

HESS J1731-347 and the existence of exotic matter

Kaon condensation in neutron stars

P.S. Koliogiannis¹, V. Petousis², M. Veselský² and Ch.C. Moustakidis¹

¹Department of Theoretical Physics, Aristotle University of Thessaloniki

²Institute of Experimental and Applied Physics, Czech Technical University

May 31, 2024 - June 01, 2024, University of Ioannina
7th International Workshop of Hellenic Institute of Nuclear Physics



ARISTOTLE
UNIVERSITY
OF THESSALONIKI

Table of Contents

- 1 Exotic Phases
 - Meson condensates
- 2 Kaon condensation
 - Interactions
 - Equilibrium conditions
- 3 Numerical results
 - Equations of state - Parameters
 - Pressure - Energy density relation
 - Second \rightarrow First order phase transition
 - Particle Fractions
 - Speed of sound
 - Mass-radius diagram and the HESS J1731-134
- 4 Concluding remarks - Pending work

Exotic Phases

- Strong interactions \rightarrow Meson condensates
- Quark structure of baryons \rightarrow Deconfinement of quarks
- Mixed-phase

Meson condensates

- Particles to be considered for meson condensate → Pions and **Kaons**

► Pions

- Lightest mesons
- $e^- \rightarrow p^-$
- $n \geq n_0$
- Soften the EoS

► Kaons

- Lightest strange mesons
- Large mass → Condensation?
- $n \geq 3n_0$
- Strong softening on the EoS

Meson condensates

- Particles to be considered for meson condensate → Pions and **Kaons**

► Pions

- Lightest mesons
- $e^- \rightarrow p^-$
- $n \geq n_0$
- Soften the EoS

► Kaons

- Lightest strange mesons
- Large mass → Condensation?
- $n \geq 3n_0$
- Strong softening on the EoS

Kaons - HESS J1731-347

Strong softening on the EoS → HESS J1731-347

$$M = 0.77^{+0.20}_{-0.17} M_{\odot} \text{ and } R = 10.4^{+0.86}_{-0.78} \text{ km}$$

Interactions

Chiral Lagrange density

$$\begin{aligned}
 \mathcal{L} = & \frac{1}{4}f^2\text{Tr}\partial_\mu U\partial^\mu U^\dagger + c\text{Tr}\left(m_q\left(U + U^\dagger - 2\right)\right) + \text{Tr}\bar{B}\gamma^\mu i\partial_\mu B + i\text{Tr}B^\dagger[V_0, B] \\
 & - D\text{Tr}B^\dagger\sigma\{A, B\} - F\text{Tr}B^\dagger\sigma[A, B] + a_1\text{Tr}B^\dagger(\xi m_q\xi + \text{h.c.})B \\
 & + a_2\text{Tr}B^\dagger B(\xi m_q\xi + \text{h.c.}) + a_3\text{Tr}B^\dagger B\text{Tr}(m_q U + \text{h.c.}) + \mathcal{L}_e + \mathcal{L}_\mu
 \end{aligned} \tag{1}$$

where the non-linear sigma field U and the ξ field are given by

$$U = \exp\sqrt{2}iM/f, \quad \xi^2 = U \tag{2}$$

and the mesonic vector and axial vector currents by

$$V_\mu = \frac{1}{2}\left(\xi^\dagger\partial_\mu\xi + \xi\partial_\mu\xi^\dagger\right), \quad A_\mu = \frac{1}{2}i\left(\xi^\dagger\partial_\mu\xi - \xi\partial_\mu\xi^\dagger\right) \tag{3}$$

Meson octet

Baryon octet

Quark mass

$$M = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\sqrt{\frac{2}{3}}\eta \end{pmatrix} \quad B = \begin{pmatrix} \frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & \Sigma^+ & p \\ \Sigma^- & -\frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & n \\ \Xi^- & \Xi^0 & -\sqrt{\frac{2}{3}}\Lambda \end{pmatrix} \quad m_q = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & m_s \end{pmatrix}$$

Interactions

Constants of hadronic interaction terms

$$m_{\Sigma} - m_N = 2a_2 m_s,$$

$$m_{\Lambda} - m_N = \frac{2}{3} (a_2 - 2a_1) m_s,$$

$$m_{\Xi} - m_N = 2(a_2 - a_1) m_s$$



$$\begin{cases} a_1 m_s = -67 \text{ MeV} \\ a_2 m_s = 134 \text{ MeV} \end{cases}$$

Interactions

Constants of hadronic interaction terms

$$m_{\Sigma} - m_N = 2a_2 m_s,$$

$$m_{\Lambda} - m_N = \frac{2}{3} (a_2 - 2a_1) m_s,$$

$$m_{\Xi} - m_N = 2(a_2 - a_1) m_s$$



$$\begin{cases} a_1 m_s = -67 \text{ MeV} \\ a_2 m_s = 134 \text{ MeV} \end{cases}$$

$a_3 m_s?$

Interactions

Constants of hadronic interaction terms

$$m_{\Sigma} - m_N = 2a_2 m_s,$$

$$m_{\Lambda} - m_N = \frac{2}{3} (a_2 - 2a_1) m_s,$$

$$m_{\Xi} - m_N = 2(a_2 - a_1) m_s$$



$$\begin{cases} a_1 m_s = -67 \text{ MeV} \\ a_2 m_s = 134 \text{ MeV} \end{cases}$$

$a_3 m_s?$

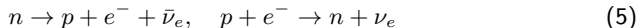


strangeness content of the proton + kaon-nucleon sigma term

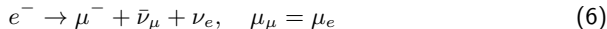
$$a_3 m_s = [-134, -310] \text{ MeV}, \quad \Sigma^{\text{KN}} = [168, 520] \text{ MeV} \quad (4)$$

Equilibrium conditions

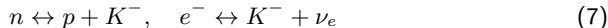
- β -decay and inverse β -decay



- Cold matter: Neutrinos leave the system $\Rightarrow \mu_n - \mu_p = \mu_e$
- Energetically favorable for electrons to convert to muons



- Strangeness changing processes



- Chemical equilibrium

$$\mu_n - \mu_p = \mu, \quad \mu_e = \mu \quad (8)$$

Equilibrium conditions

Fixed baryon number state (**including** nuclear interactions)

$$\begin{aligned}
 \tilde{\varepsilon}(u, x, \mu, \theta) &= \varepsilon_{\text{MDI}}(u, x) + un_0(1 - 2x^2)S(u) \\
 &- f^2 \frac{\mu^2}{2} \sin^2 \theta + 2m_K^2 f^2 \sin^2 \frac{\theta}{2} \\
 &+ \mu un_0 x - \mu un_0 (1 + x) \sin^2 \frac{\theta}{2} \\
 &+ (2a_1 x + 2a_2 + 4a_3) m_s un_0 \sin^2 \frac{\theta}{2} \\
 &+ \tilde{\varepsilon}_e + \eta(|\mu| - m_\mu) \tilde{\varepsilon}_\mu
 \end{aligned} \tag{9}$$

where the symmetry energy is given by

$$S(u) = \varepsilon_{\text{MDI}}(u, x = 0) - \varepsilon_{\text{MDI}}(u, x = 1/2) \tag{10}$$

Why the MDI?

- reproduces with high accuracy the properties of symmetric nuclear matter
- reproduces correctly the microscopic calculations of the Chiral model and the results of state-of-the-art calculations of Akmal et al¹
- predicts M_{max} at least higher than the observed ones

¹ A. Akmal, V. R. Pandharipande, and D. G. Ravenhall, Phys. Rev. C **58**, 1804 (1998).

Thermodynamics of the system

Energy density of the ground state

$$\frac{\partial \tilde{\varepsilon}}{\partial x} = 0, \quad \frac{\partial \tilde{\varepsilon}}{\partial \mu} = 0, \quad \frac{\partial \tilde{\varepsilon}}{\partial \theta} = 0 \quad (11)$$



$$\mu = 4(1 - 2x)S(u) \sec^2 \frac{\theta}{2} - 2a_1 m_s \tan^2 \frac{\theta}{2} \quad (12)$$

$$f^2 \mu \sin^2 \theta + un_0(1 + x) \sin^2 \frac{\theta}{2} - xun_0 + \frac{\mu^3}{3\pi^2} + \eta(|\mu| - m_\mu) \frac{(\mu^2 - m_\mu^2)^{3/2}}{3\pi^2} = 0 \quad (13)$$

$$\theta = \cos^{-1} \left[\frac{1}{\mu^2} \left(m_K^2 - \frac{\mu}{2f^2} un_0(1 + x) + \frac{un_0}{2f^2} (2a_1x + 2a_2 + 4a_3)m_s \right) \right] \quad (14)$$

Energy density and Pressure

The energy density and pressure of the model are calculated as

$$\begin{aligned}
 \varepsilon(u, x, \mu, \theta) &= \varepsilon_{\text{MDI}}(u, x) + un_0(1 - 2x^2)S(u) \\
 &+ f^2 \frac{\mu^2}{2} \sin^2 \theta + 2m_K^2 f^2 \sin^2 \frac{\theta}{2} \\
 &+ (2a_1 x + 2a_2 + 4a_3) m_s un_0 \sin^2 \frac{\theta}{2} \\
 &+ \varepsilon_e + \eta(|\mu| - m_\mu) \varepsilon_\mu
 \end{aligned} \tag{15}$$

$$P(u, x, \mu, \theta) = P_b(u, x, \mu) + P_K(u, x, \mu, \theta) + \sum_l P_l(u, x, \mu), \tag{16}$$

where

$$P_b(u, x, \mu) = u^2 \frac{\partial}{\partial u} \left(\frac{\varepsilon(u, x, \mu)}{u} \right) \tag{17}$$

Equations of state - Parameters

► Slope parameter

- $L = 3n_0 \left. \frac{dS(n)}{dn} \right|_{n_0}$

► Incompressibility

- $K = 9n_0^2 \left. \frac{d^2\varepsilon(n,0)}{dn^2} \right|_{n_0}$

strangeness of the proton

$$a_3 m_s = -134, -222, -310 \text{ MeV} \rightarrow \text{no strangeness, 10\%, 20\%}$$

Equations of state - Parameters

► Slope parameter

$$\bullet L = 3n_0 \left. \frac{dS(n)}{dn} \right|_{n_0}$$

► Incompressibility

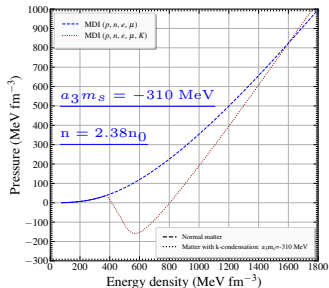
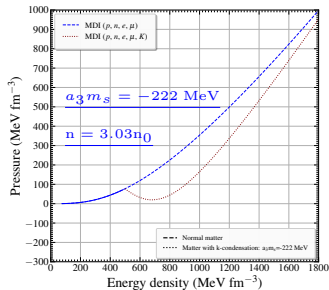
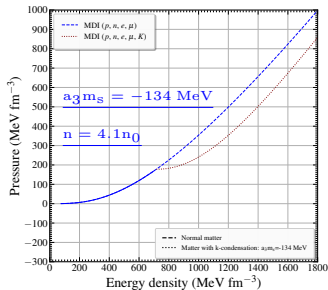
$$\bullet K = 9n_0^2 \left. \frac{d^2\varepsilon(n,0)}{dn^2} \right|_{n_0}$$

strangeness of the proton

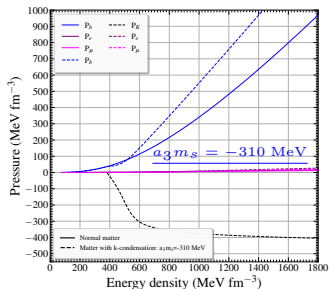
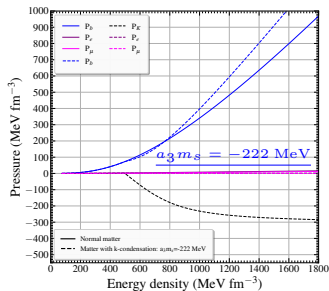
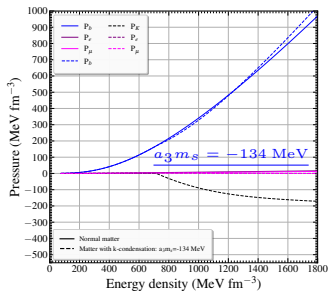
$$a_3 m_s = -134, -222, -310 \text{ MeV} \rightarrow \text{no strangeness, 10\%, 20\%}$$

- EoSs based on various slope parameters, incompressibilities and symmetry energies in the ranges [70, 90] MeV, [200, 260] MeV, and [30 – 34] MeV, respectively.
- Presented case: $L = 80$ MeV, $K_0 = 240$ MeV, and $S_0 = 32$ MeV.

Pressure - Energy relation

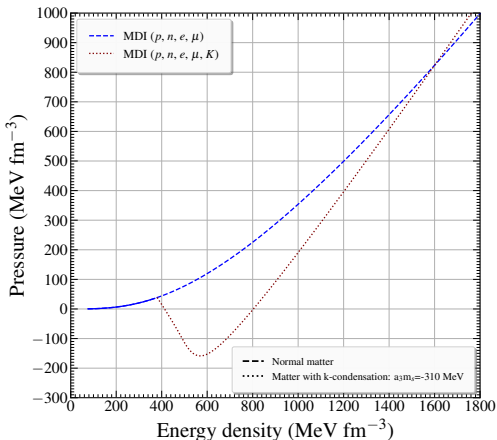


Pressure contribution



Second \rightarrow First order phase transition

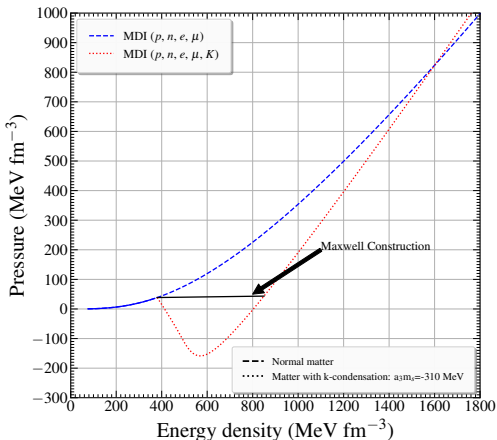
$$\blacktriangleright a_3 m_s = -310 \text{ MeV}, \quad n = 2.38 n_0$$



- Second order phase transition
- Compressibility at threshold is negative
- Maxwell construction \rightarrow positive compressibility

Second \rightarrow First order phase transition

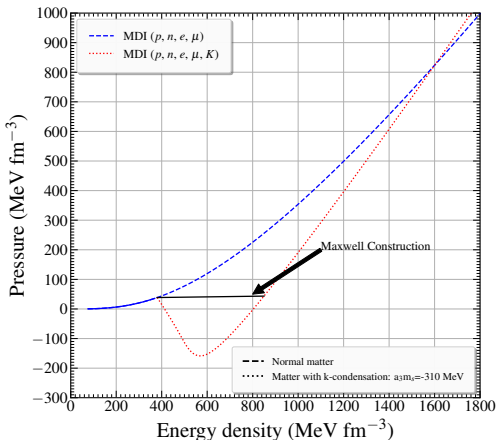
$$\blacktriangleright a_3 m_s = -310 \text{ MeV}, \quad n = 2.38 n_0$$



- Second order phase transition
- Compressibility at threshold is negative
- Maxwell construction \rightarrow positive compressibility

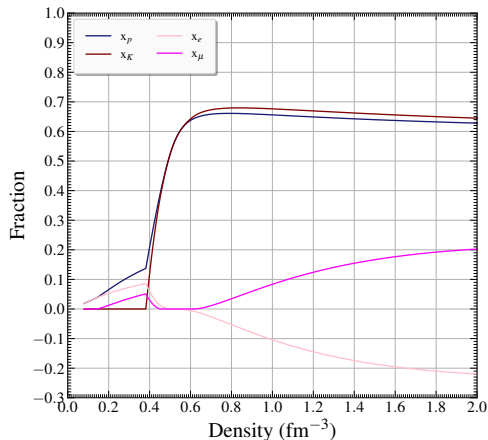
Second \rightarrow First order phase transition

$$\blacktriangleright a_3 m_s = -310 \text{ MeV}, \quad n = 2.38 n_0$$



- Second order phase transition
- Compressibility at threshold is negative
- **Maxwell construction \rightarrow positive compressibility**
- $\Delta \mathcal{E} \simeq 400 \text{ MeV fm}^{-3} \rightarrow$ Twin stars

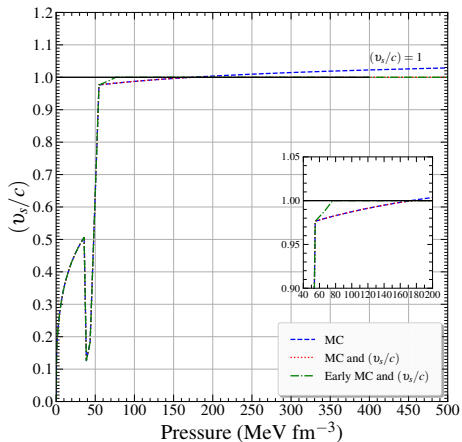
Particle Fractions



- Large x_p is required in presence of a x_k
- Net negative charge in kaon fields causes the lepton concentrations to decrease
- Existence of a density where leptons start producing \rightarrow production of positrons

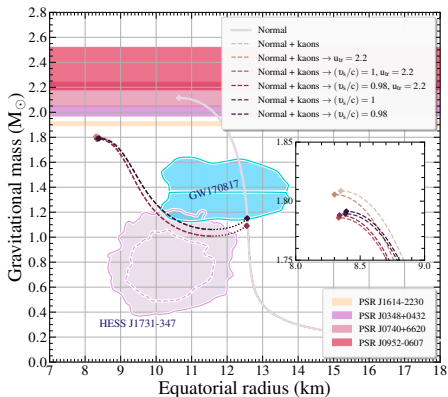
Speed of sound

- Speed of sound must be causal up to densities that correspond to M_{\max}



- ✓ MC to fix the gap
- ✓ MC to fix the gap and the speed of sound
- ✓ Early MC to fix the gap and the speed of sound

Mass-radius diagram and the HESS J1731-134



- ✓ Strong softening on the EoS $\rightarrow M_{\max} = 2.1 M_{\odot}$ to $M_{\max} = 1.8 M_{\odot}$
- ✓ The 2 approximations have insignificant effect on the M_{\max}
- ✓ Transition density is related to the boundaries of the HESS J1731-347
- ✓ M_{\max} constraints are not fulfilled

Concluding remarks - Pending work

- The strangeness of the proton plays critical role in the location of the transition density
- Transition density is directly related to the region of HESS J1731-347
- kaon condensation can be an explanation of the HESS J1731-347
- Constraints for the M_{\max} are not fulfilled

Future work

- Gibbs construction
- Hadronic EoS with $M_{\max} \sim 2.4 M_{\odot}$
- Relativistic Mean Field model

THANK YOU FOR YOUR ATTENTION!

The project is supported by the Special Account for Research Funds (ELKE) of the Aristotle University of Thessaloniki in the framework of the Research Fellowships for Postdoctoral Researchers (Fellowship Project: 50186, Fellowship Number: 673402)