



# Reactions of weakly-bound nuclei at near-barrier energies

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# Contents

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## 1. OMPs of weakly-bound nuclear systems

${}^6\text{He}+{}^{209}\text{Bi}$ ,  ${}^6\text{Li}+{}^{208}\text{Pb}$

## 2. Breakups of weakly-bound nuclei

- stable nuclei:  ${}^{6,7}\text{Li}+{}^{209}\text{Bi}$

- proton-rich nuclei:  ${}^{17}\text{F}+{}^{58}\text{Ni}$ ,  ${}^8\text{B}+{}^{120}\text{Sn}$

## 3. Summary and outlook

# Optical Model Potential

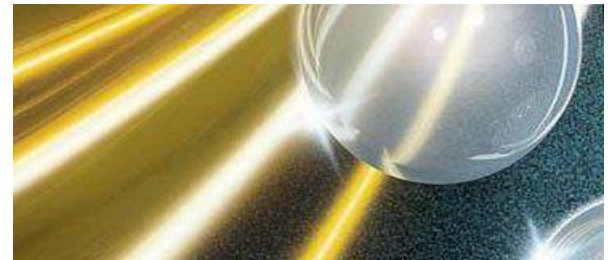
- ♠ Optical Model is a successful model to explain the nuclear scattering and reaction, which resembles the case of light scattered by an opaque glass sphere.

## Optical Model Potential (OMP):

$$U = V(r) + iW(r)$$

↙  
**attractive**

↘  
**absorptive**



★ phenomenological potential, independent on energy.

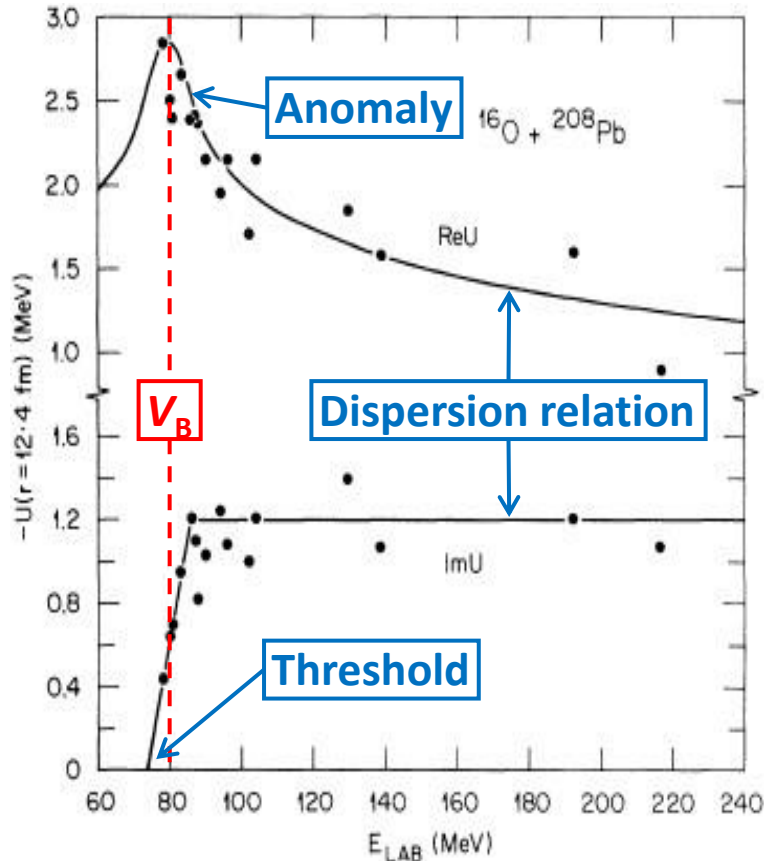
- ♠ A basic task in nuclear reaction study is to understand the nuclear interaction potential.

Cf: 1) S. Fernbach, R. Serber, and T. B. Taylor, Phys. Rev. **73**, 1352 (1949).

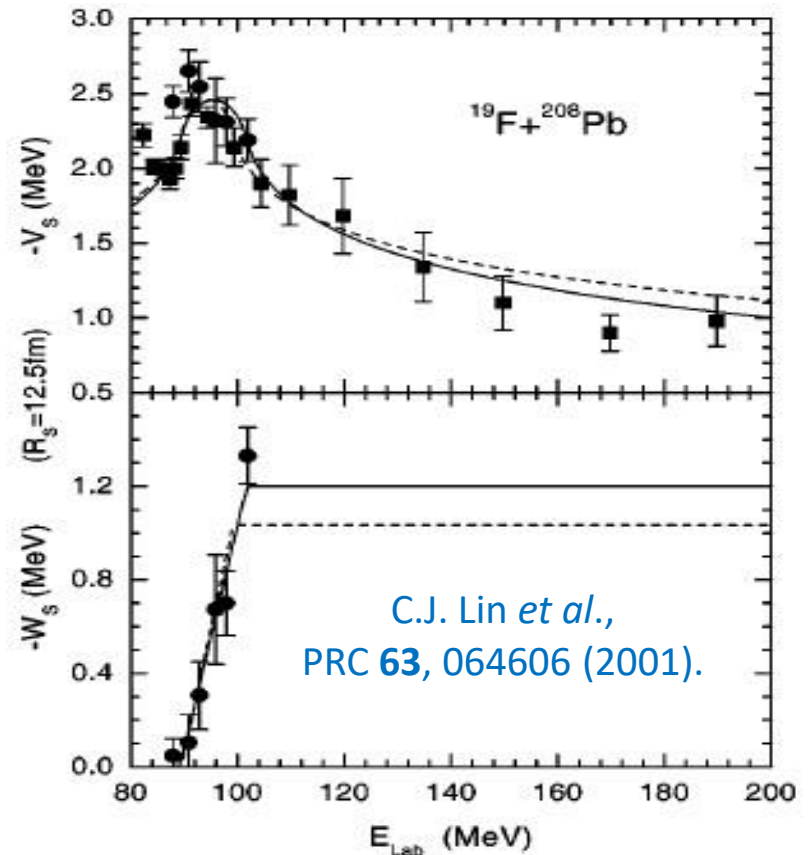
2) H. Feshbach, "The optical model and its justification", Ann. Rev. Nucl. Sci. **8**, 49 (1958).

# Tightly-bound Nuclei

## Threshold Anomaly



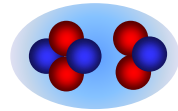
A universal phenomenon  
at energies around the Coulomb barrier



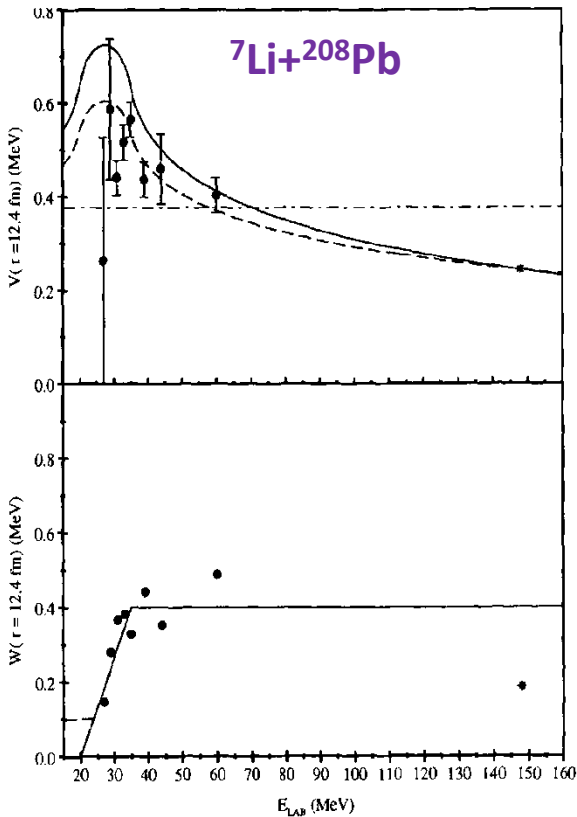
- Cf: 1) M. A. Nagarajan, C. C. Mahaux, and G. R. Satchler, Phys. Rev. Lett. **54**, 1136 (1985).  
 2) C. Mahaux, H. Ngo, and G. R. Satchler, Nucl. Phys. **A449**, 354 (1986).  
 3) G. R. Satchler, Phys. Rep. **199**, 147 (1991).

# Weakly-bound Stable Nuclei

## Threshold Anomaly

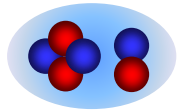


${}^7\text{Li} (\alpha+t)$   
 $S_\alpha = 2.47 \text{ MeV}$

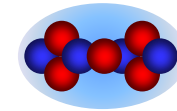
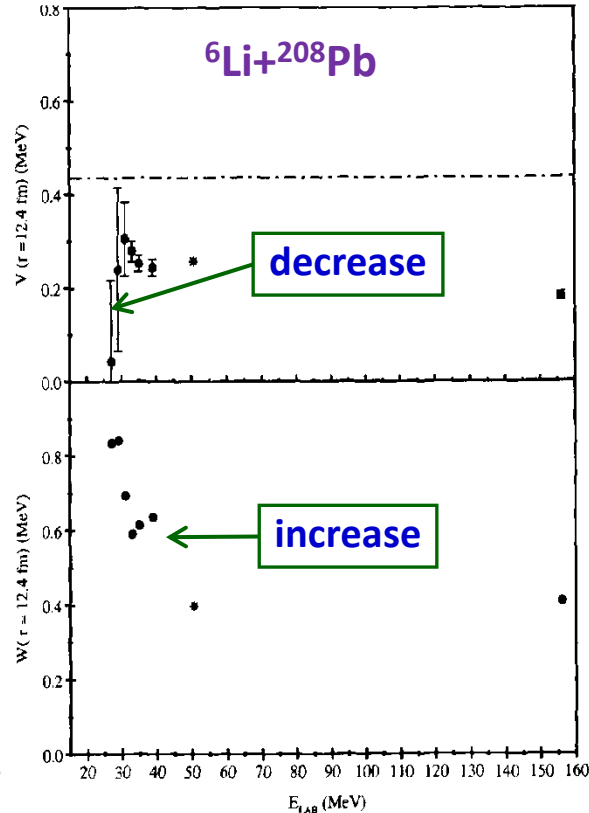


N. Keeley et al., Nucl. Phys. A **571**, 326 (1994).

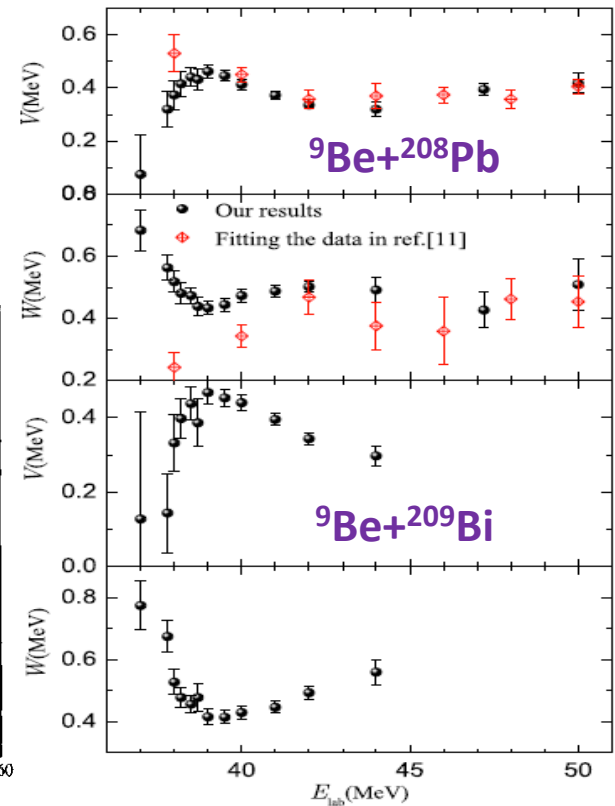
## Abnormal Threshold Anomaly



${}^6\text{Li} (\alpha+d)$   
 $S_\alpha = 1.47 \text{ MeV}$

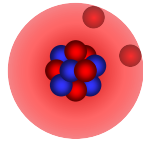


${}^9\text{Be} (\alpha+n+\alpha)$   
 $S_n = 1.66 \text{ MeV}$



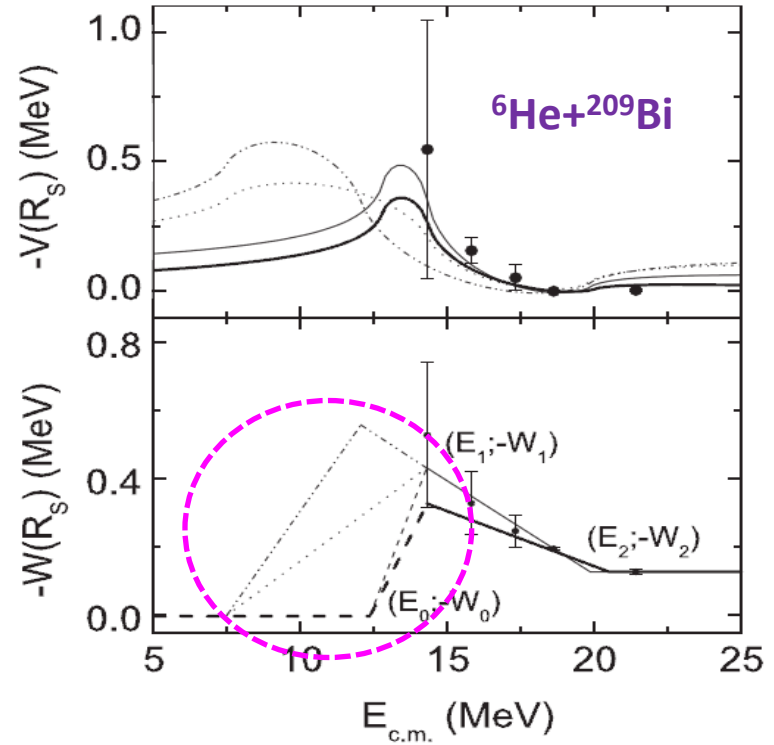
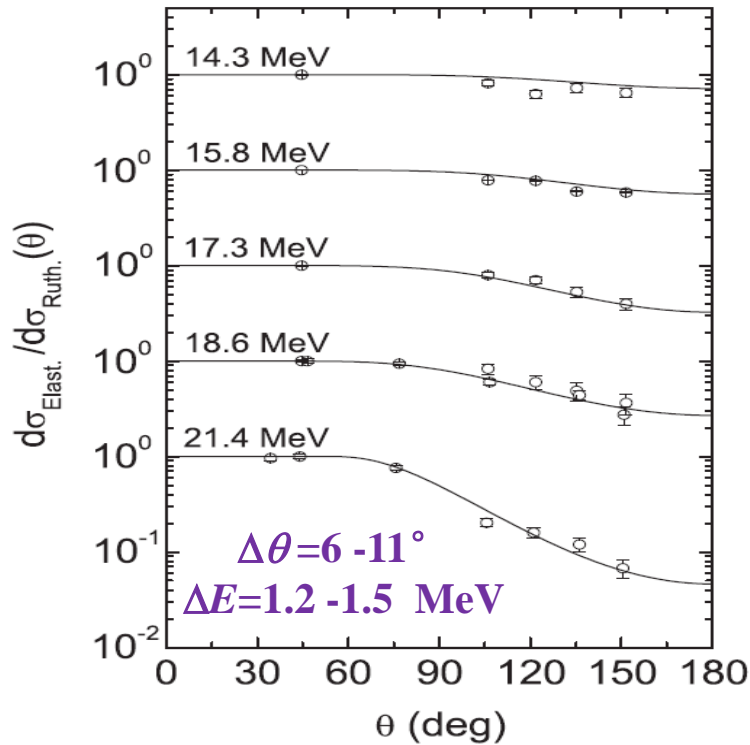
N. Yu et al., JPG **371**, 075108 (2010).

# Halo Nuclei



${}^6\text{He} (\alpha+2n)$   
 $S_{2n} = 0.98 \text{ MeV}$

**Abnormal Threshold Anomaly**

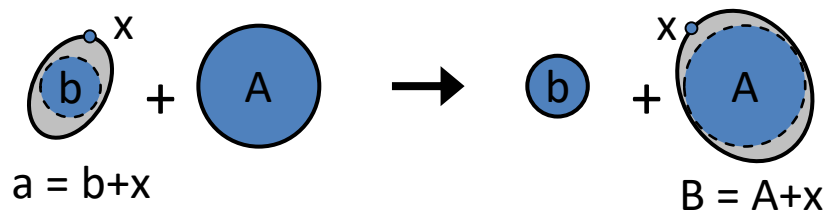


OMP's are usually extracted from elastic scattering.

★ Impossible to extract effective OMP's at energy far below the barrier.

Cf: 1) E.F. Aguilera *et al.*, PRL **84**, 5058 (2000); PRC **63**, 061603R  
 2) A. R. Garcia *et al.*, Phys. Rev. C **76**, 067603 (2007).

# OMP from Transfers



Transfer reaction  $A(a,b)B$

$$\left(\frac{d\sigma}{d\Omega}\right)_{if} = P_{if} \left( \underbrace{\left(\frac{d\sigma}{d\Omega}\right)_{ii}}_{\text{elastic scattering}} \cdot \underbrace{\left(\frac{d\sigma}{d\Omega}\right)_{ff}}_{\text{cross sections}} \right)^{1/2}$$

elastic scattering cross sections

Transition amplitude:  $T = J \int d^3r_b \int d^3r_a \chi^{(-)}(\vec{k}_f, \vec{r}_b)^* \langle bB|V|aA\rangle \chi^{(+)}(\vec{k}_i, \vec{r}_a)$ ,

4 wave functions are needed,

- ♣ two bound states:  $b+x$  &  $A+x$  (single-particle potential model)
- ♣ two scattering states: incoming & outgoing (optical potentials)

**First presented** at the **FUSION06**, Venice; C. J. Lin et al., AIP Conf. Proc. **853**, 81 (2006).

$^{16}\text{O}(^{14}\text{N}, ^{13}\text{C})^{17}\text{F}$ : Chin. Phys. Lett. **25**, 4237 (2008).

$^{11}\text{B}(^7\text{Li}, ^6\text{He})^{12}\text{C}$ : Chin. Phys. Lett. **26**, 022503 (2009). Phys. Rev. C **87**, 047601 (2013).

$^{208}\text{Pb}(^7\text{Li}, ^6\text{He})^{209}\text{Bi}$ : Phys. Rev. C **89**, 044615 (2014), Il Nuovo Cimento C **39**, 367 (2016), Chin. Phys. Lett. **31**, 092401 (2014), Phys. Rev. C **96**, 044615 (2017), Phys. Rev. Lett. **119**, 042503 (2017).

$^{63}\text{Cu}(^7\text{Li}, ^6\text{He})^{64}\text{Zn}$ : Phys. Rev. C **95**, 034616 (2017).



# Experiment of $^{208}\text{Pb}(^7\text{Li}, ^6\text{He})^{209}\text{Bi}$

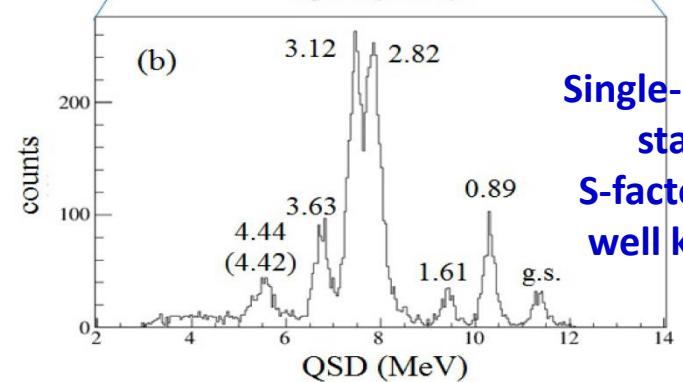
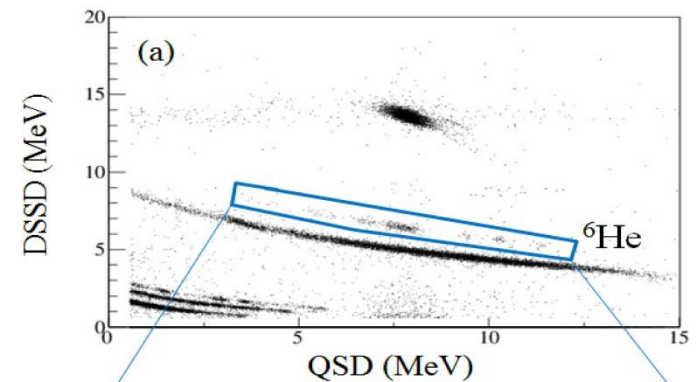
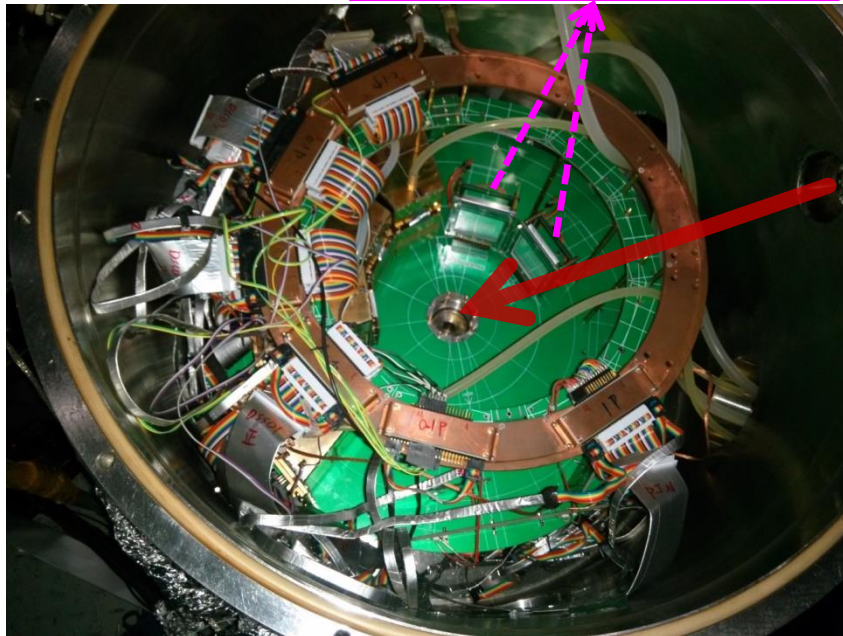
Two experiments have been done at HI-13 tandem accelerator @ CIAE

Exp1:  $E_{\text{beam}} = 42.55, 37.55, 32.55, \mathbf{28.55}, 25.67$  MeV – high energies **【2004.8】**

Exp2:  $E_{\text{beam}} = \mathbf{28.55}, 25.67, 24.3, 21.2$  MeV -- low energies **【2016.4】**

★ Angular distributions of both **elastic** scattering and **transfer** were measured.

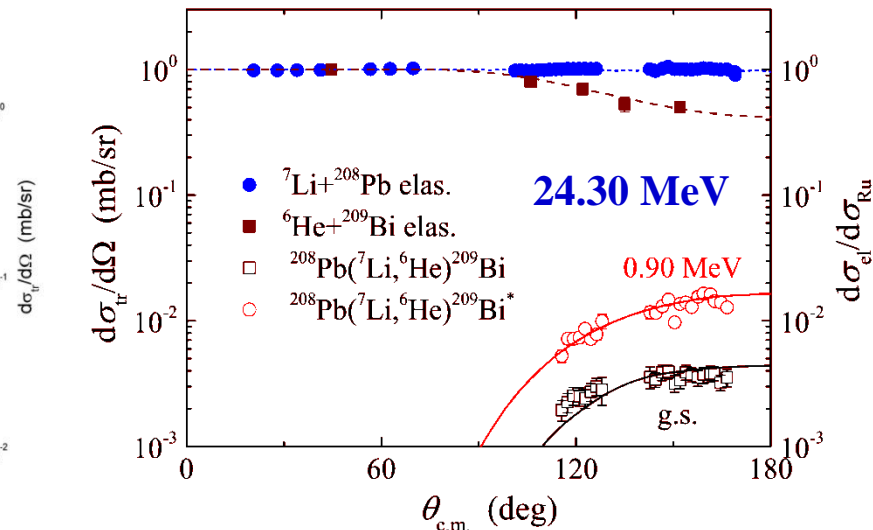
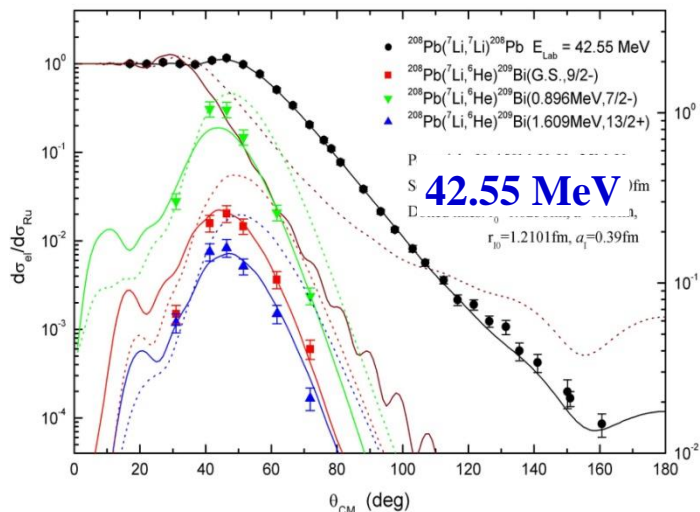
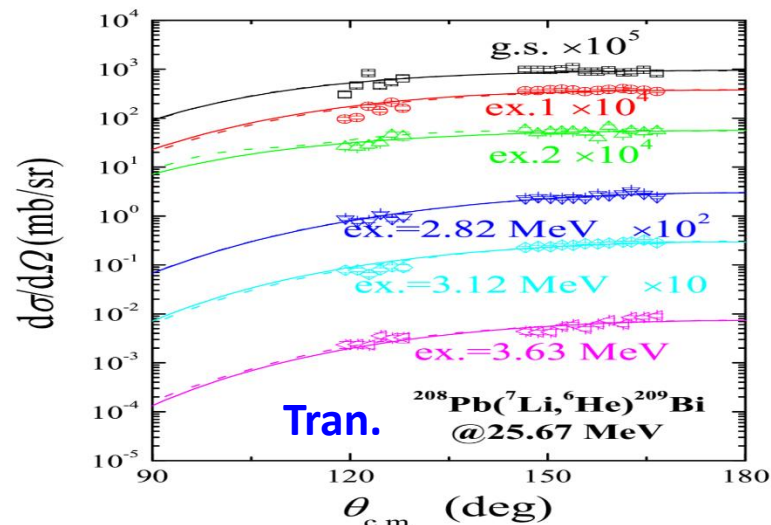
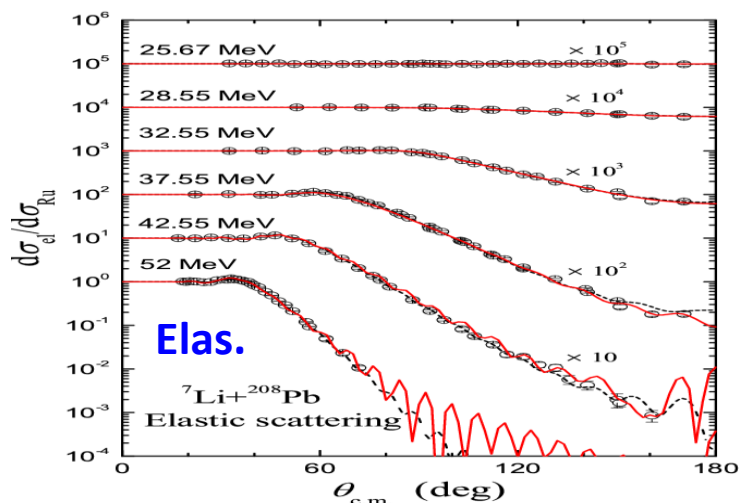
2 Telescopes: SSSD(20 $\mu\text{m}$ ) +  
DSSD(60 $\mu\text{m}$ ) + QSD(100 $\mu\text{m}$ )



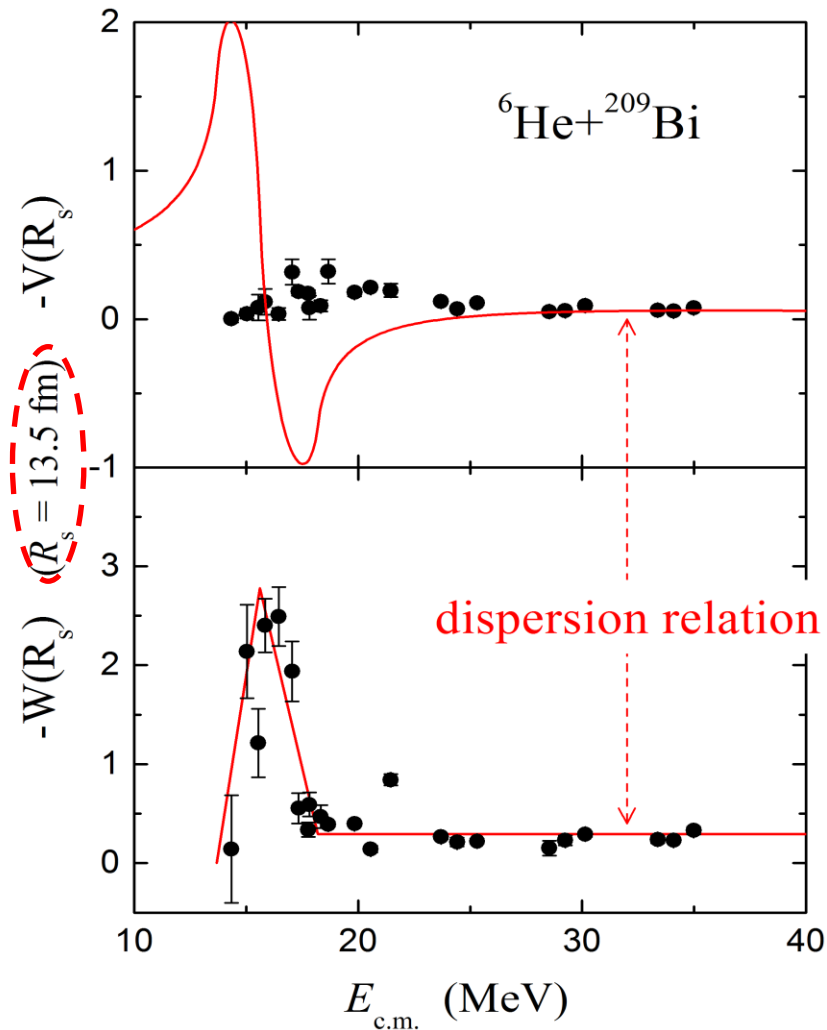


# Data Analysis of $^{208}\text{Pb}(^7\text{Li}, ^6\text{He})^{209}\text{Bi}$

## DWBA & CRC analyses



# OMPs of ${}^6\text{He}+{}^{209}\text{Bi}$



- ★ OMPs of the  ${}^6\text{He}+{}^{209}\text{Bi}$  system are determined precisely;
- ★ The decreasing trend in the imaginary part is observed, and the threshold energy is about 13.73 MeV ( $\sim 0.68V_B$ );
- ★ The dispersion relation cannot describe the behavior between the real and imaginary part.

L. Yang, C.J. Lin\*, H.M. Jia et al.,  
Phys. Rev. Lett. **119**, 042503 (2017);  
Phys. Rev. C **96**, 044615 (2017).

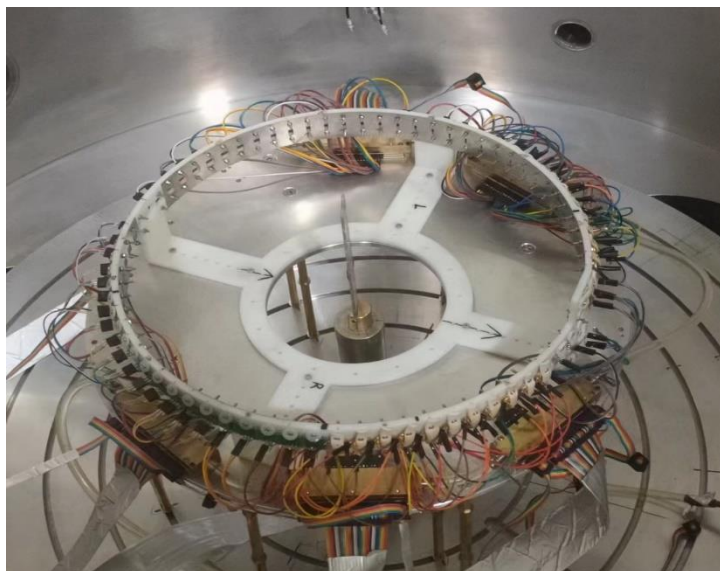
# Experiment of ${}^6\text{Li}+{}^{208}\text{Pb}$

**Motivation:** to extract the OMPs of  ${}^6\text{Li}+{}^{208}\text{Pb}$  with high precisions, especially at sub-barrier energies.

**Tow experiments have been done by the HI-13 tandem accelerator at CIAE.**

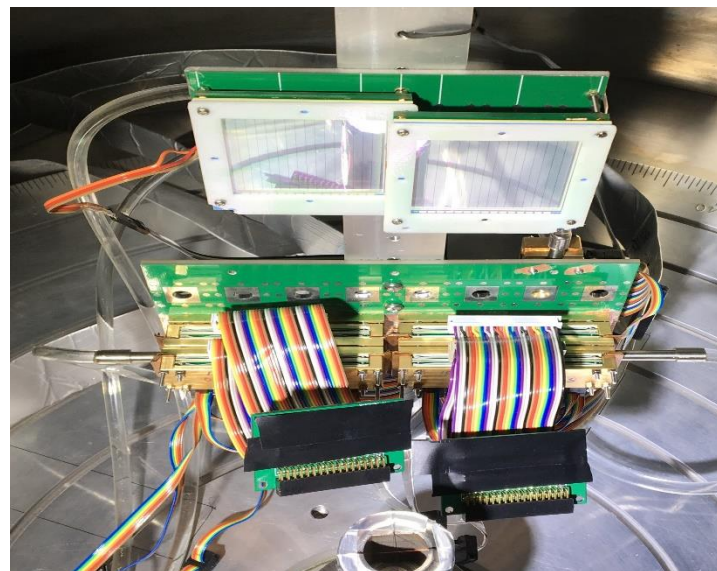
## 1. ${}^6\text{Li}+{}^{208}\text{Pb}$ elastic scattering

64 Si-PIN detectors have been installed around the target, covering  $20^\circ$ - $175^\circ$  in step of  $5^\circ$ .



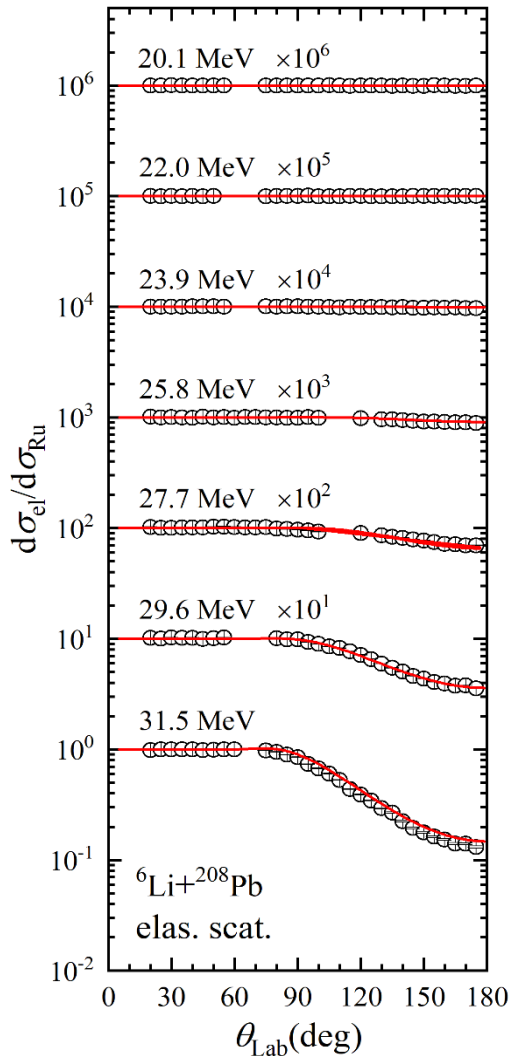
## 2. ${}^{207}\text{Pb}({}^7\text{Li}, {}^6\text{Li}){}^{208}\text{Pb}$ transfers

2  $\Delta E$ - $E_1$ - $E_2$  telescopes have been installed, consisting of  $40\ \mu\text{m}$  DSSD,  $300\ \mu\text{m}$  and  $1500\ \mu\text{m}$  QSD.

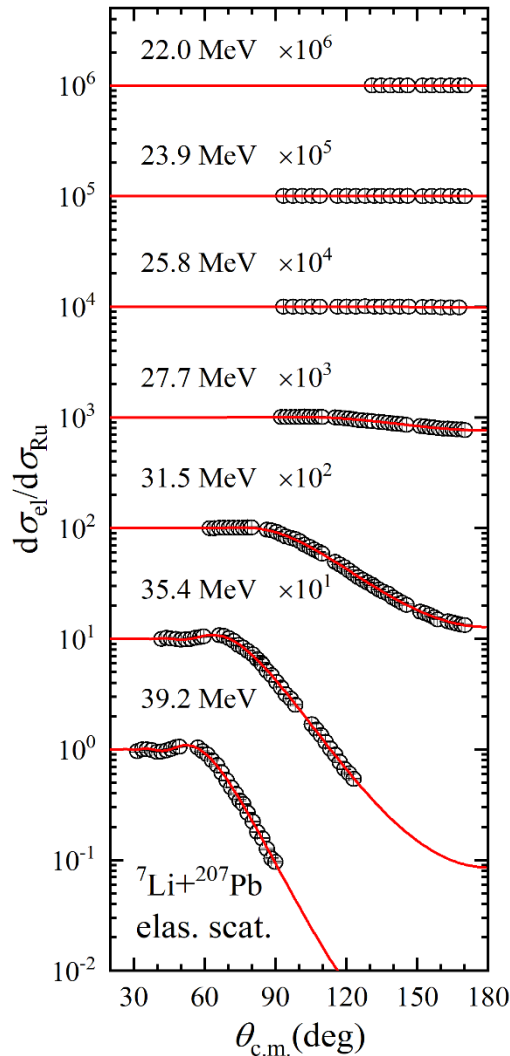


# Angular Distributions

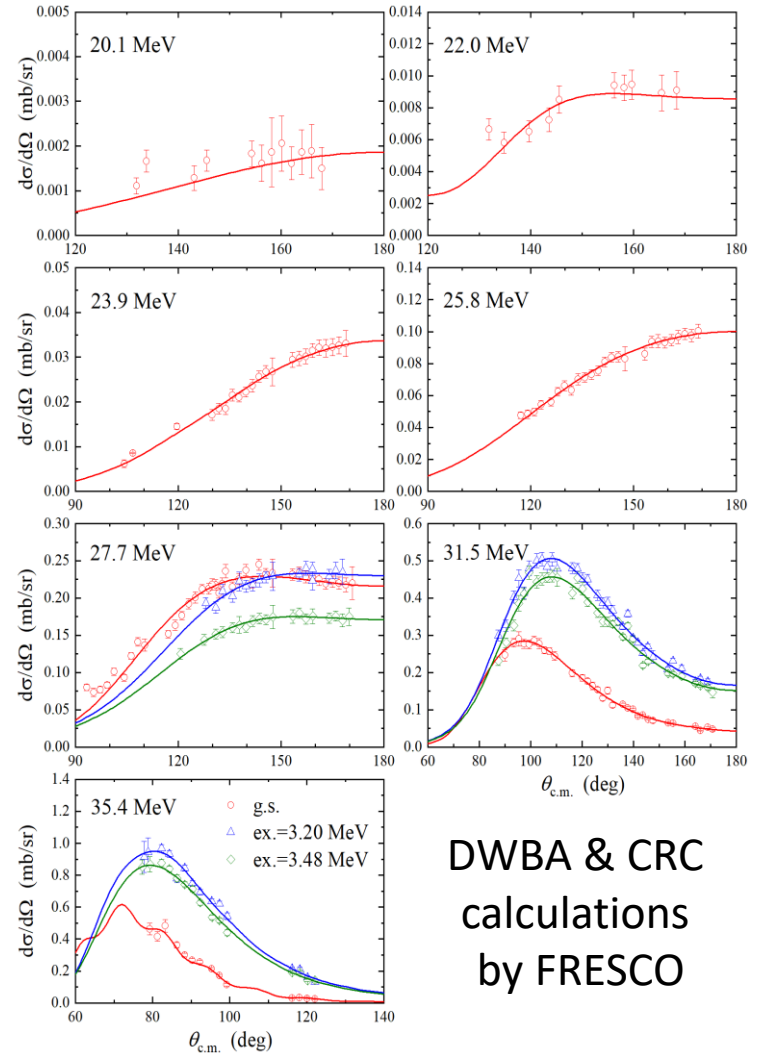
${}^6\text{Li}+{}^{208}\text{Pb}$  elas.



${}^7\text{Li}+{}^{207}\text{Pb}$  elas.

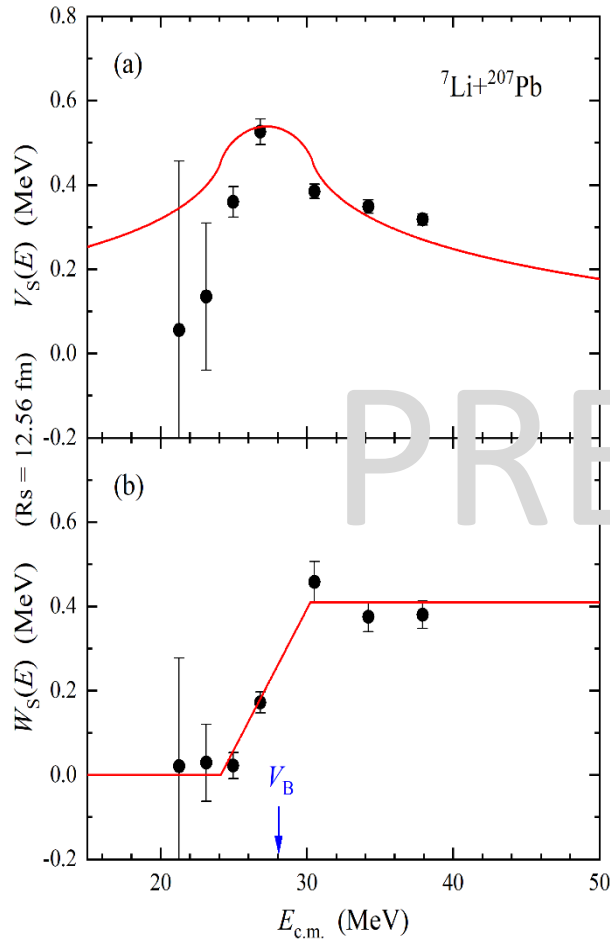


${}^{207}\text{Pb}({}^7\text{Li}, {}^6\text{Li}){}^{208}\text{Pb}$  tran.



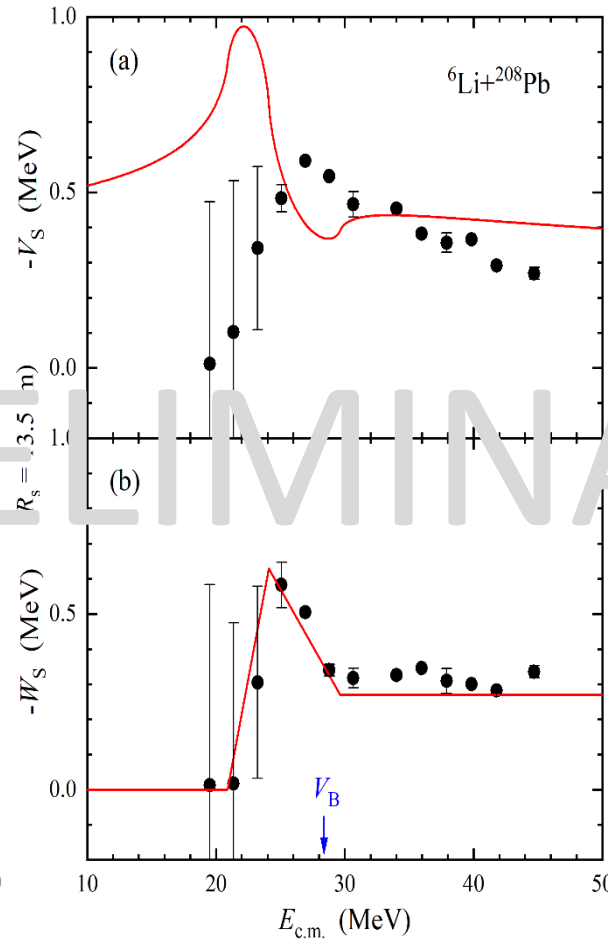
# OMPs

${}^7\text{Li}+{}^{207}\text{Pb}$   
from elastic



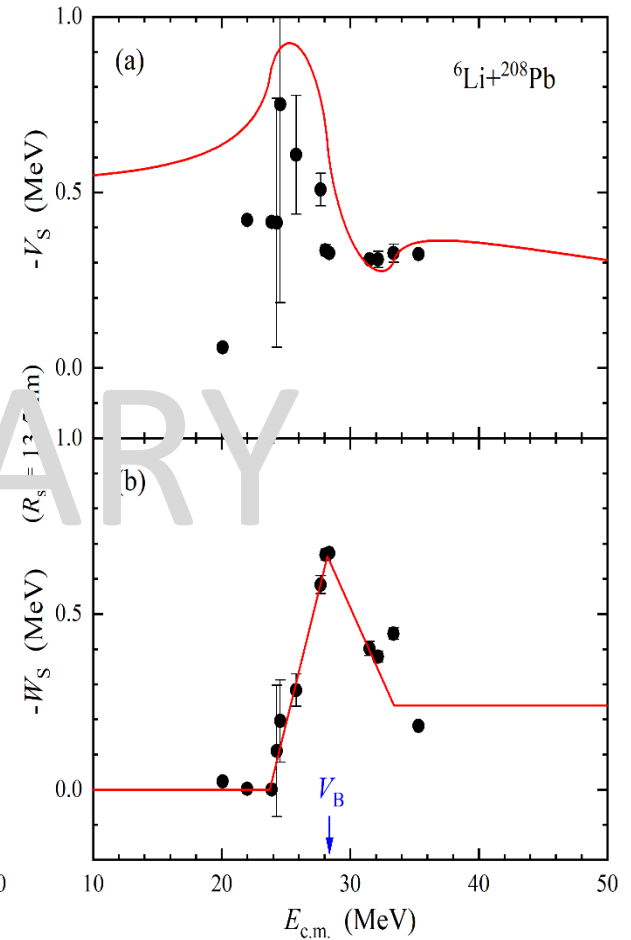
normal

${}^6\text{Li}+{}^{208}\text{Pb}$   
from elastic



abnormal

${}^6\text{Li}+{}^{208}\text{Pb}$   
from transfer



abnormal

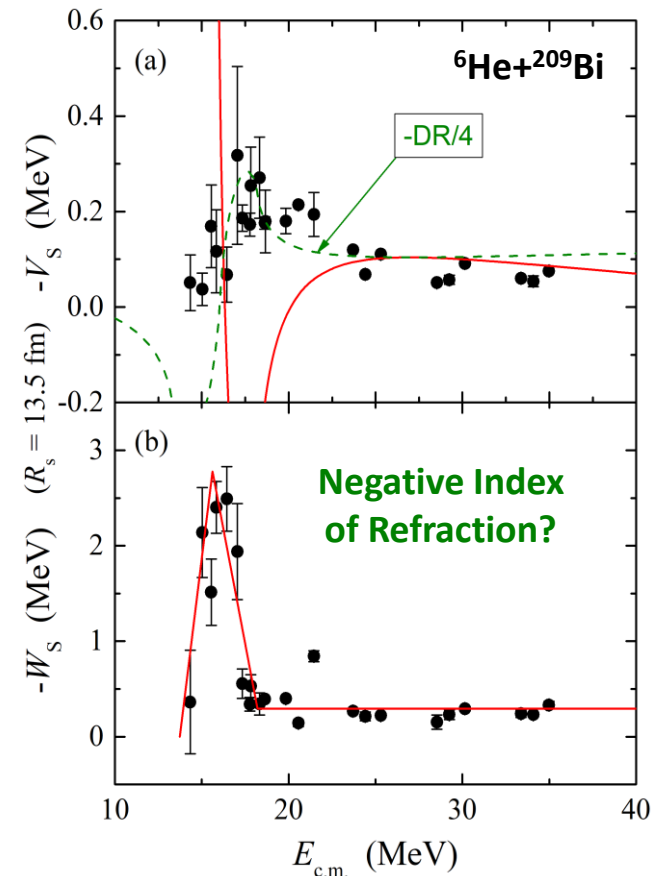
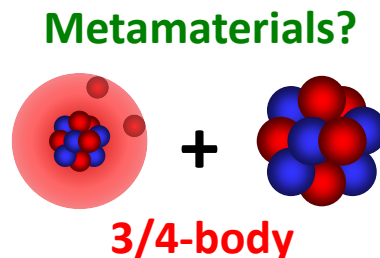
# Dispersion Relation



- ★ Dispersion relation results from causality, connecting real and imaginary part;
- ★ Any wave/particle should follow this rule when it passes through a media;
- ★ The classical dispersion relation is **not** applicable for  ${}^6\text{He}+{}^{209}\text{Bi}$  and  ${}^6\text{Li}+{}^{208}\text{Pb}$ .

## Possible reasons:

- Causality  $\rightarrow$  dispersion relation  
stable systems: causality  $\leftrightarrow$  analyticity
- Cauchy integration  
infinity poles (breakup) & off-axis (multi-process)
- **Negative Index of Refraction**  
causality based criteria must be used with care  
[Phys. Rev. Lett. **101**, 167401 (2008).]
- **Locality vs. non-locality**  
equivalent local potential in Schrödinger equation



# Contents

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## 1. OMPs of weakly-bound nuclear systems

${}^6\text{He}+{}^{209}\text{Bi}$ ,  ${}^6\text{Li}+{}^{208}\text{Pb}$

## 2. Breakups of weakly-bound nuclei

- stable nuclei:  ${}^{6,7}\text{Li}+{}^{209}\text{Bi}$

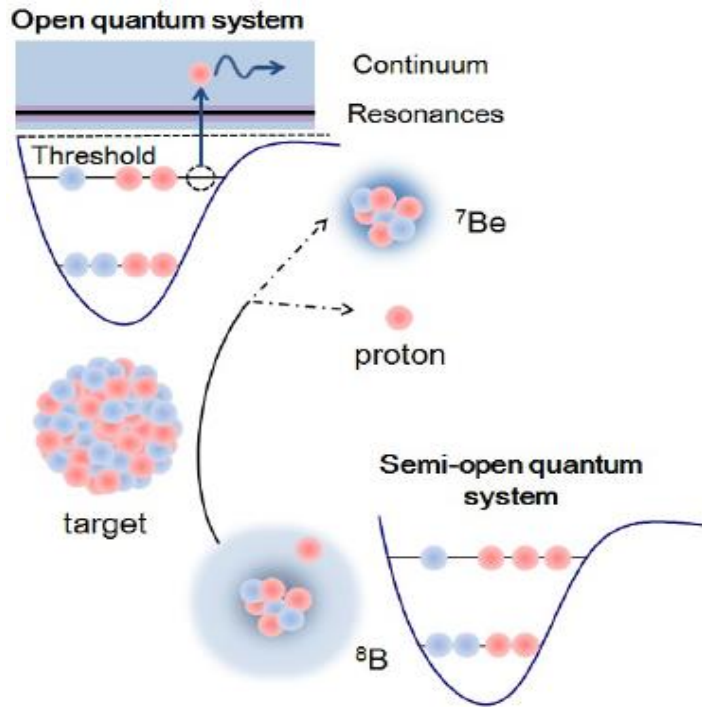
- proton-rich nuclei:  ${}^{17}\text{F}+{}^{58}\text{Ni}$ ,  ${}^8\text{B}+{}^{120}\text{Sn}$

## 3. Summary and outlook

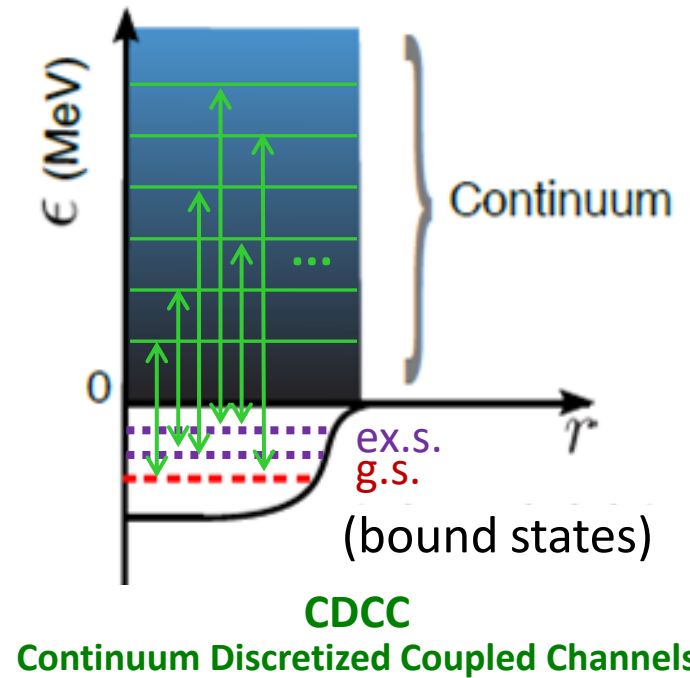


# Breakup $\rightarrow$ Open Quantum System

- ★ Reactions with weakly-bound nuclei: easily breakup, and leading to continuum state



From semi-open quantum system to open quantum system



Strongly couplings of low-lying states to continuum states

# Complex Processes

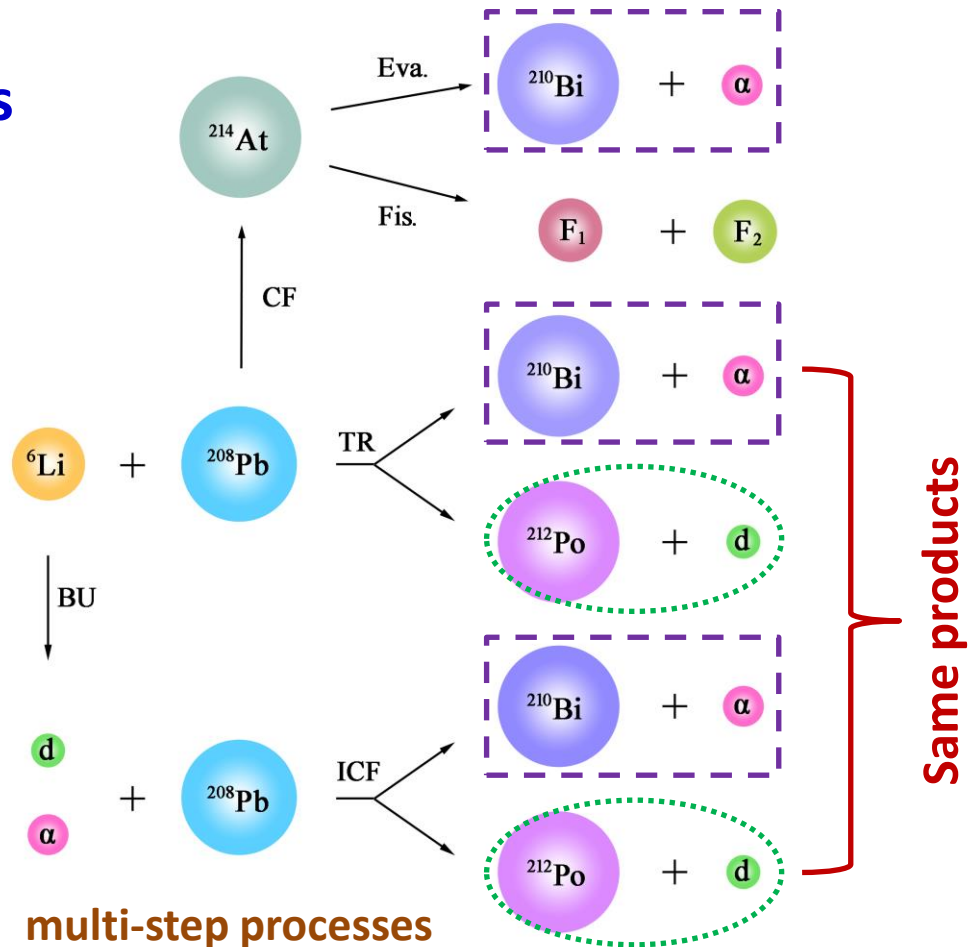
★ How to identify different reaction processes in a experiment?

complete-kinematics  
measurement



2-body kinematics 

3-body kinematics 



# Researches in NRG@CIAE

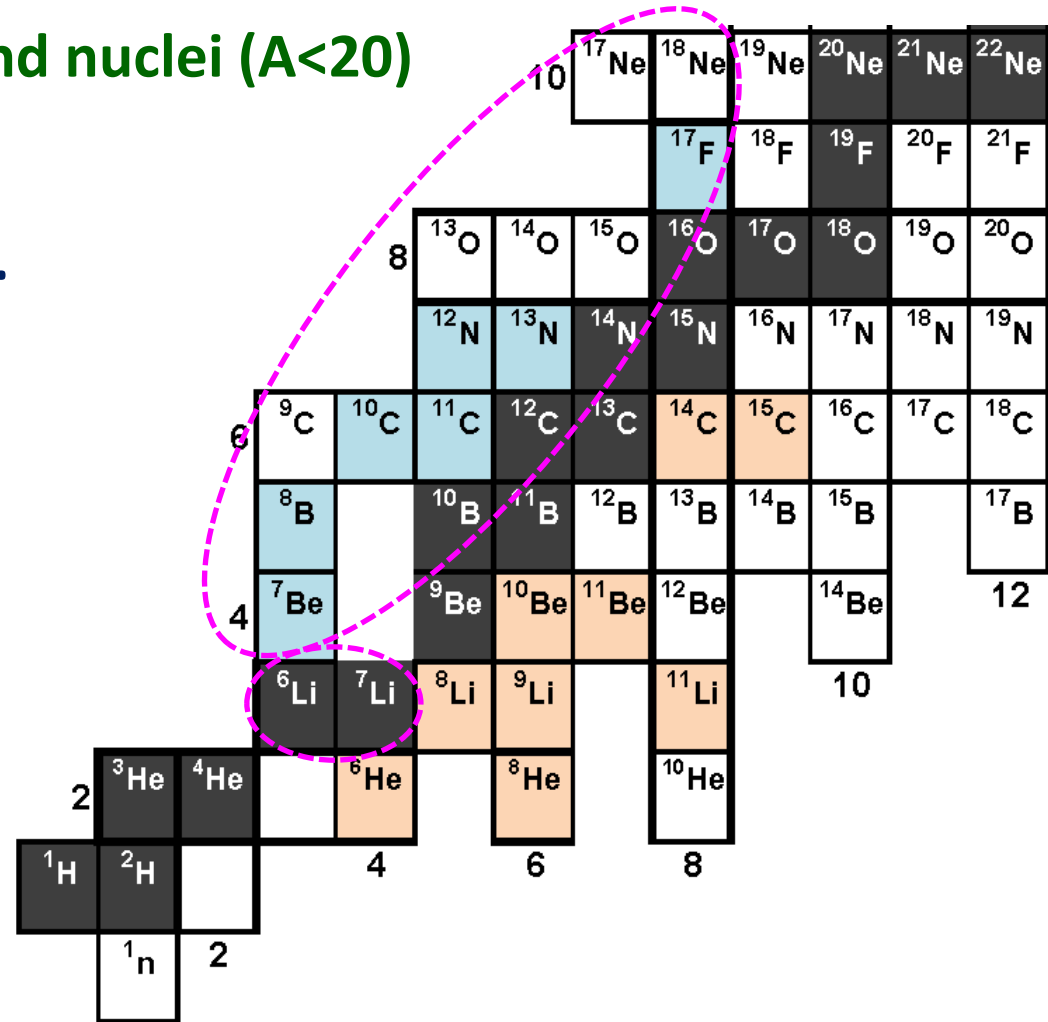
## Reactions with weakly-bound nuclei ( $A < 20$ )

👉 Elastic, fusion, breakup ...

👉 Stable:  ${}^6, {}^7\text{Li}$ ,  ${}^9\text{Be}$

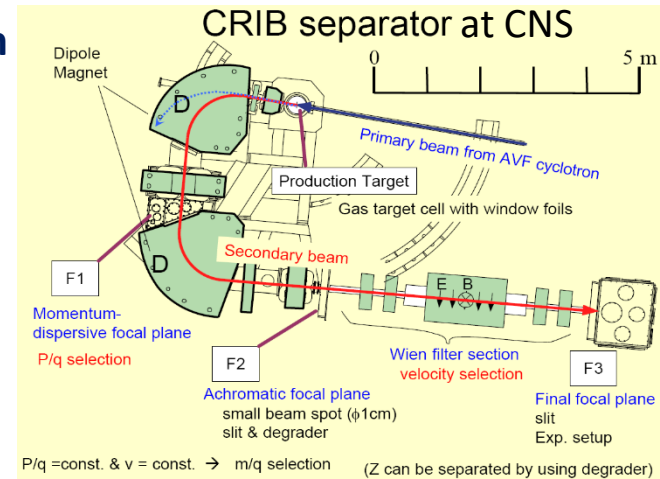
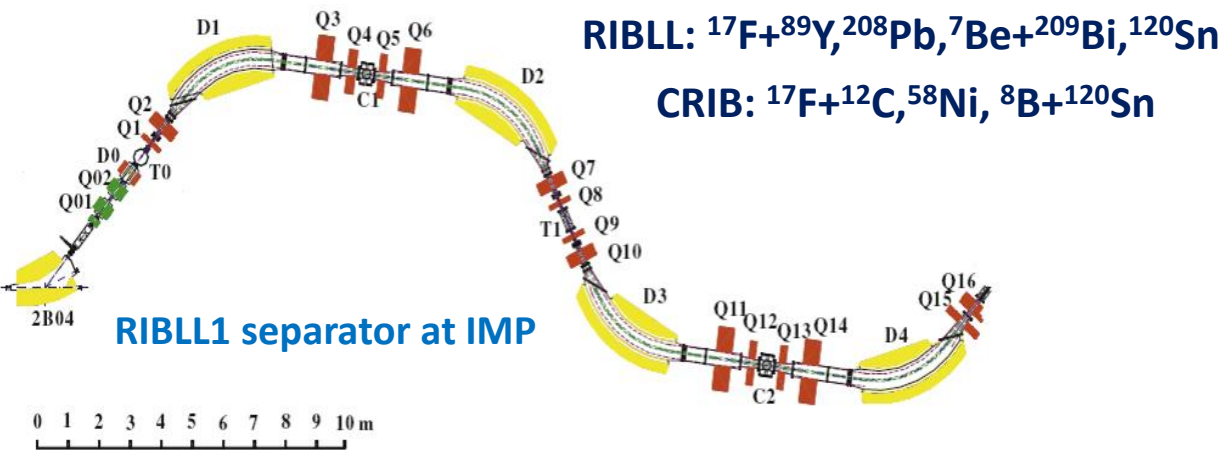
👉 p-rich:  ${}^7\text{Be}$ ,  ${}^8\text{B}$ ,  ${}^{17}\text{F}$ ,  
 ${}^{10}\text{C}$ ,  ${}^{12}\text{N}$ ,  ${}^{17,18}\text{Ne}$  ...

👉 Complete-kinematics  
measurement  
(particle identification &  
large solid-angle covered)



# Overview of RIB Experiments

★ Complete-kinematics measurement ; ★ Reactions induced by  ${}^7\text{Be}$ ,  ${}^8\text{B}$ ,  ${}^{17}\text{F}$  ...

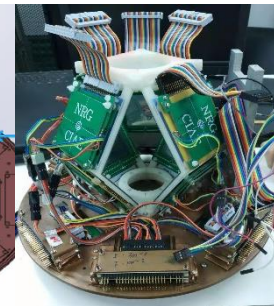
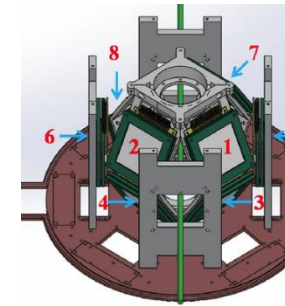
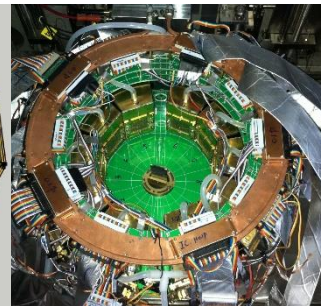
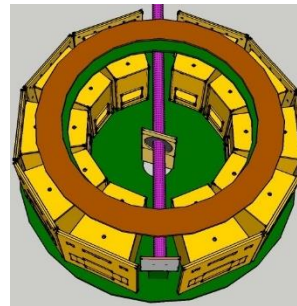
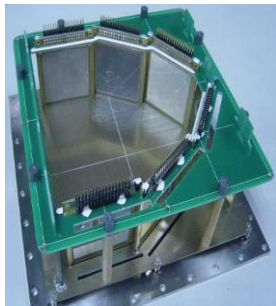


${}^{17}\text{F}+{}^{12}\text{C}$   
 2007@CRIB

${}^{17}\text{F}+{}^{89}\text{Y}$   
 2015@RIBLL1

${}^{17}\text{F}+{}^{208}\text{Pb}$ , 2015@RIBLL1  
 ${}^{17}\text{F}+{}^{58}\text{Ni}$ , 2015@CRIB

${}^7\text{Be}+{}^{209}\text{Bi}$ , 2018@RIBLL1  
 ${}^8\text{B}+{}^{120}\text{Sn}$ , 2019@CRIB  
 ${}^7\text{Be}+{}^{120}\text{Sn}$ , 2021@RIBLL1



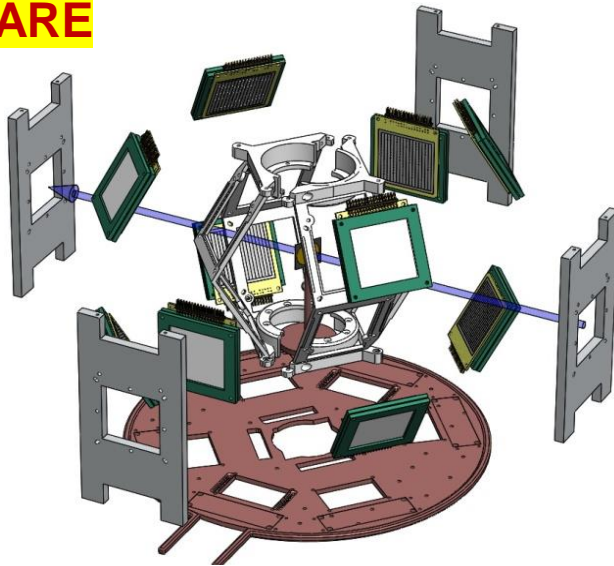
EPJA **48**, 65 (2012); PRC **97**, 044618 (2018); EPJA **57**, 143 (2021); PLB **813**, 136045 (2021); NC **13**, 7193 (2022) ...



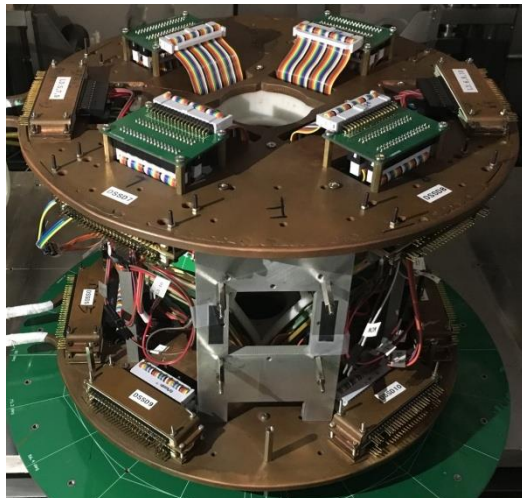
# Detector Arrays

## STARE

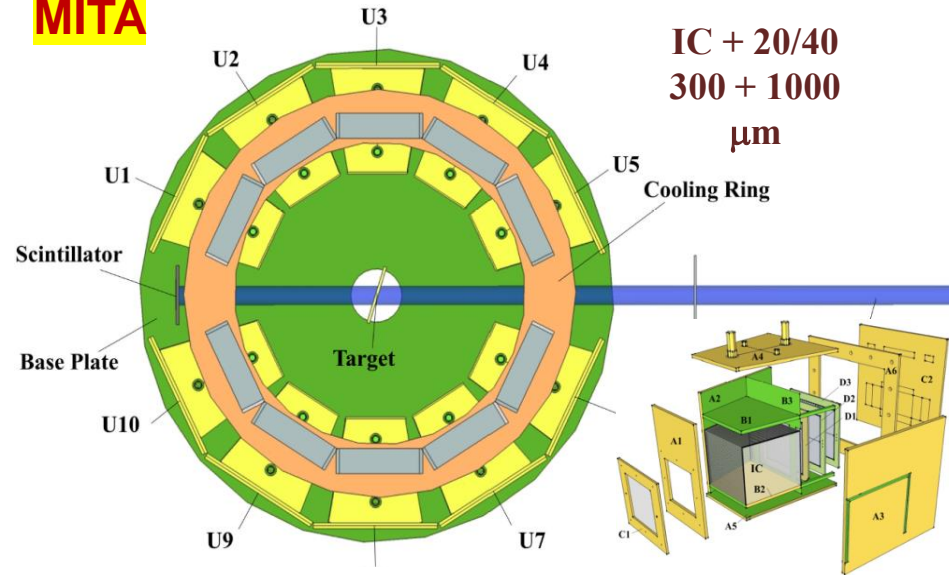
20/40  
+  
300  
+  
1000  
 $\mu\text{m}$



10 sets, 3 layers, 40%  $4\pi$



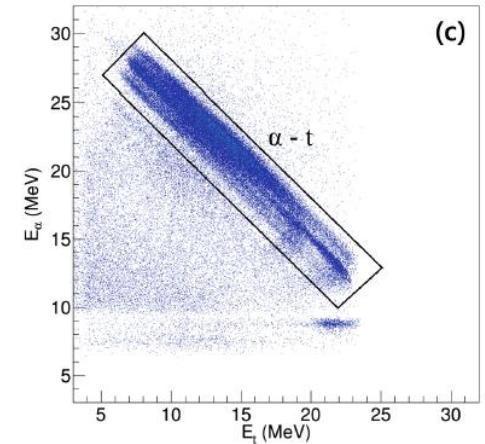
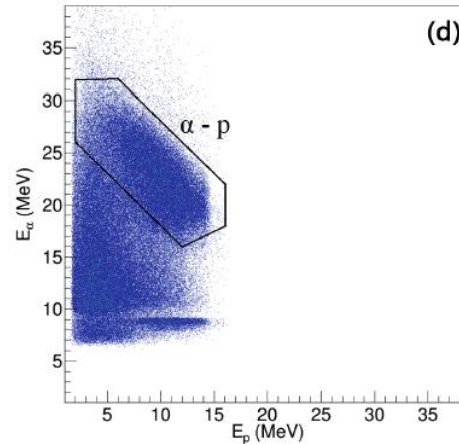
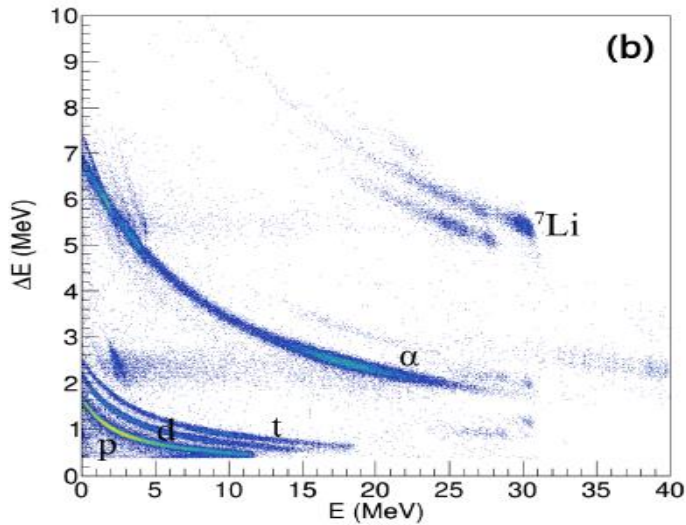
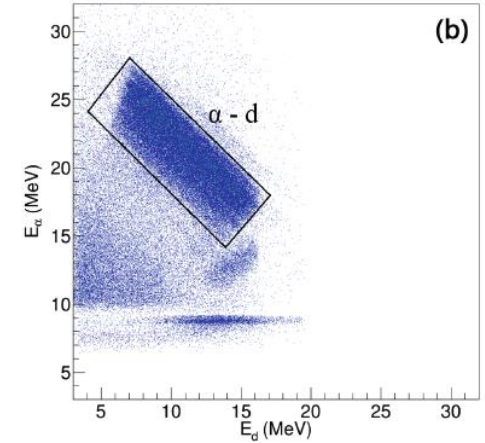
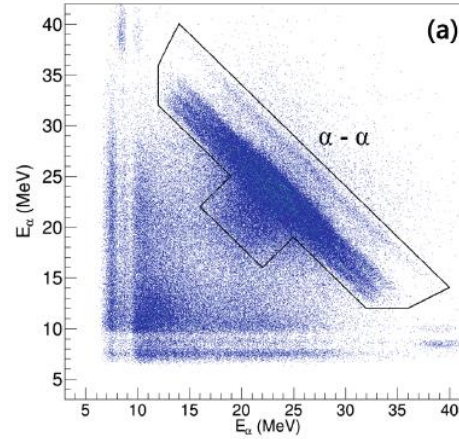
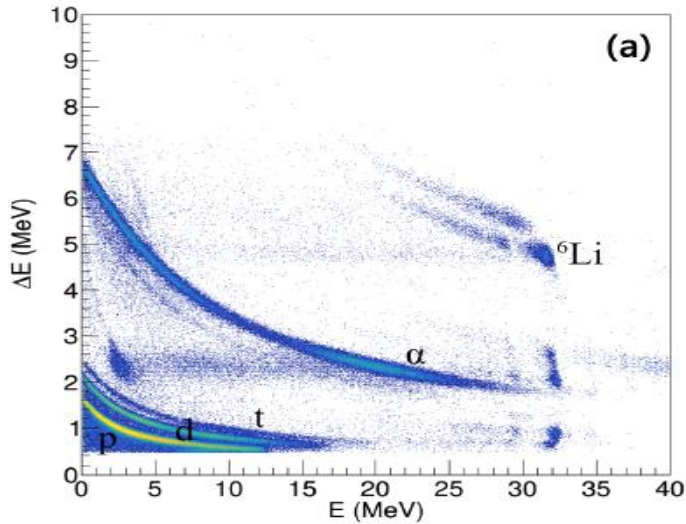
## MITA



10 sets, 4 layers, 8%  $4\pi$



# $6,7\text{Li}+^{209}\text{Bi}$ : Spectra

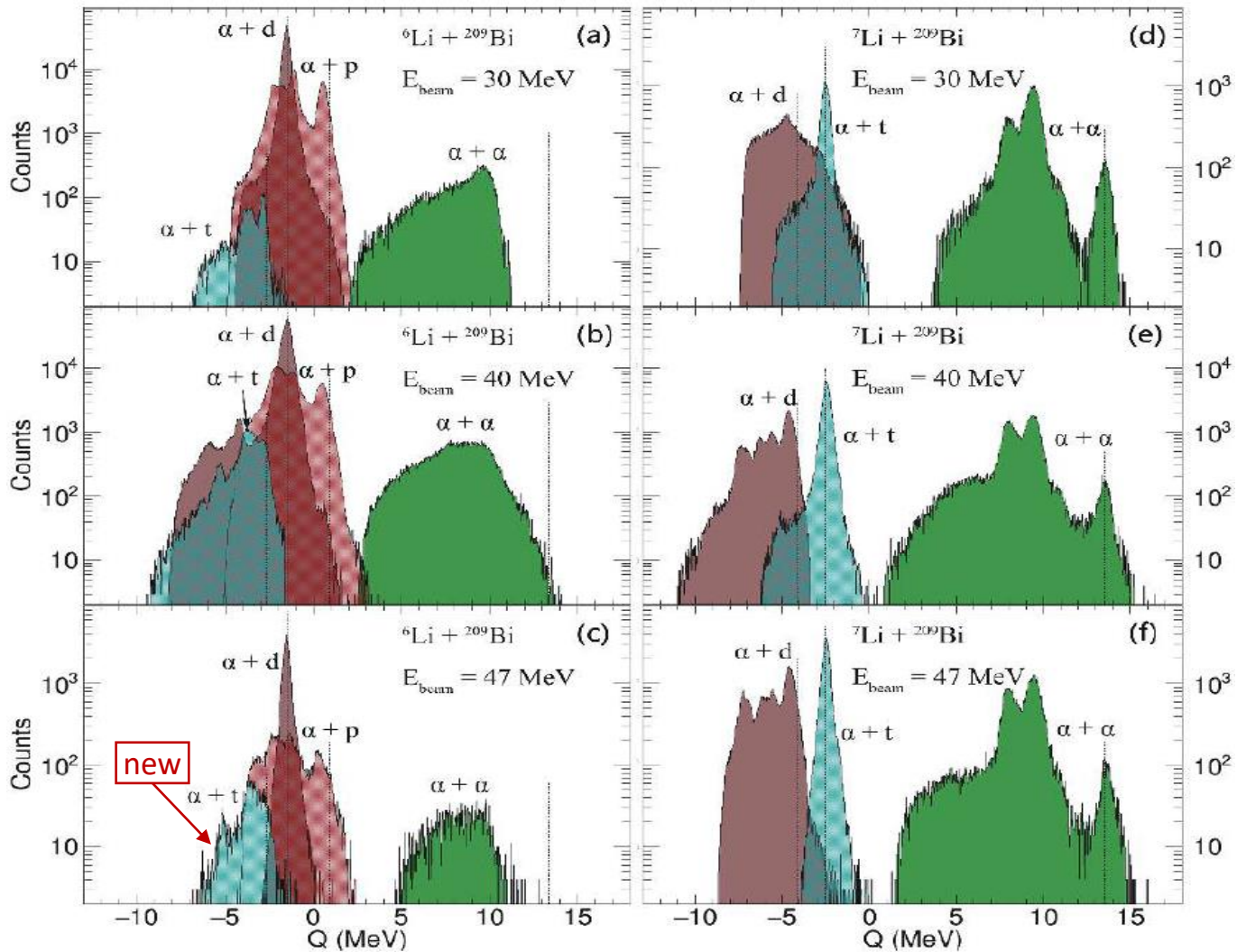


Energy correlations of breakup fragments

$\Delta E$ - $E$  Spectra of  $6,7\text{Li}+^{209}\text{Bi}$  @ 40 MeV



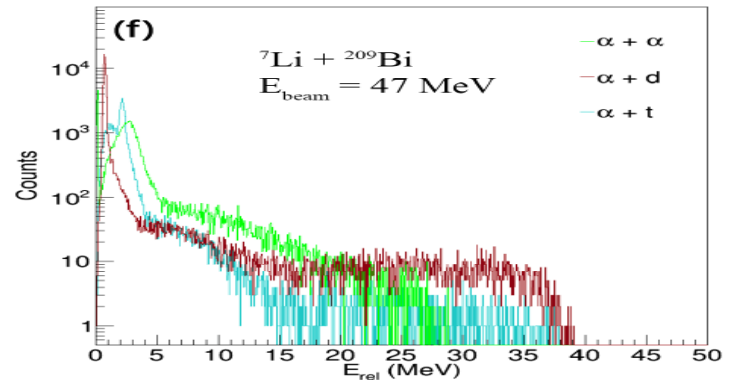
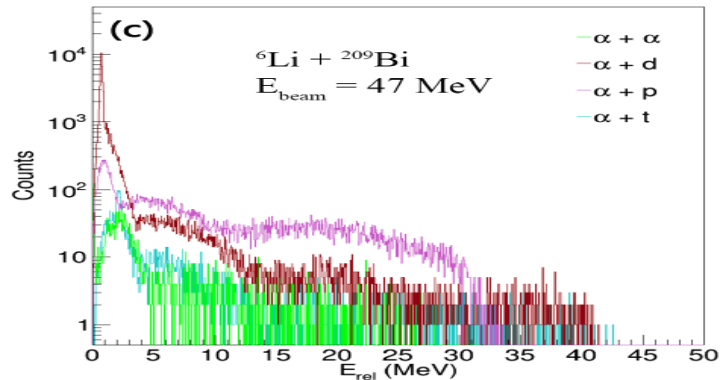
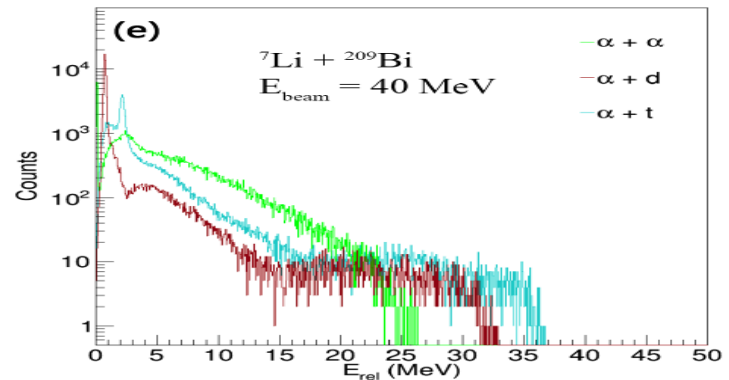
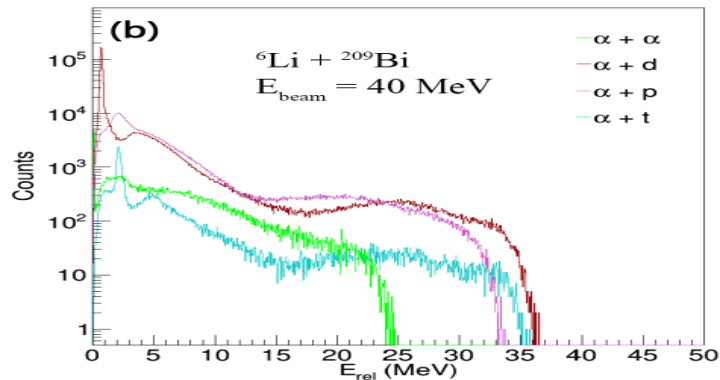
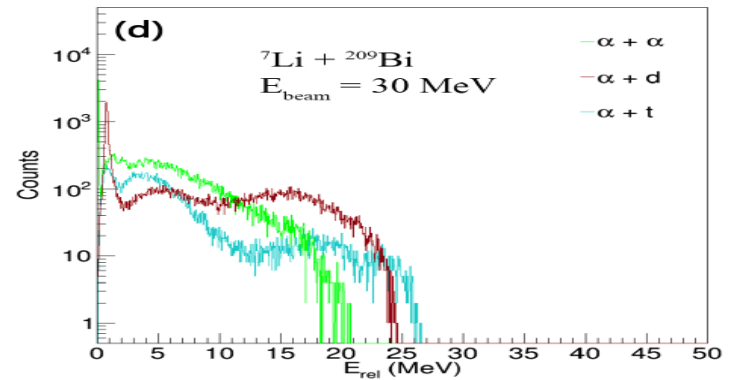
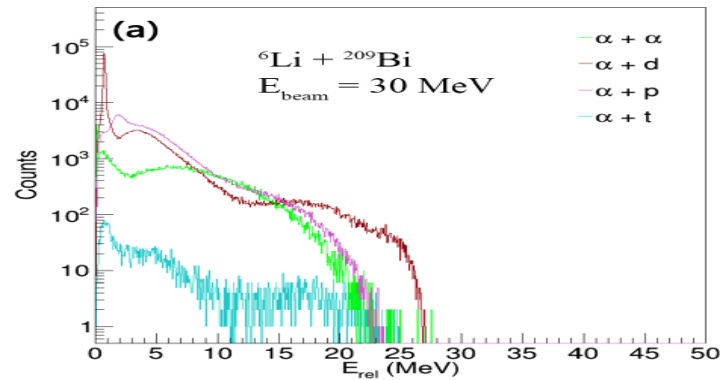
# ${}^6,7\text{Li} + {}^{209}\text{Bi}$ : Q-value Spectra



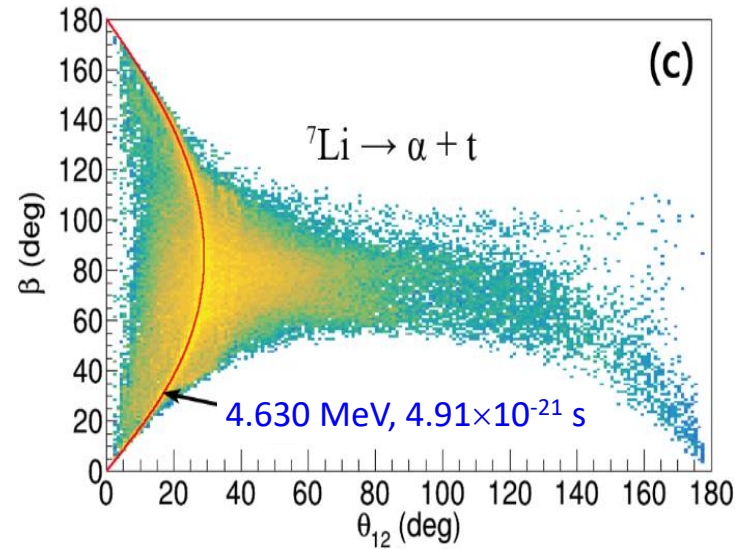
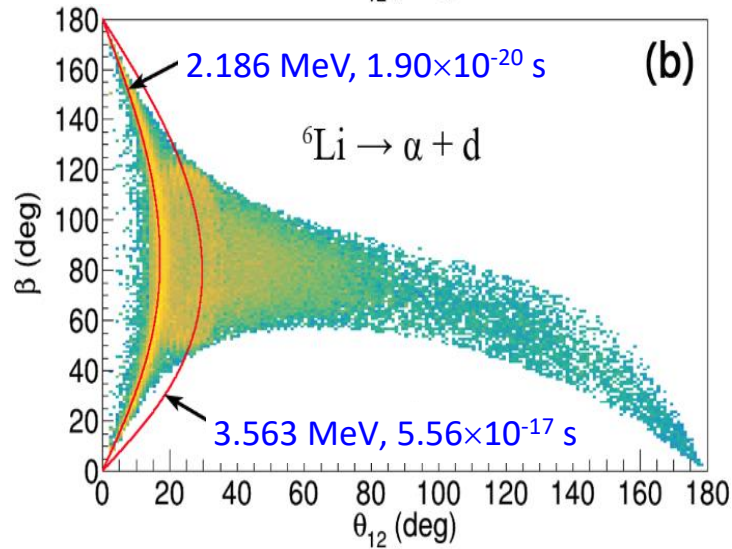
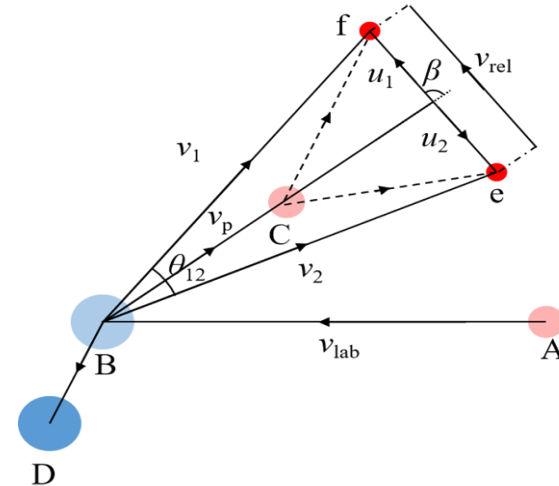
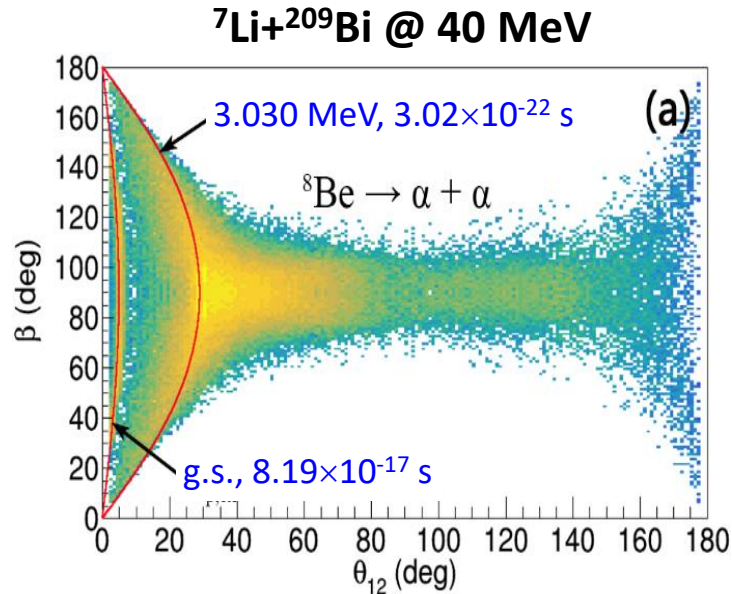
Y.J. Yao *et al.*, Nucl. Sci. Tech. **32**, 14 (2021); Chin. Phys. C **45**, 054104 (2021).



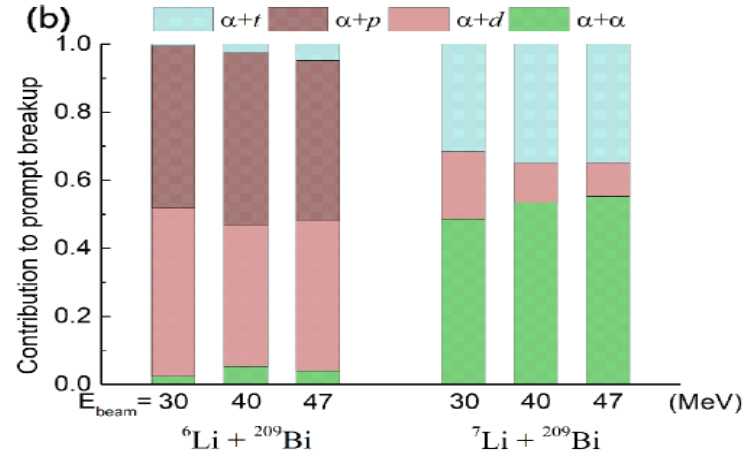
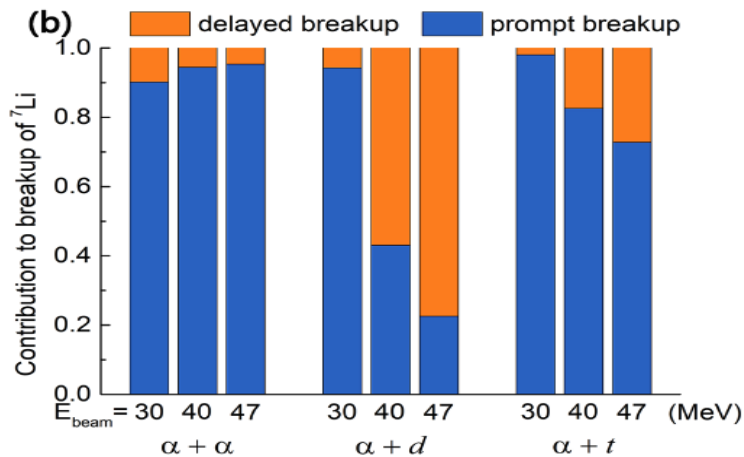
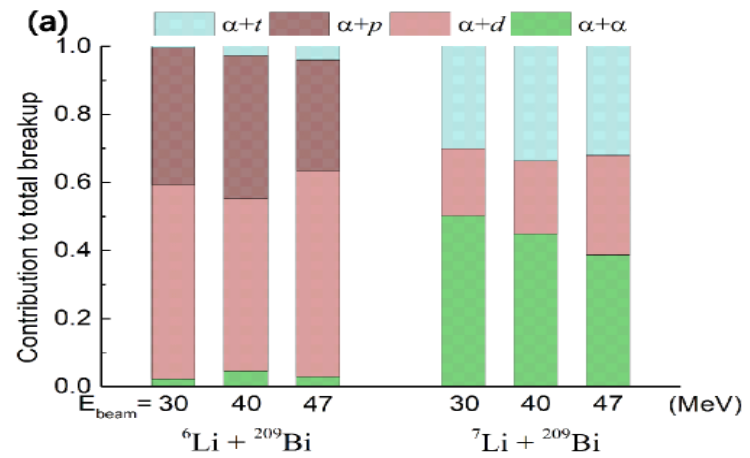
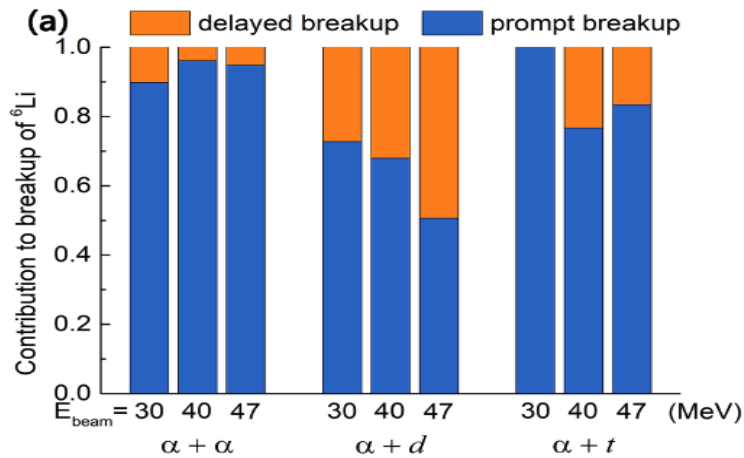
# ${}^6,7\text{Li} + {}^{209}\text{Bi}$ : Relative Energies



# 6,7Li+<sup>209</sup>Bi: Angular Correlations



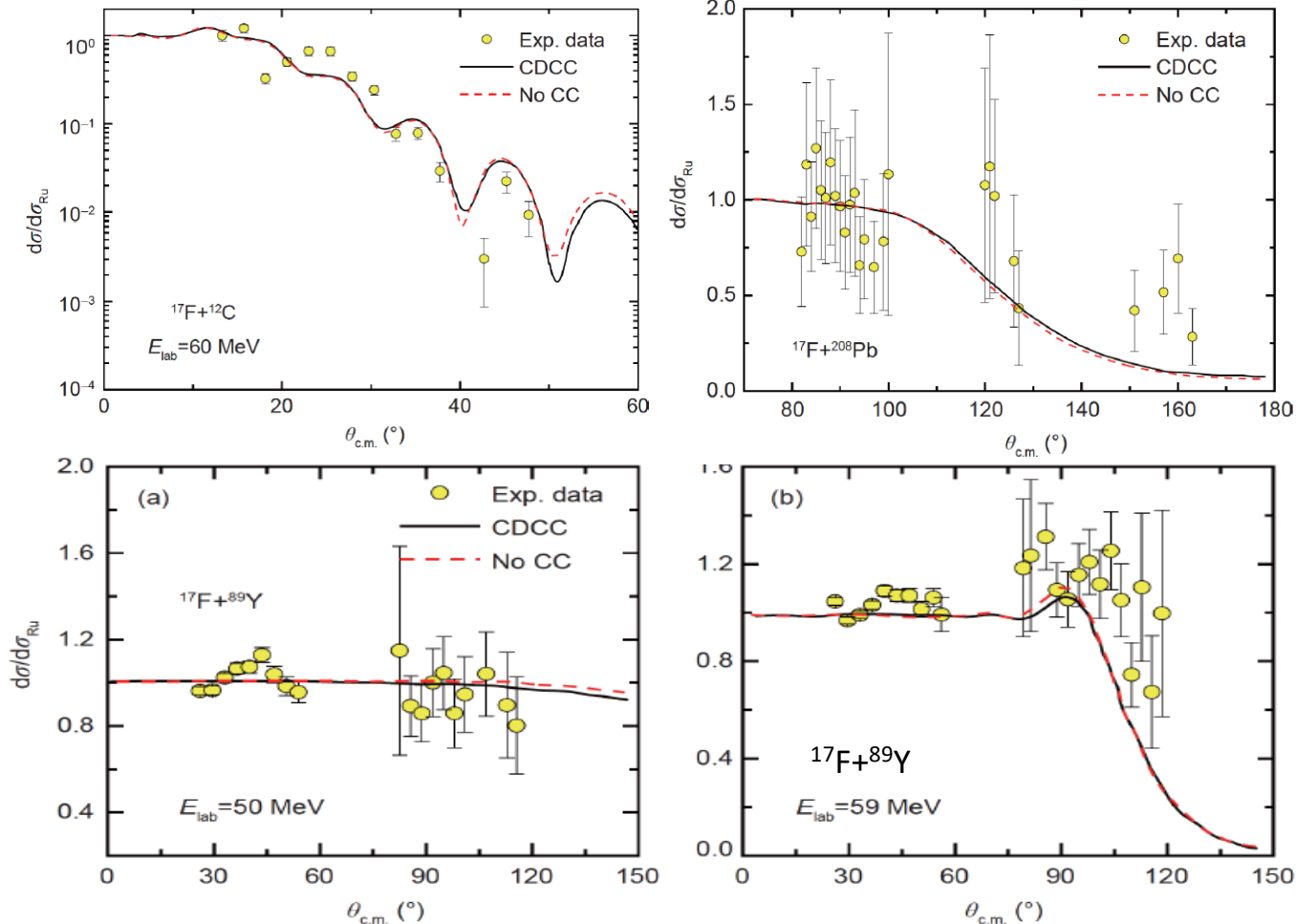
# $6,7\text{Li} + {}^{209}\text{Bi}$ : Branch Ratios of Breakups



L. Yang *et al.*, Fundamental Research, in press.

★ Rich information on breakups of  $6,7\text{Li} + {}^{209}\text{Bi}$  was obtained experimentally, which requires a unified theory to comprehensively understand the dynamics and its influences.

# $^{17}\text{F}+^{12}\text{C}$ , $^{89}\text{Y}$ , $^{208}\text{Pb}$ : Elastic Scattering



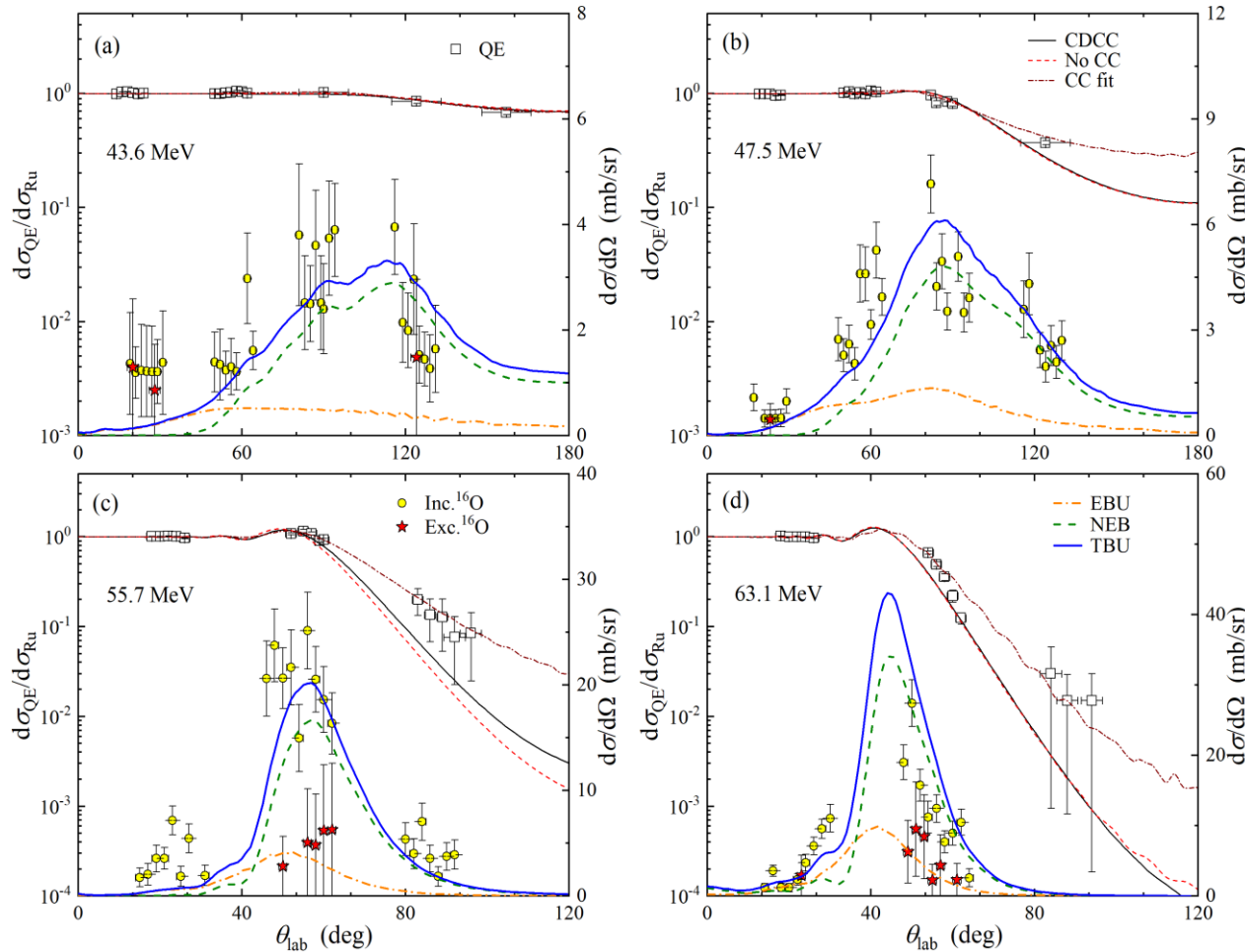
No obvious breakup effects were observed.

Eur. Phys. J. A **48**, 65 (2012); Phys. Rev. C **97**, 044618 (2018); Eur. Phys. J. A **57**, 143 (2021).

# $^{17}\text{F} + ^{58}\text{Ni}$ : Nonelastic Breakup

Quasielastic, inclusive & exclusive breakup, total fusion have been obtained by the

complete-kinematics measurement for the first time.



**Quasi-elastic:**

□ CDCC effects are not significant

**Breakup:**

□ EBU — CDCC

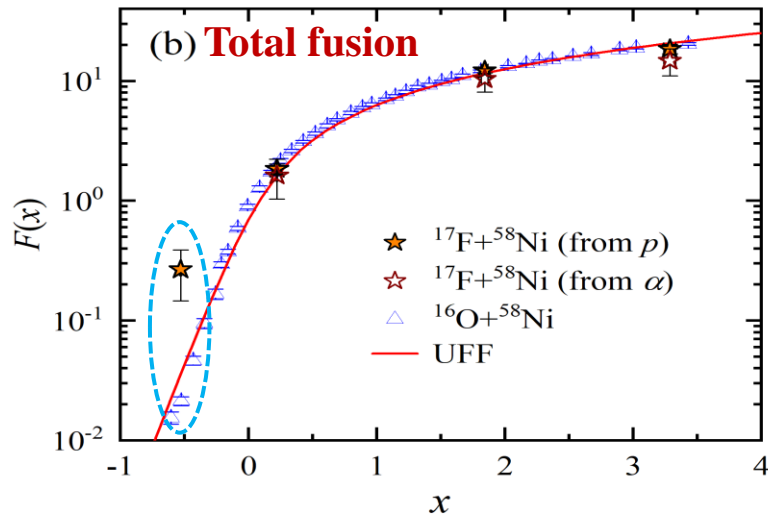
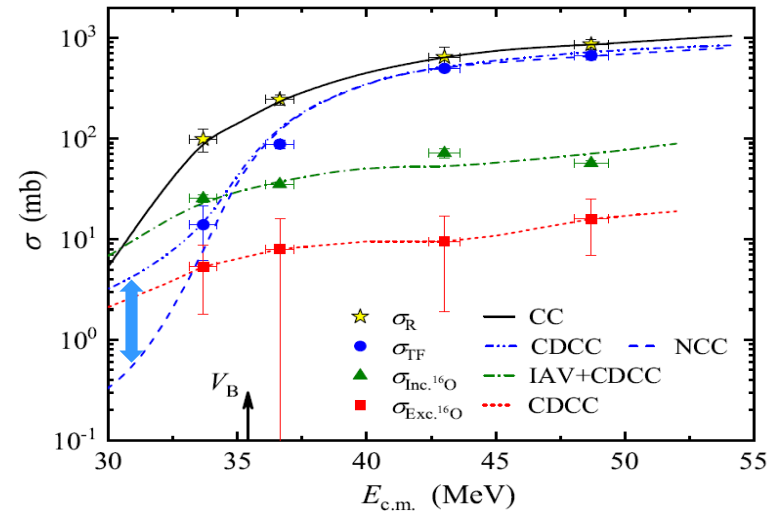
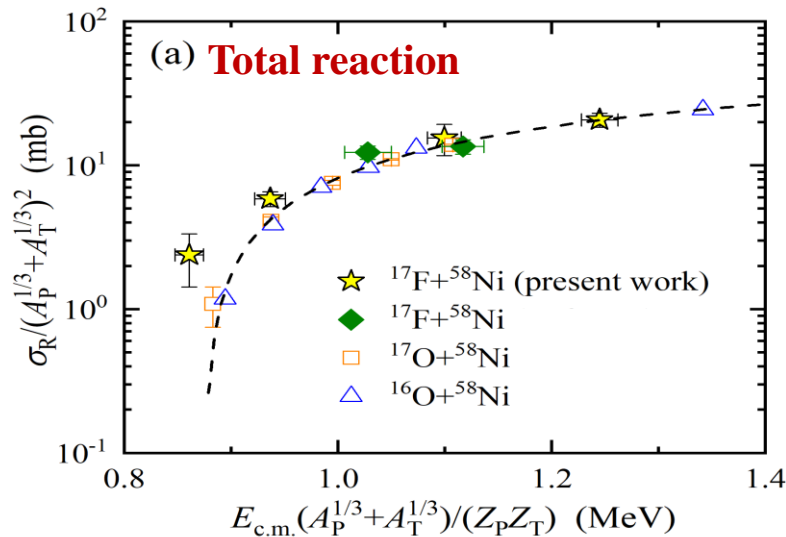
□ NEB — IAV

□ TBU — EBU+NEB

**NEB is dominant**

L. Yang, C. J. Lin, H. Yamaguchi *et al.*, Phys. Lett. B **813**, 136045 (2021).

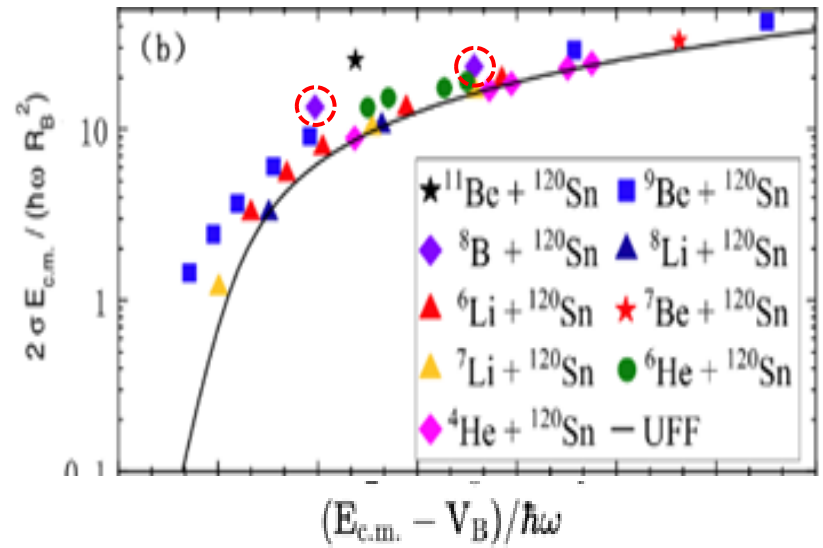
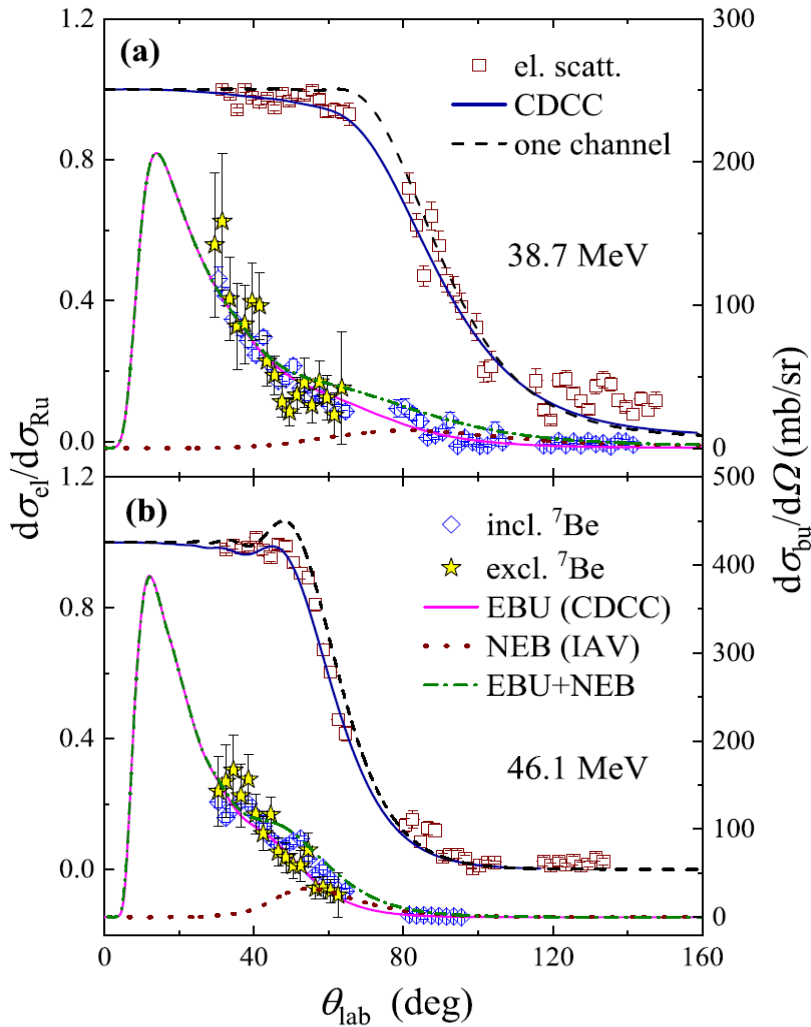
# $^{17}\text{F}+^{58}\text{Ni}$ : Cross Sections



★ Cross section of total fusion is enhanced below the barrier, mainly due to the couplings to the continuum states.

L. Yang, C. J. Lin, H. Yamaguchi *et al.*, Phys. Lett. B **813**, 136045 (2021).

# $^8\text{B} + ^{120}\text{Sn}$ : Elastic Breakup

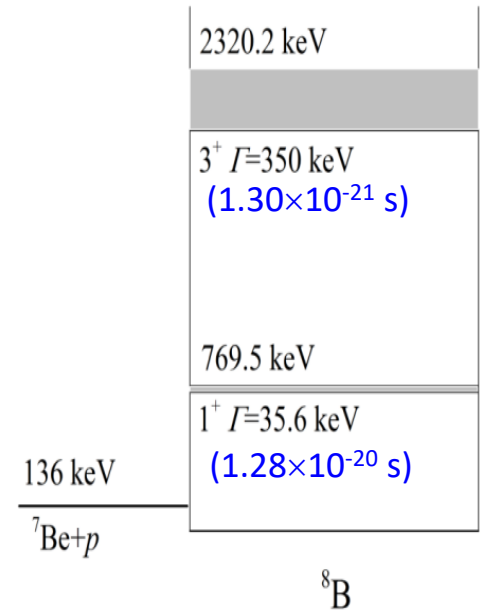
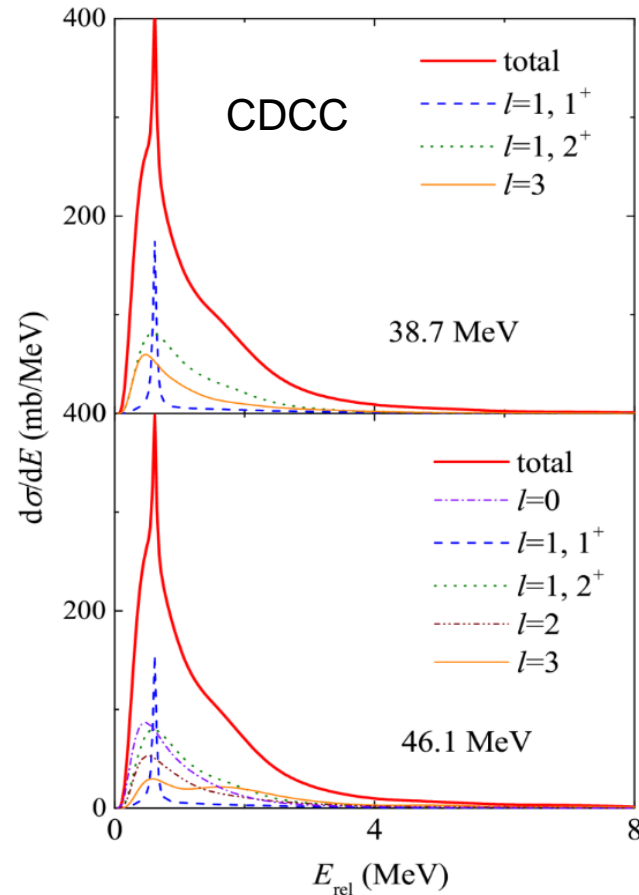
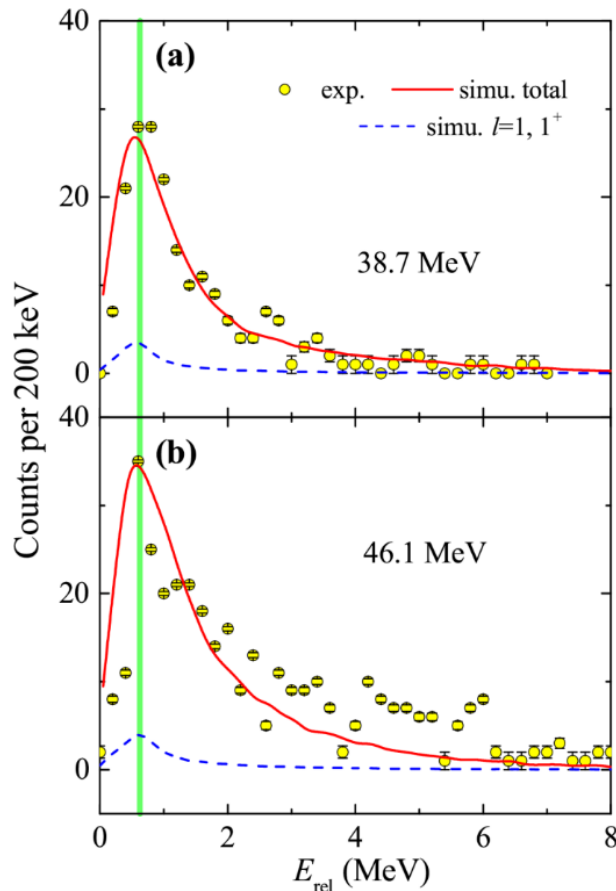


- Couplings to the continuum cannot be neglected;
- The yield of  $^7\text{Be}$  is almost exhausted by **breakup reaction**;
- **EBU is dominant**, the contribution of **NEB is ~18%**.

L. Yang, C.J. Lin, H. Yamaguchi *et al.*, Nat. Commun.13, 7193 (2022).



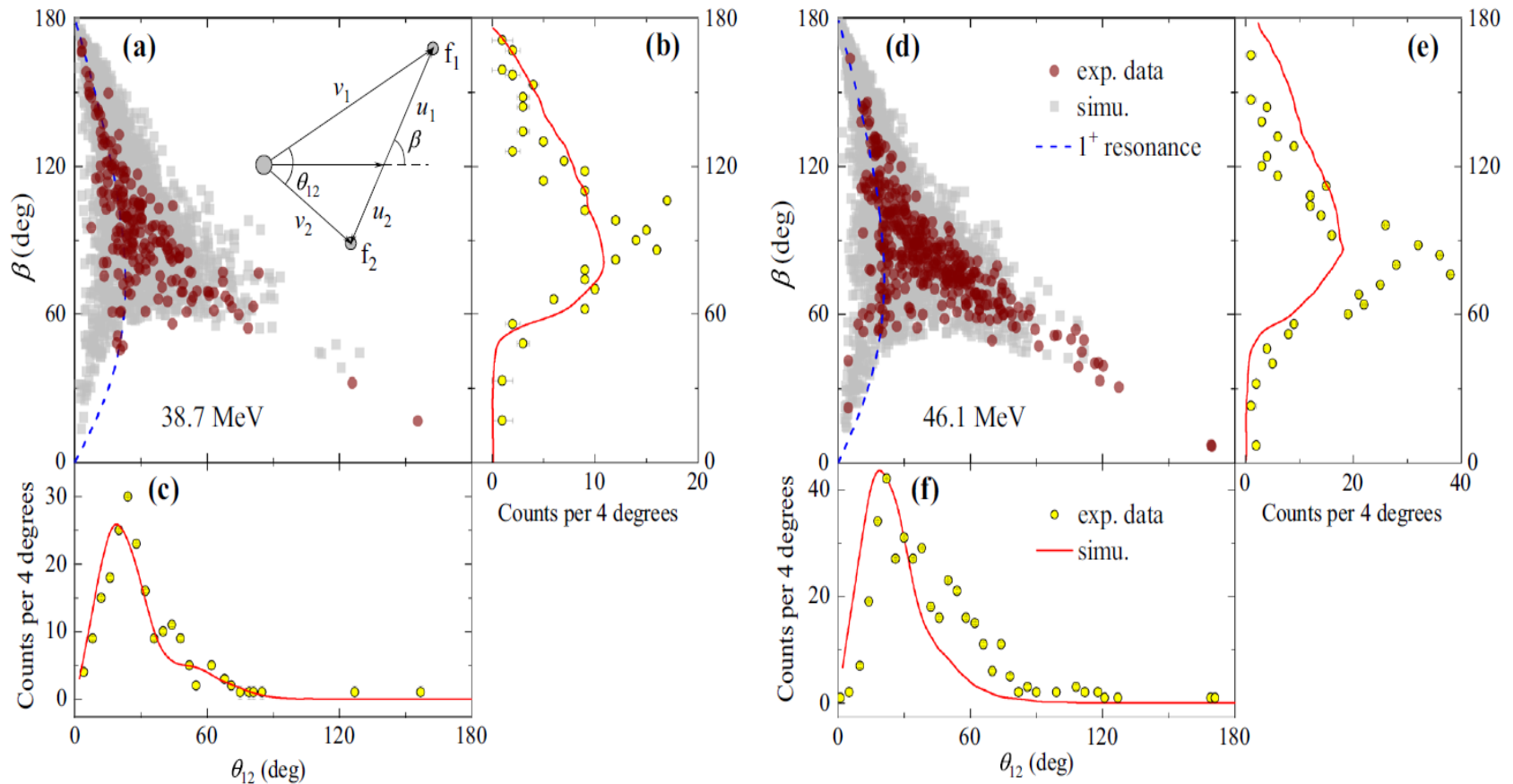
# $^8\text{B} + ^{120}\text{Sn}$ : Energy Correlations



★ Contributions of the  $1^{\text{st}}$  ex. state is  $\sim 4\%$ , indicating prompt breakups are dominant.

L. Yang, C.J. Lin, H. Yamaguchi *et al.*, Nat. Commun. **13**, 7193 (2022).

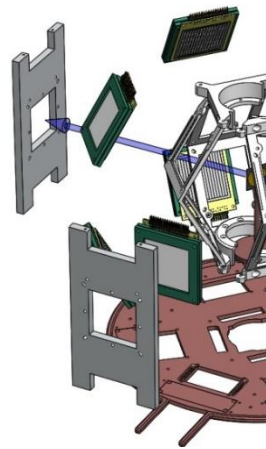
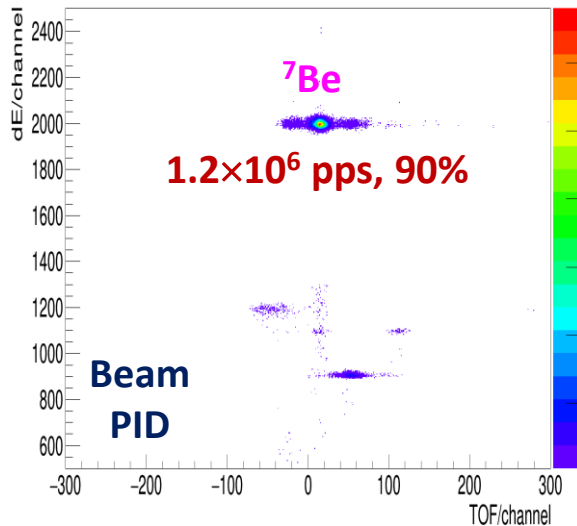
# $^8\text{B}+^{120}\text{Sn}$ : Angular Correlations



- Breakup of  $^8\text{B}$  occurs predominantly on the outgoing trajectory, close to the target.
- The continuum of  $^8\text{B}$  breakup may not significantly influence the complete fusion.

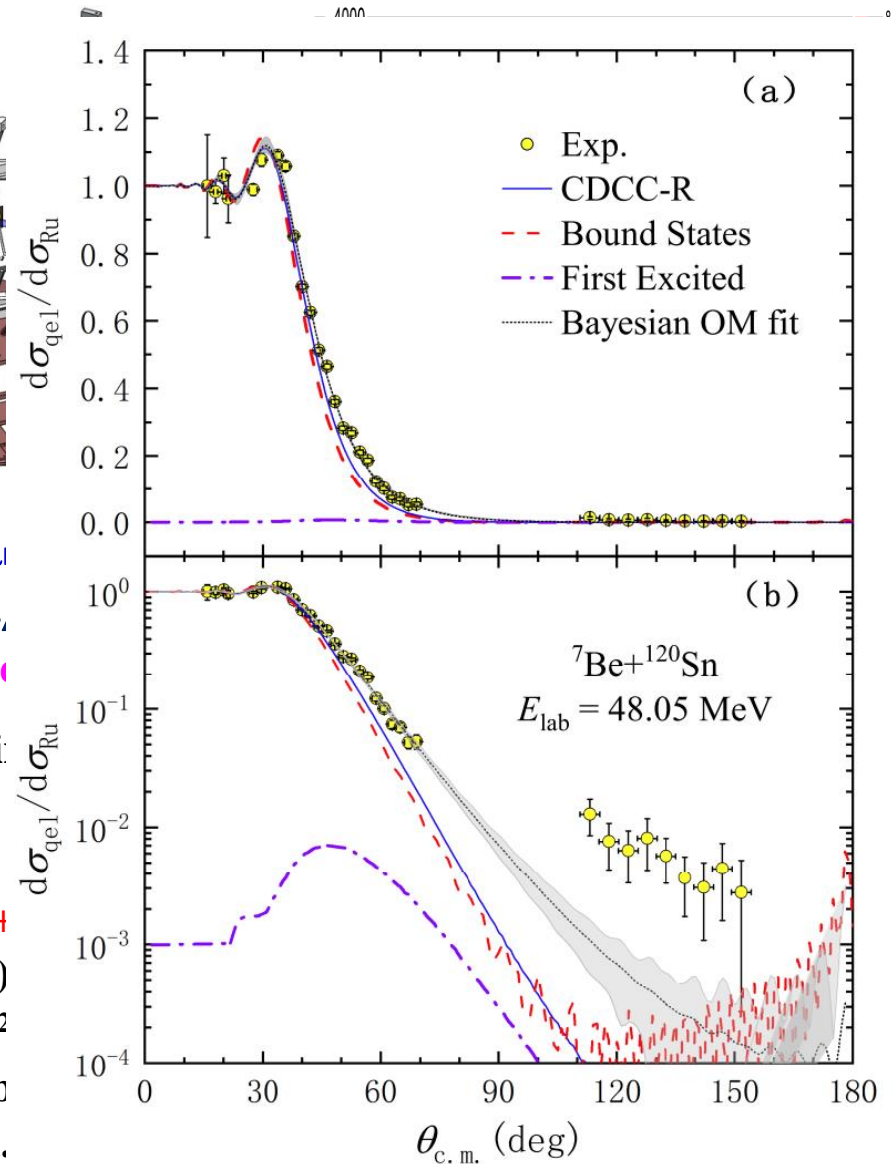
L. Yang, C.J. Lin, H. Yamaguchi *et al.*, Nat. Commun.**13**, 7193 (2022).

# In Progress: ${}^7\text{Be}+{}^{209}\text{Bi}, {}^{120}\text{Sn}$



$p({}^7\text{Li}, {}^7\text{Be})n$   $20/40\mu\text{m SSD} + 300\mu\text{m}$   
 ${}^7\text{Li}$ : 8.8 MeV/u, 1.5 euA  $10$  group of  $\Delta E_1$   
 $\text{H}_2$  gas: 1000 mbar, 8 cm, 90 K  $40\%$

1. Exclusive breakup:  ${}^7\text{Be} \rightarrow {}^3\text{He}+{}^4\text{He}$  (coi
2.  ${}^4\text{He}$  stripping:  ${}^7\text{Be}+{}^{209}\text{Bi} \rightarrow {}^3\text{He}+{}^{213}\text{At}$ ;
3.  ${}^3\text{He}$  stripping:  ${}^7\text{Be}+{}^{209}\text{Bi} \rightarrow {}^4\text{He}+{}^{212}\text{At}$ ;
4.  $1n$  stripping:  ${}^7\text{Be}+{}^{209}\text{Bi} \rightarrow {}^6\text{Be}(\rightarrow {}^4\text{He}+p+)$
5.  $1n$  pickup:  ${}^7\text{Be}+{}^{209}\text{Bi} \rightarrow {}^8\text{Be}(\rightarrow {}^4\text{He}+{}^4\text{He})$
6.  $1p$  striping:  ${}^7\text{Be}+{}^{209}\text{Bi} \rightarrow {}^6\text{Li}(\rightarrow {}^4\text{He}+d)+^2$
8.  $1p$  pickup:  ${}^7\text{Be}+{}^{209}\text{Bi} \rightarrow {}^8\text{B}(\rightarrow ???)+{}^{208}\text{Pb}$
9. Fusion:  ${}^7\text{Be}+{}^{209}\text{Bi} \rightarrow {}^{216}\text{Fr} \rightarrow \alpha, p, n$  eva.



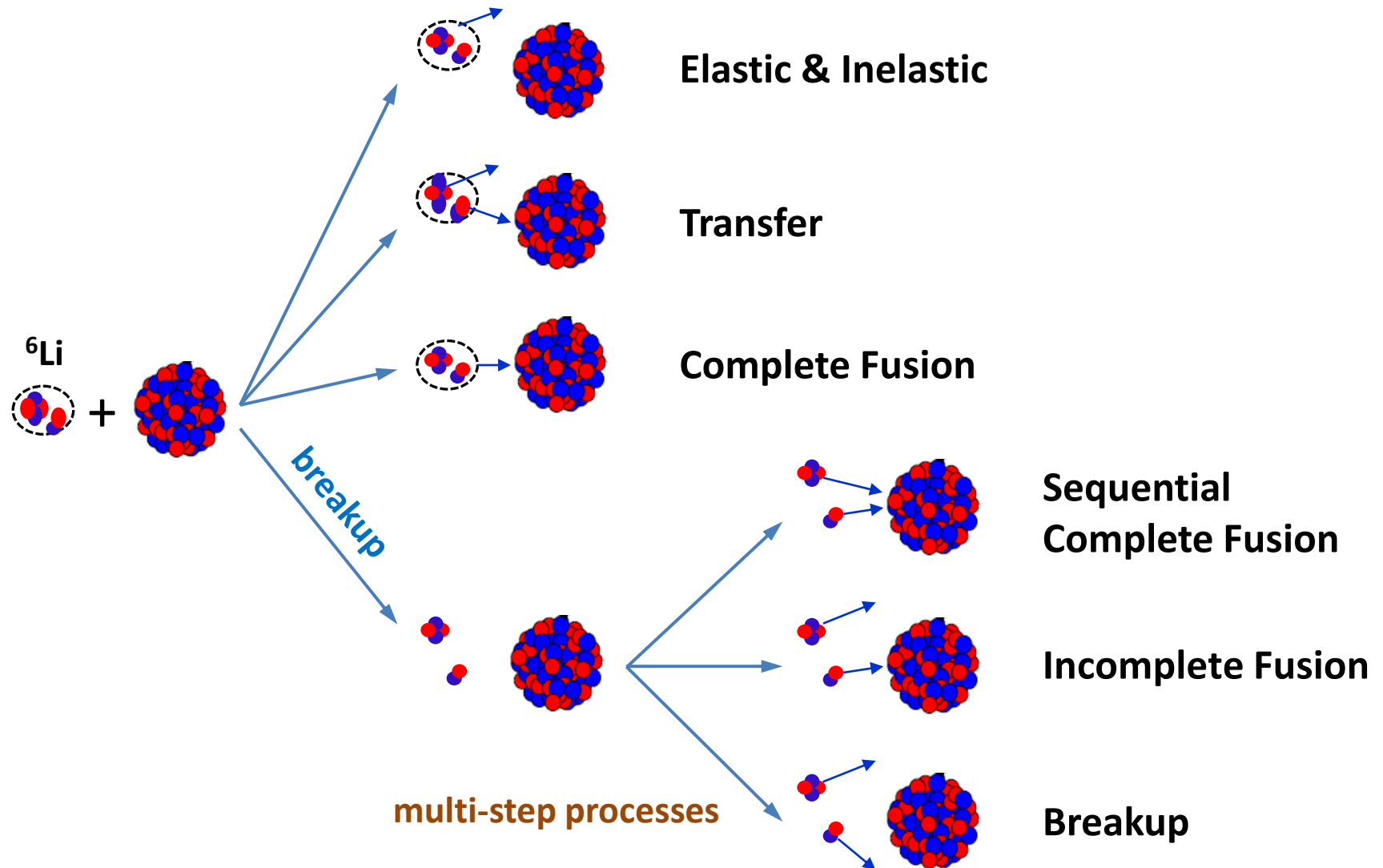
# Summary and Outlook

- ★ **Optical potentials** of both  ${}^6\text{He}+{}^{209}\text{He}$  and  ${}^6\text{Li}+{}^{208}\text{Pb}$  show a phenomenon of **abnormal “threshold anomaly”**, where the **dispersion relation** is NOT applicable. Further investigations are strongly desired to explore the underlying physics.
- ★ Rich information on **breakups of  ${}^{6,7}\text{Li}+{}^{209}\text{Bi}$**  has been obtained experimentally (e.g. energy & angular correlations), waiting for a fully understanding.
- ★ For  ${}^{17}\text{F}$ , **NEB** is dominant, and total fusion is enhanced below the barrier; for  ${}^8\text{B}$ , **EBU** is dominant, occurring promptly on the outgoing trajectory.
- ★ More system with exotic nuclei are required to understand the **dynamics of open quantum systems**.

# Thank you for your attention!

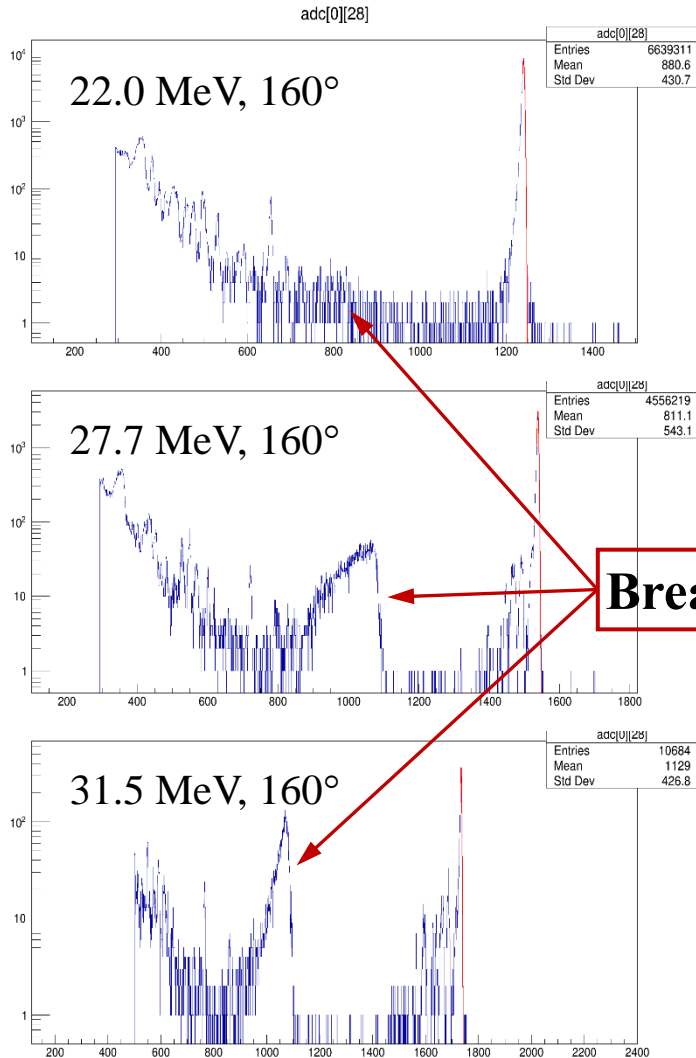


# Reactions with Weakly-bound Nuclei

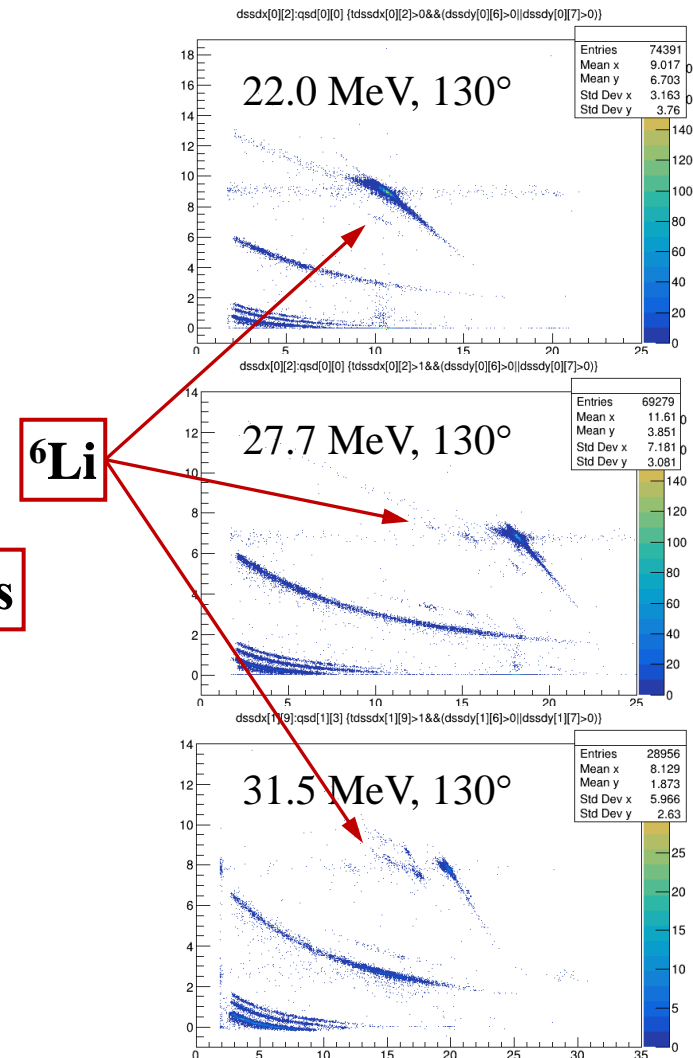


# Experimental Spectra

## ${}^6\text{Li}+{}^{208}\text{Pb}$ elastic scattering



## ${}^{207}\text{Pb}({}^7\text{Li}, {}^6\text{Li}){}^{208}\text{Pb}$ transfers





# Detector Arrays

