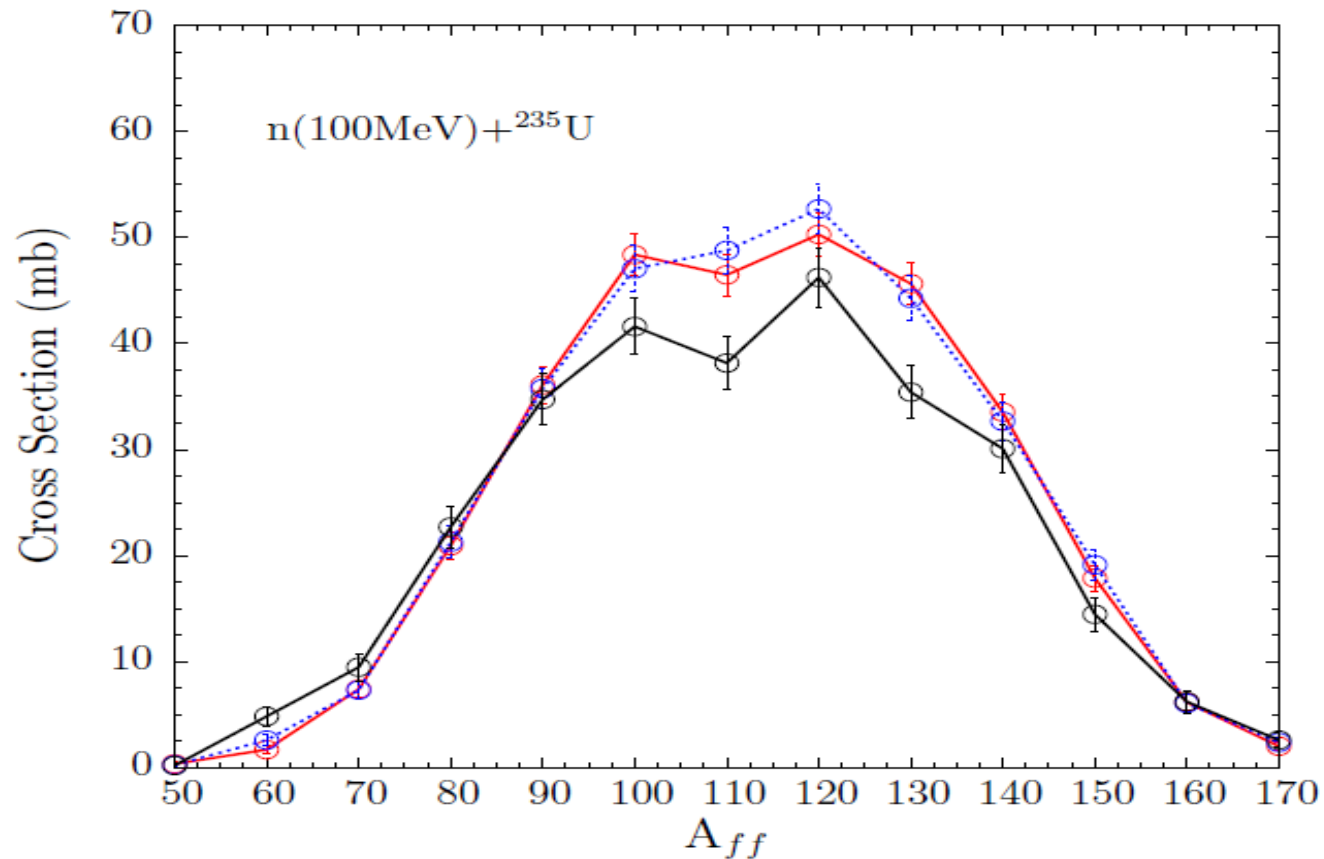
# Yield curve: $n(50\text{MeV}) + {}^{235}\text{U}$



**Red line: standard  $V_{\text{sym}} \sim \rho$ ,  $C_s=0$**   
**Blue line: soft  $V_{\text{sym}} \sim \rho^{1/2}$ ,  $C_s=0$**   
**Black line: standard  $V_{\text{sym}} \sim \rho$ ,  $C_s=f(t)$**



# YIELD CURVE: $n(100\text{MeV}) + {}^{235}\text{U}$

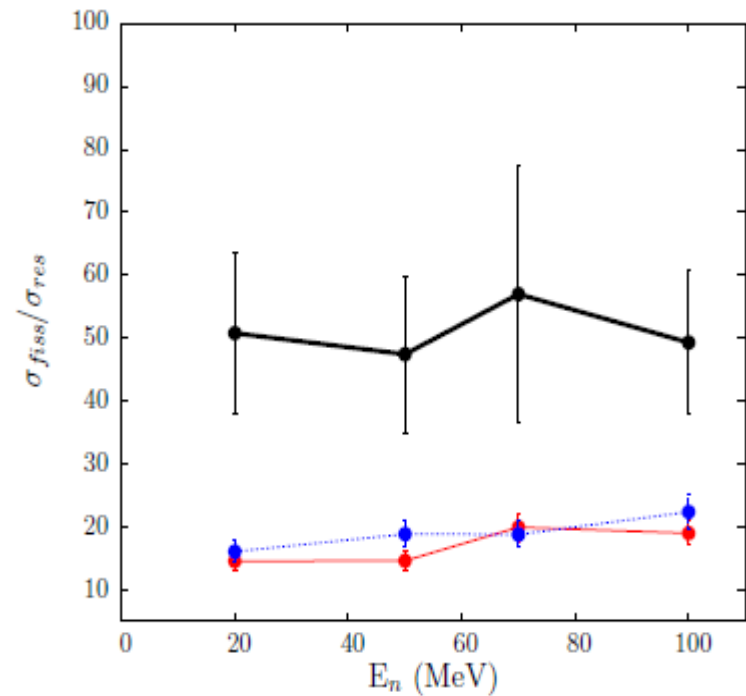
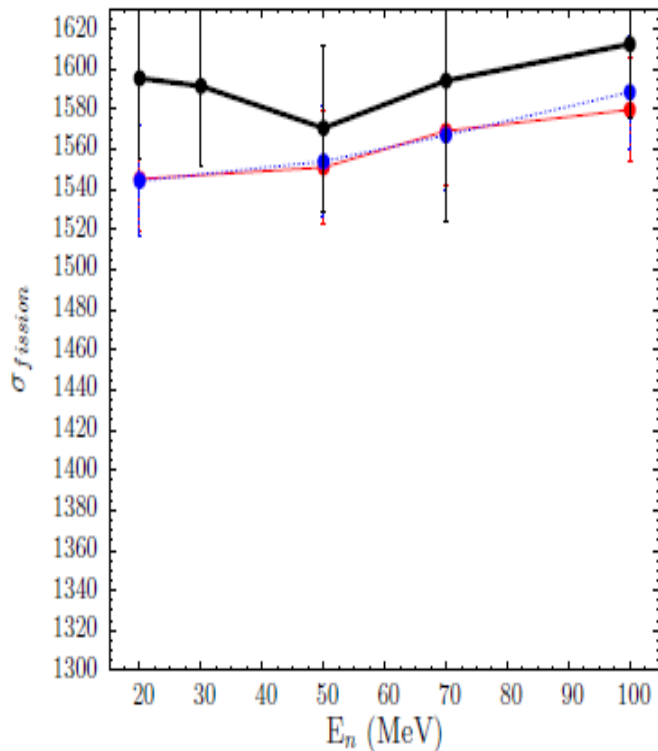


**Red line: standard  $V_{\text{sym}} \sim \rho$ ,  $C_s=0$**   
**Blue line: soft  $V_{\text{sym}} \sim \rho^{1/2}$ ,  $C_s=0$**   
**Black line: standard  $V_{\text{sym}} \sim \rho$ ,  $C_s=f(t)$**



## Total fission cross section

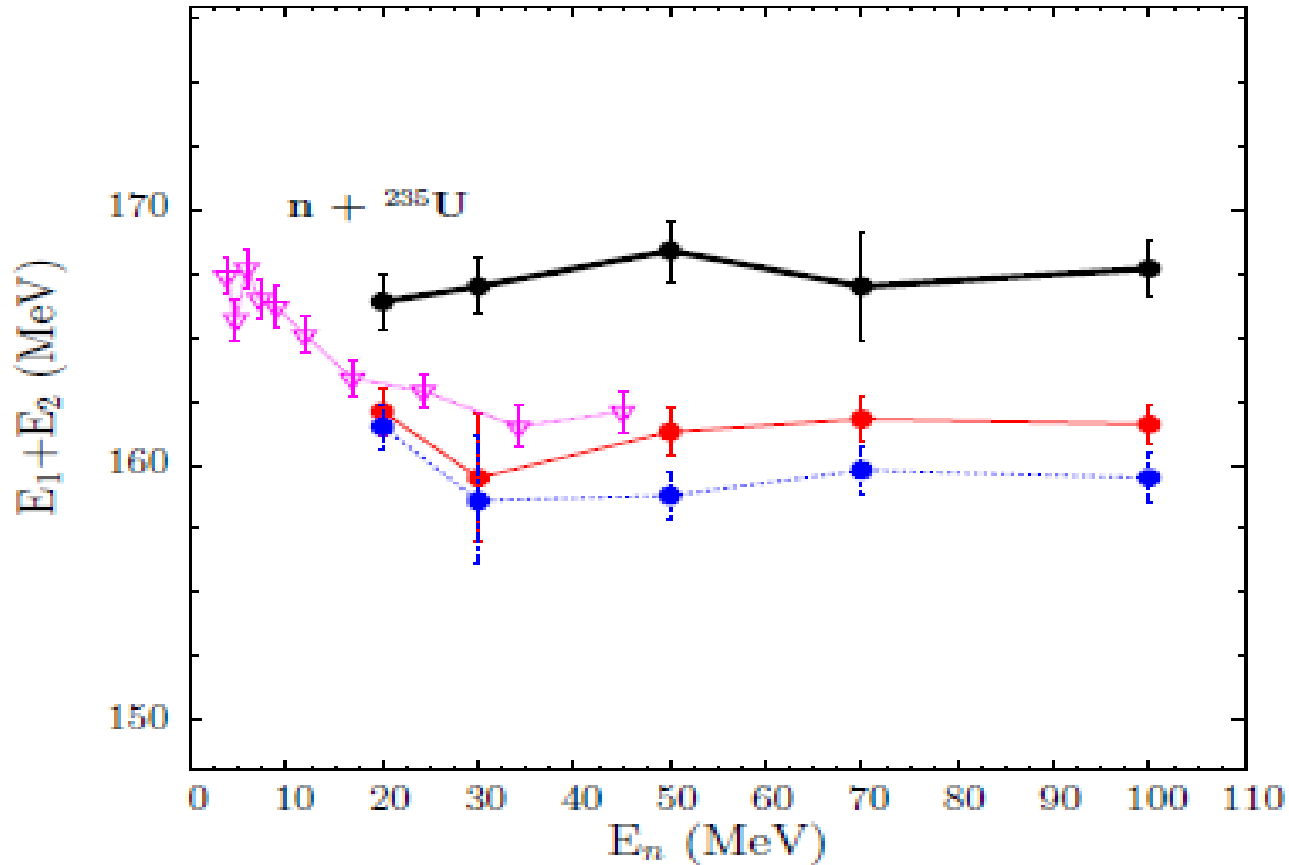
## Fission cross section/residue cross section



**Red line: standard  $V_{\text{sym}} \sim \rho$ ,  $C_s=0$**   
**Blue line: soft  $V_{\text{sym}} \sim \rho^{1/2}$ ,  $C_s=0$**   
**Black line: standard  $V_{\text{sym}} \sim \rho$ ,  $C_s=f(t)$**



# TOTAL KINETIC ENERGY OF THE FISSION FRAGMENTS



**Red line: standard  $V_{\text{sym}} \sim \rho, C_s=0$**

**Blue line: soft  $V_{\text{sym}} \sim \rho^{1/2}, C_s=0$**

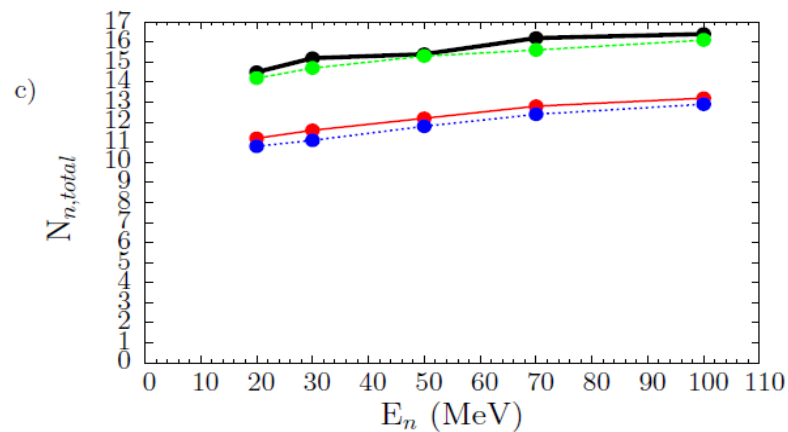
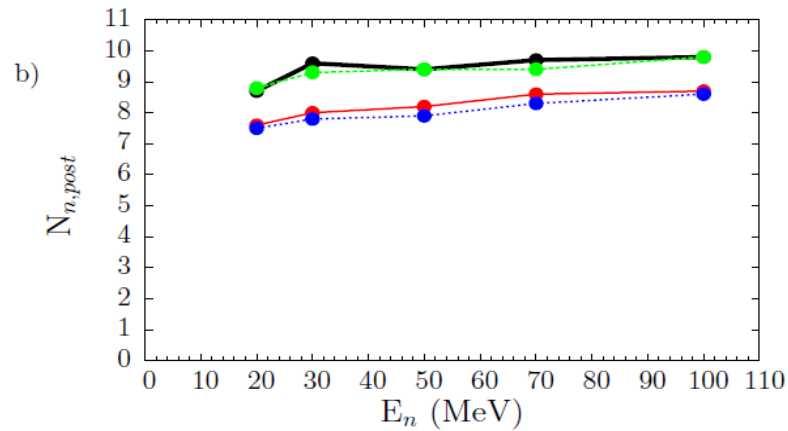
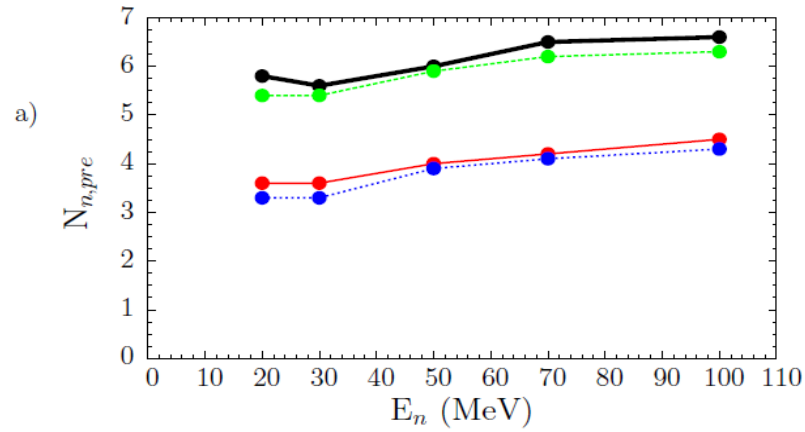
**Black line: standard  $V_{\text{sym}} \sim \rho, C_s=f(t)$**

**Pink line: experimental data**

[3]R. Yanez, W. Loveland et al, arXiv: 1605.09690v2 [nucl-ex] (2016)



# NEUTRON MULTIPLICITY



**Red line:**  
standard  $V_{\text{sym}} \sim \rho$   
( $C_s=0$ )

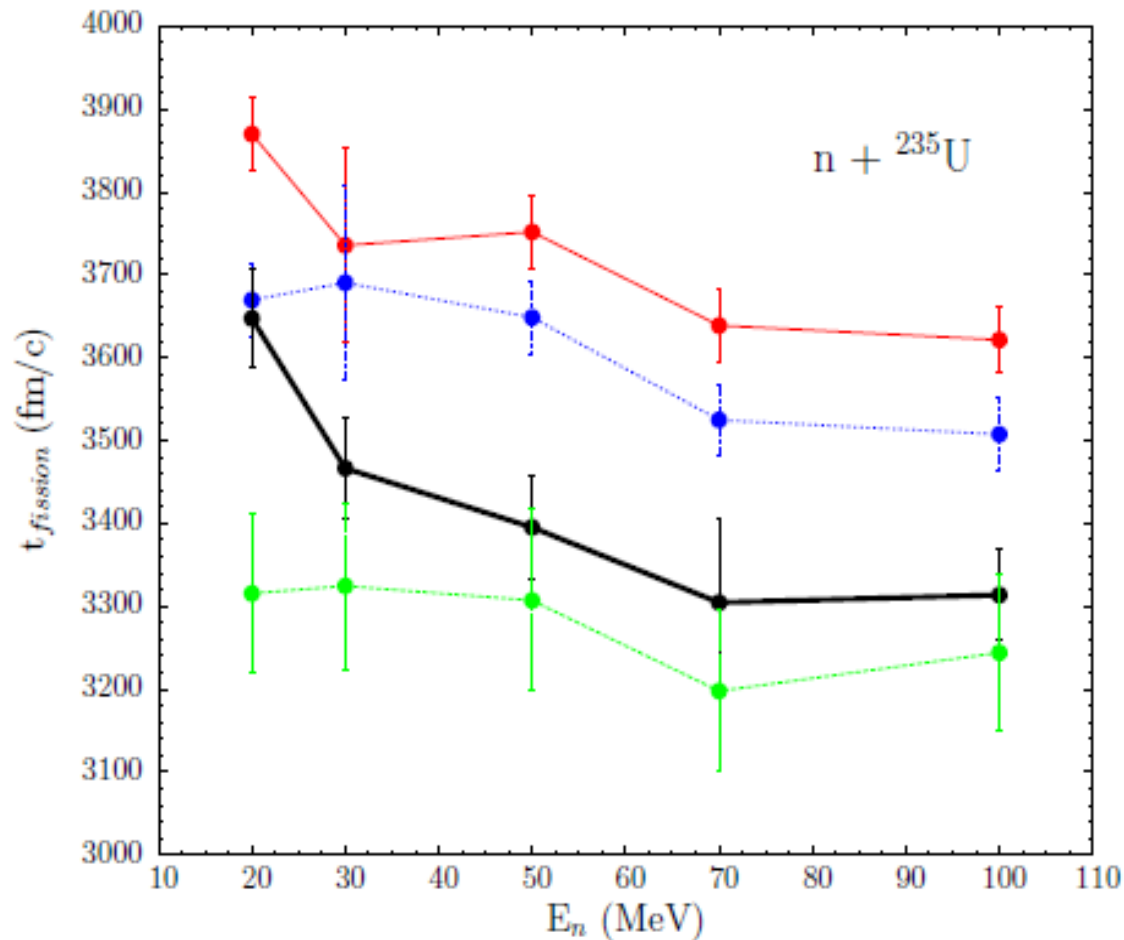
**Blue line:** soft  
 $V_{\text{sym}} \sim \rho^{1/2}$   
( $C_s=0$ )

**Black line:**  
standard  
 $V_{\text{sym}} \sim \rho$   
( $C_s=f(t)$ )

**Green line:**  
 $V_{\text{sym}} \sim \rho^{1/2}$   
( $C_s=f(t)$ )



# TIME OF FISSION PROCESS



← Old approach

← New approach

**Red line: standard  $V_{sym} \sim \rho, C_s=0$**   
**Blue line: soft  $V_{sym} \sim \rho^{1/2}, C_s=0$**   
**Black line: standard  $V_{sym} \sim \rho, C_s=f(t)$**   
**Green line:  $V_{sym} \sim \rho^{1/2}, C_s=f(t)$**



# SUMMARY AND CONCLUSIONS

- **Microscopic dynamical calculations of low energy fission induced by neutrons**
- **Careful treatment of the surface term and energy correction**
- **Our recent calculations point to asymmetric fission as known from experiment**
- **Collective dynamics of the fission process is described “adequately”**
- **Meaningful fission –time information**



# FUTURE WORK PLAN

- **Systematic study of fission observables**
  - ✓ **mass yield curves**
  - ✓ **Energy distributions**
  - ✓ **Fission time scale**
  - ✓ **Pre-fission and post fission neutron emission**
- **Inclusion of the shell effects in the model (spin-orbit term in the potential)**
- **Possible experimental work in Catania with MAGNEX using  $^{238}\text{U}$  on light targets (inverse kinematics)**





**THANK YOU!**

